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Downscaling MODIS-derived maps using GIS and boosted regression trees: the case of frost occurrence over the arid Andean highlands of Bolivia

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Abstract

Frost risk assessment is of critical importance in tropical highlands like the Andes where human activities thrive at altitudes up to 4200 m, and night frost may occur all year round. In these semi-arid and cold regions with sparse meteorological networks, remote sensing and topographic modeling are of potential interest for understanding how physiography influences the local climate regime. After integrating night land surface temperature from the MODIS satellite, and physiographic descriptors derived from a digital elevation model, we explored how regional and landscape-scale features influence frost occurrence in the southern altiplano of Bolivia. Based on the high correlation between night land surface temperature and minimum air temperature, frost occurrence in early-, middle- and late-summer periods were calculated from satellite observations and mapped at a 1-km resolution over a 45000 km² area. Physiographic modeling of frost occurrence was then conducted comparing multiple regression (MR) and boosted regression trees (BRT). Physiographic predictors were latitude, elevation, distance from salt lakes, slope steepness, potential insolation, and topographic convergence. Insolation influence on night frost was tested assuming that ground surface warming in the daytime reduces frost occurrence in the next night. Depending on the time period and the calibration domain, BRT models explained 74% to 90% of frost occurrence variation, outperforming the MR method. Inverted BRT models allowed the downscaling of frost occurrence maps at 100-m resolution, illustrating local processes like cold air drainage. Minimum temperature lapse rates showed seasonal variation and mean values higher than those reported for temperate mountains. When applied at regional and subregional scales successively, BRT models revealed prominent effects of elevation, latitude and distance to salt lakes at large scales, whereas slope, topographic convergence and insolation gained influence at local scales. Our results highlight the role of daytime insolation on night frost occurrence at local scale, particularly in the early- and mid-summer periods when solar astronomic forcing is maximum. Seasonal variations and interactions in physiographic effects are also shown. Nested effects of physiographic factors across scales are discussed, as well as potential applications of physiographic modeling to downscale ecological processes in complex terrains.

Key words

altiplano; Andes; Bolivia; boosted regression trees; DEM; downscaling; frost risk mapping; MODIS; physiography; temperature lapse rate; topoclimate model; satellite land surface temperature; seasonal variation; spatial variation
1. Introduction

Low air temperature is one of the most important factors controlling vegetation zonation and key processes such as evapotranspiration, carbon fixation and decomposition, plant productivity and mortality in natural and cultivated mountain ecosystems (Chen et al., 1999; Nagy et al., 2003). Depending on vegetation structure, landscape position or soil properties, frost can damage plant tissues thus affecting forest, pasture and crop productivity (Blennow & Lindkvist, 2000). These damages have consequences for human populations, particularly in the tropics where highlands often remain densely populated (Grötzbach & Stadel, 1997). In the Andes of Argentina, Bolivia, Chile, Ecuador and Peru agriculture thrives at altitudes up to 4200 m (Del Castillo et al., 2008) and treeline reaches its world’s highest elevation up to 5100 m (Hoch & Körner, 2005) in spite of night frost occurring on more than 300 days practically spread all over the year (Garcia et al., 2007; Gonzalez et al., 2007; Rada et al., 2009; Troll, 1968). In the southern Andes, sparsely vegetated areas juxtaposing extended flat plains around salt lakes and steep slopes on the cordilleras and volcanos, display semi-arid and desert landscapes largely dominated by terrain structure. Subjected to the night/day and sunlit/shaded slope contrasts characteristic of the mountain climate, this environment is well suited for examining the influence of regional and landscape-scale physiography on the local climate regime, and particularly frost occurrence.

Several studies on topoclimate in highlands showed that elevation and slope are the main explanatory variables in modeling local climate spatial variability (Chuanyan et al., 2005). By means of digital elevation models and astronomical equations, the potential insolation (incoming solar radiation) has been included as an additional independent variable in some of these models, substantially improving their capacity to predict free-air as well as soil-surface temperature distributions (Benavides et al., 2007; Blennow & Lindkvist, 2000; Fridley 2009; Fu & Rich, 2002). Among the physiographic variables, elevation and slope steepness are known to influence cold air drainage at night and, hence, the distribution of frost risks at landscape scale (Lundquist et al., 2008; Pypker et al., 2007a). In the daytime, slope aspect and physiographic shading effects control the effective radiation load per unit of soil areas, resulting in very contrasted values of daily maximum soil temperature (Fu & Rich, 2002). Minimum night temperature might be sensitive to insolation during the previous day, since soil surface warming during that day could dampen soil radiative cooling in the next night. Though challenged by studies on minimum air temperature variations in moderately high mountains under temperate climate (Blennow 1998; Dobrowski et al., 2009), this hypothesis should be tested in the central part of the Andes, where low latitude, high elevation (typically ranging between 3600 and 4200 m) and sparse vegetation result in much greater radiation load and thermal contrasts across shaded and sunlit areas. Besides, using a downscaling approach, Fridley (2009) noticed that the lack of relationship between daytime radiation and nighttime temperature is true at local scale lower than 1000 m but not at regional scale (Great Smoky Mountains, USA), where variations in radiation balance across locations do influence nighttime temperature distribution particularly in cooler situations. Considering the Andes, recent work by Bader & Ruijten (2008) and Bader et al. (2008) used topographic modeling and remote sensing data to examine the response of vegetation distribution to climate warming, but we should go back to Santibañez et al. (1997) and François et al. (1999) to find studies on the links between frost
climatology and physiography over this region. These early works were not continued, and the case of the Andean highlands remained poorly documented in spite of the potential interest of that region, densely populated and representative of the tropical mountains vulnerable to global warming (Vuille et al., 2008).

Analyzing topographic effects on free-air or land surface temperature also led to reevaluate the simplifying assumption of a generic environmental lapse rate (the decrease in free-air temperature as elevation rises, typically assumed to be -0.6 °C per 100 m), commonly applied in hydrological and ecological studies to extrapolate air temperature in mountain areas. In fact, several studies show temperature lapse rate variations due to seasonality, height above the ground, or ground surface characteristics (Blandford et al., 2008; Dobrowski et al., 2009; Fridley 2009; Lookingbill & Urban, 2003; Marshall et al., 2007), though no detailed reports were published for the Central Andes.

Most of the above mentioned studies used multiple linear regression for modeling the influence of physiography on free-air or soil-surface temperatures. The present study resorts to an advanced form of regression, the boosted regression trees (BRT). BRT use the boosting technique to combine large numbers of relatively simple tree models to optimize predictive performance. BRT have been used successfully in human biology (Friedman and Meulman 2003), land cover mapping (Lawrence et al., 2004), biogeography (Parisien & Moritz, 2009), species distribution (Elith et al., 2008), and soil science (Martin et al., 2009). They offer substantial advantages over classical regression models since they handle both qualitative and quantitative variables, can accommodate missing data and correlated predictive variables, are relatively insensitive to outliers and to the inclusion of irrelevant predictor variables, and are able to model complex interactions between predictors (Elith et al., 2008; Martin et al., 2009). Though direct graphic representation of the complete tree model is impossible with BRT, the model interpretation is made easy by identifying the variables most relevant for prediction, and then visualizing the partial effect of each predictor variable after accounting for the average effect of the other variables (Friedman & Meulman, 2003).

The aims of the present work were: i) to explore how regional and landscape-scale physiography influence frost occurrence in Andean highlands through integration of field and remote sensing data, digital terrain analysis, and GIS, ii) to downscale regional frost occurrence maps at a level relevant for farming and land management decisions using BRT models. This study was focused on the austral summer period, from November to April, when frost holds the greatest potential impact for local farming activities.

2. Material and methods

2.1. Study area and regional climate

The study area was located at the southwest of the Bolivian highlands, near the borders of Argentina and Chile, between 19°15’ and 22°00’ South and between 66°26’ and 68°15’ West. This region, boarded by the western Andes cordillera, is characterized by the presence in its centre of a ca.100 x 100 km dry salt expanse, the Salar of Uyuni, while another salt lake, the Salar of Coipasa, lies at the north of the study area. The landscapes show a mosaic of three types of land units: more or less extended flat shores surrounding the salt lakes (elevation ca. 3650 m) and an alternation of valleys and
volcanic relieves (culminating at 6051 m) in the hinterland. The native vegetation of this tropical Andean ecosystem, also known as puna, consists of a mountain steppe of herbaceous and shrub species (e.g. *Baccharis incarum*, *Parastrephia lepidophylla*, and *Stipa spp.*) (Navarro & Ferreira, 2007) traditionally used as pastures but progressively encroached by the recent and rapid expansion of quinoa crop (*Chenopodium quinoa* Willd.) (Vassas et al., 2008).

Due to its low latitude and high elevation, the study area is characterized by a cold and arid tropical climate. Average precipitations vary between 100 and 350 mm year\(^{-1}\) from the South to the North of the region (Geerts et al., 2006), presenting an unimodal distribution with a dry season from April to October. The annual average temperature (close to 9 °C) hides daily thermal amplitudes higher than seasonal amplitudes, of up to 25 °C (Frère et al., 1978). These particular thermal conditions lead to high frost risks throughout the year. Advections of air masses from the South Pole represent only 20% of the observed frosty nights (Frère et al., 1978) and are four times less frequent in the summer than during the winter, when the intertropical convergence zone goes northward (Ronchail, 1989). Therefore, the main climatic threat lies in radiative frost, occurring during clear and calm nights. As reported by local peasants, frost occurrence shows a strong topographical and orographical dependence, as well as a marked seasonality. This seasonality lead us to split the active vegetation period into three time periods characterizing the mean regional climate dynamics in the summer rainy season: November-December when precipitation and minimum temperature rise progressively, January-February when precipitation and temperature are at their maximum, and March-April when both begin to decrease.

2.2. Data

2.2.1. Meteorological ground data

In the study area, daily air temperature records were available in three meteorological stations: one at Salinas de Garci Mendoza (19°38’S, 67°40’W) managed by the SENAMHI (Meteorology and Hydrology National Service, Bolivia) where daily minimum air temperature (Tn) was recorded in 1989 and from 1998 to 2006, and two others at Irpani (19°45’S, 67°41’W) and Jirira (19°51’S, 67°34’W) where meteorological stations set up by the IRD (Research Institute for Development, France) recorded semi-hourly air temperature from 23 November 2005 to 18 February 2006 in Irpani, and from 6 November 2006 to 31 December 2007 in Jirira. This dataset was temporally and spatially insufficient to interpolate frost risks at a regional scale, but it allowed to establish the relationship between air temperature and remotely sensed land surface temperature.

2.2.2. Remotely sensed data

The two sensors, Terra and Aqua, of the satellite system MODIS give daily images of the Earth radiative land surface temperature. Images from the fifth version of the MYD11A1 MODIS product were concatenated and projected in the UTM-19S (Universal Transverse Mercator 19 South) coordinate system using the MODIS projection tool. In this way, daily 1-km resolution images of the radiative land surface temperature (Ts) over the study area were obtained. Ts images recorded by the Aqua sensor around 2 a.m. were used as they were closer to the Tn data recorded at ground level and closer to the true physiological conditions experienced by the vegetation (François et al., 1999). Time series of nominal 1-km spatial resolution MODIS data were downloaded from NASA’s EOS data gateway
(https://wist.echo.nasa.gov/) from 20 July 2001 to 25 April 2006 and from 01 January 2007 to 31 December 2007. Due to the particular surface properties of the salt lakes of Coipasa and Uyuni in terms of surface moisture and radiative emissivity, parameter estimations were considered dubious there and Ts data for the salt lakes were discarded from the analysis. This database was managed and analyzed using the ENVI 4.2. software (ITT Visual Information Solutions, www.itvis.com). The statistical correspondence between Tn data recorded in the meteorological stations of Salinas, Irpani and Jirira and Ts data of the pixels including these three localities was examined by linear regression and Pearson correlation.

Apart from Ts measurements during clear nights, MODIS images also bring information about the possible presence of clouds between the Earth surface and the satellite at the time of the record. The information of these “flagged” images is valuable for our purpose since radiative frost would not occur during cloudy nights. The frequency of cloudy pixels in the daily MODIS images was thus calculated and used in the frost occurrence calculation (see below).

2.2.3. Digital elevation model and physiographic predictors

The SRTM digital elevation model (Farr et al., 2007) with a 90 m horizontal resolution and a vertical accuracy better than 9 m was used after resampling to 100 m to make easier the correspondence between the digital elevation model and the MODIS images at 1-km scale. In a GIS environment using Idrisi Kilimanjaro, Envi 4.2. and ArcMap 9.2. softwares, eight physiographic variables were calculated at a 100-m resolution for each location to examine their potential role in the spatial determinism of frost and to downscale frost maps to levels closer to those of frost impacts on anthropic activities (Table 1). The compound topographic index (CTI) was used as an index of cold air drainage (Gessler et al., 2000), with low CTI values representing convex positions like moutain crests and with high CTI values representing concave positions like coves or hillslope bases. Three insolation variables (DPI, MPI and API) were calculated by the ArcMap 9.2. solar analysis tool. They express the amount of radiative energy received across all wavelengths over the course of a typical seasonal day (DPI), or from sunrise to 12:00 (MPI), or from 12:00 to sunset (API) of such a day.

These insolation variables account for site latitude and elevation, slope steepness and aspect, daily and seasonal sun angle, and shadows cast by surrounding heights. API was calculated to examine the specific influence of insolation in the afternoon just before the considered night, with the hypothesis that high soil surface insolation and warming would affect the soil energy balance, and thus reduce the risk of radiative frost in the following night (without regards to other potential factors such as soil albedo, soil water content, air humidity, etc. see Garcia et al. (2004)). Similarly, MPI was calculated as a surrogate to the early morning insolation, with the hypothesis that areas in the shade of surrounding heights in the early morning would experience cooler conditions for a longer time, thus being more vulnerable to frost than sunlit areas. In the calibration procedure, these 100-m resolution variables were upscaled at 1-km resolution by averaging 10 x 10 pixel clusters in the DEM 100-m images, thus fitting the 1-km resolution of the remotely sensed frost occurrence maps.
Table 1. Ranges of physiographic variables observed over the study area.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Minimum</th>
<th>Maximum</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>LAT latitude in UTM 19 South</td>
<td>-22.00</td>
<td>-19.24</td>
<td>decimal degree</td>
</tr>
<tr>
<td>ELE elevation</td>
<td>3540</td>
<td>6051</td>
<td>m</td>
</tr>
<tr>
<td>SLO slope steepness</td>
<td>0</td>
<td>35</td>
<td>degree</td>
</tr>
<tr>
<td>DPI daily potential insolation</td>
<td></td>
<td></td>
<td>W m⁻²</td>
</tr>
<tr>
<td>Nov-Dec</td>
<td>6900</td>
<td>9075</td>
<td></td>
</tr>
<tr>
<td>Jan-Feb</td>
<td>7040</td>
<td>8935</td>
<td></td>
</tr>
<tr>
<td>Mar-Apr</td>
<td>4604</td>
<td>7897</td>
<td></td>
</tr>
<tr>
<td>MPI morning potential insolation</td>
<td></td>
<td></td>
<td>W m⁻²</td>
</tr>
<tr>
<td>Nov-Dec</td>
<td>510</td>
<td>1861</td>
<td></td>
</tr>
<tr>
<td>Jan-Feb</td>
<td>466</td>
<td>1772</td>
<td></td>
</tr>
<tr>
<td>Mar-Apr</td>
<td>264</td>
<td>1240</td>
<td></td>
</tr>
<tr>
<td>API afternoon potential insolation</td>
<td></td>
<td></td>
<td>W m⁻²</td>
</tr>
<tr>
<td>Nov-Dec</td>
<td>2819</td>
<td>5075</td>
<td></td>
</tr>
<tr>
<td>Jan-Feb</td>
<td>2816</td>
<td>5000</td>
<td></td>
</tr>
<tr>
<td>Mar-Apr</td>
<td>2079</td>
<td>4308</td>
<td></td>
</tr>
<tr>
<td>LDS distance from salt lakes</td>
<td>0</td>
<td>5.04</td>
<td>Ln (km + 1)</td>
</tr>
<tr>
<td>CTI compound topographic index</td>
<td>5.7</td>
<td>14.1</td>
<td>-</td>
</tr>
</tbody>
</table>

2.3. Physiographic modeling of frost occurrence over regional and subregional domains

2.3.1. MODIS-derived frost occurrence

Frost is detected by remote sensing when surface temperature appears negative on cloudfree images. Based on the standard meteorological threshold of 0 °C, frost occurrence (R) for a specific time period was therefore defined as follows:

\[ R = \text{Prob} (T_s < 0 \, ^\circ\text{C}) \times F \]  

where: \( R \) = frost occurrence at the 0 °C threshold (relative probability ranging from 0 to 1), \( \text{Prob} (T_s < 0 \, ^\circ\text{C}) \) = probability of the surface radiative temperature being lower than 0°C, \( F \) = frequency of cloudless days in the considered period. Note that “frost occurrence” is used here instead of frost risk to differentiate our estimates based on 6-year daily \( T_s \) values from climatological estimates based on longer data series.

In order to calculate the probability \( \text{Prob} (T_s < 0 \, ^\circ\text{C}) \), the distribution of the random variable \( T_s \) during successive time periods (namely: November-December, January-February, March-April) was studied, checking its normality through the Kolmogorov-Smirnov test. For each 1-km pixel and each time period, \( T_s \) mean and standard deviation, cloudless day frequency (F) and, finally, frost occurrence
(R) were calculated from the available nighttime remotely sensed data series (n = 366, 355, and 361 in the ND, JF and MA periods respectively). Maps of observed (remotely sensed) frost occurrence at 1-km resolution were then generated by applying Eq. (1) for each time period.

2.3.2. Frost occurrence models over regional and subregional domains

A subsample of 1-km pixels (n = 7500) was randomly selected for the calibration of the physiography-frost occurrence relationships over the entire study area (hereafter called "regional models"). Regional BRT were built for each seasonal period (November-December, January-February, March-April) using the gbm package version 1.6-3 developed under R software (R Development Core Team 2006). A bag fraction of 0.5 was used which means that, at each step of the boosting procedure, 50% of the data in the training set were drawn at random without replacement. The loss function (LF), defining the lack-of-fit, used a squared-error criterion. The learning rate or shrinkage parameter (LR), the tree size or tree complexity (TS), the number of trees (NT) and the minimal number of observations per terminal node (MO) were the main parameters for these fittings, and were set through a tuning procedure (Martin et al., 2009). LR, determining the contribution of each tree to the model, was thus taken equal to 0.05. NT, the maximal number of trees for optimal prediction was set to 2000. For optimal prediction, TS, the maximal number of nodes in the individual trees, was set to a value of 9, and MO was set to 10 observations per terminal node. For sake of comparison, multiple linear regression models were calculated at the regional scale using the same predictors and the same calibration datasets as for the regional BRT. These "regional MR" were built using the Statistica package (StatSoft France 2005).

The regional BRT and MR models were validated comparing observed (remotely sensed) and predicted frost occurrence over the entire study area in the three time periods. This was made excluding the pixels used for calibration, which resulted in a 49353 pixels validation set. The predictive capacity of the models was analysed examining the observed versus predicted values plots, the bias (B), the root mean square error of prediction (RMSE), and the coefficient of determination of the regression between estimated and observed values (R²). Once validated, the BRT were interpreted, looking first at the relative contribution of the physiographic variables to the predictive models, and then considering the partial dependence of the predictions on each variable after accounting for the average effect of the other variables.

In order to test the scale-dependence of the predictors, a similar BRT procedure was applied over a smaller spatial domain defined by a selected range of regionally varying factors, namely: latitude between 19°5 and 20° South and elevation lower than 4200 meters (total area = 7775 km²). This spatial domain corresponds to the Intersalar, the area of major agricultural activities in the region, where local populations cultivate quinoa and rear camelids up to an altitude of ca. 4200 meters. A new set of 7500 training pixels was randomly selected from this smaller domain to calibrate these "subregional BRT", using the same values of fitting parameters and a similar validation procedure as in the previous analysis. Excluding the training pixels, this validation was conducted on the remaining 275 pixels of this smaller domain. The relative contribution of the physiographic predictors to the subregional models was
also examined. The interactions between predictive variables were considered by joint plots of their partial dependence in the subregional models.

2.3.3. **Downscaling frost occurrence prediction at 100-m resolution**

Once validated, the regional BRT were applied on each pixel of the DEM 100-m image in order to downscale frost occurrence from 1-km to 100-m resolution in the three considered time periods. An indirect validation of these 100-m frost occurrence maps was then conducted by aggregating 10 x 10 pixel clusters of 100-m frost predictions and comparing the resulting 1-km predictions to the observed (remotely sensed) frost occurrence at 1-km resolution. A qualitative validation was also conducted by examining the capacity of these 100-m maps to display well-known local patterns of frost and cold air distribution over complex terrains.

2.3.4. **Estimation of the land surface temperature lapse rate**

The regression of Ts recorded over sloping areas versus elevation of the corresponding pixels allowed to calculate average values of the land surface temperature lapse rate at night for successive dates in each considered time periods. Sloping areas were defined as terrains with slope steepness greater than 3° and elevation lower than 5000 meters. This elevation limit was chosen to discard high-altitude sites possibly covered with snow or ice which superficial thermal properties modify lapse rate estimations (Marshall et al., 2007). The resulting sampling area represented 22529 km², covering an elevation range of 1341 m (from 3659 to 5000 m).

3. **Results**

3.1. **Climate information and remotely sensed frost occurrence evaluation**

The frequency analysis of daily minimum air temperature (Tn) recorded at Salinas over 10 discontinuous years (1989, and the 1998-2006 period) was made using the standard climatological threshold of 0 °C (Fig. 1).

![Fig. 1. Frequency analysis of daily minimum air temperatures lower than 0 °C registered at Salinas in 1989 and from 1998 to 2006.](image-url)
During the austral summer (November-April), two periods of frequent below zero temperatures surround a ca. 80-day time interval of low frost occurrence, from the beginning of January to the end of March.

Daily Tn values recorded at screen height by the meteorological stations of Salinas, Irpani and Jirira were highly correlated to Ts data remotely sensed over these three localities at night by the MODIS satellite ($T_n = 0.97^*T_s + 0.93, R^2 = 0.81, n = 750$). The percentage of cloudy pixels on the MODIS images gives a general information about the seasonal pattern of cloud cover in the study area: the January-February period was the most overcast with on average $46 \pm 8.2\%$ of the study area masked by clouds in each daily satellite image, while this percentage fell to $30 \pm 7.4\%$ and $29 \pm 6.6\%$ in the November-December and March-April periods respectively. The test of Kolmogorov-Smirnov applied to
the Ts data series was statistically significant in all the cases \( P < 0.05 \). This allowed to apply a normal probability density function in equation (1) in order to generate the 1-km resolution maps in Fig. 2 showing the regional patterns of frost occurrence variations in three successive time periods as derived from satellite observations.

3.2. Physiographic modeling of frost occurrence

3.2.1. Model validation of regional and subregional BRT models

The results of the statistical comparison between observed and predicted frost occurrence at 1-km resolution in three time periods are presented in Fig. 3 and Table 2. The regional BRT clearly outperformed the MR models, the latter being affected by strong non-linearities in the high frost occurrence range, showing its poor predictive capacities in the early and late summer periods. On the other hand, the regional BRT negligibly overestimated the satellite observations with practically no bias whatever the time period. The RMSE and \( R^2 \) values showed that BRT predictions were fairly good in January-February (RMSE = 0.057, \( R^2 = 0.90 \)), and only slightly more dispersed by the beginning or the end of the summer season (RMSE between 0.07 and 0.08, \( R^2 \) between 0.78 and 0.83). With an error generally less than 8% on predicted frost occurrence values, the regional BRT thus appear suitable for predicting frost occurrence from physiographic variables alone. Table 2 shows similar performances of the regional and subregional BRT, with only higher bias for the subregional model.

3.2.2. Hierarchy of physiographic variables in regional and subregional BRT

Regional BRT showed large effects of elevation, distance from the salt lakes, latitude and CTI on frost occurrence, while slope and insolation variables had only marginal influence (Fig. 4a). Comparing the three time periods, the relative contributions of the predictive variables showed some variations, with the distance from the salt lakes dominating in the initial period (November-December), while elevation became more important from January to April, and particularly in the mid-summer period. In contrast, latitude, CTI and insolation variables kept a fairly constant effect with similar contributions at the beginning and at the end of the season. Calibrating BRT models over a limited spatial domain reveals slightly different patterns in the contributions of the predictors (Fig. 4b): distance from the salt lakes gained importance on elevation in the three time periods, and daily potential insolation showed noticeable contribution until mid-summer (though the influence of its morning and afternoon components remained marginal). The weights of CTI and latitude were intermediate whatever the time period, while the contribution of slope became important by the end of the season.
Fig. 3. Comparison of frost occurrence values observed in three time periods with frost occurrence predicted by the MR (multiple regression) and BRT regional models (ND = November-December; JF = January-February; MA = March-April, n = 49353 in each time period)

Fig. 4. Relative contributions of the physiographic variables in the regional (a) and subregional (b) BRT in three time periods. (ND = November-December; JF = January-February; MA = March-April; see Table 1 for variables abbreviations)
3.2.3. Partial dependence in regional and subregional BRT

The plots of partial dependence for frost occurrence in the regional BRT (Fig. 5) indicate that frost events in the study area occur mostly at high and medium latitude, increase continuously up to 4500 m elevation, and are more frequent far away from the salt lakes. Concave positions (high CTI values) are more prone to frost, and low daily potential insolation in those shaded areas also increases frost occurrence at night, though separating the morning and afternoon components of the daily insolation gives opposite results (data not shown). The dependence of frost occurrence on slope steepness remained fairly constant. These partial responses of frost occurrence to the most active physiographic variables show only limited seasonal changes.

![Partial dependence plots of the six most influential physiographic variables in the regional BRT in three time periods (continuous line: November-December, dashed line: January-February, dotted line: March-April; ticks at the inside top of the plots show deciles of site distribution across the variable; see Table 1 for variables abbreviations).](image)

More details emerge from the partial dependence plots of interactions in subregional BRT (Fig. 6 illustrating the January-February period, with similar results in the other two periods). For instance, up to a distance of 10 km from the salt lakes (LDS ≈ 4.0) the effect of elevation on frost occurrence is low and nearly constant below 3900 m, and then rises gradually above that level. But farther than 10 km
away from the salt lake borders, frost occurrence first decreases as elevation rises up to 3900 m and then increases sharply above. This suggests that thermal inversions at night are more frequent at distance from the salt lakes. Considering the interaction of elevation with CTI, while frost occurrence at low elevation increases gradually up to CTI values of 9 and more sharply thereafter (concave situations), at high elevation the effect of CTI is already important at values below 8 and then rose only marginally. The effect of landscape concavity thus appears prominent at low elevation, where cold air can accumulate in local depressions, while it becomes negligible at high elevation where crests and peaks dominate.

Fig. 6. Joint partial dependence plots of some interactions between topographic variables in the subregional BRT of the January-February period (see Table 1 for variables abbreviations).
Table 2. Validation statistics of frost occurrence multiple regression (MR) and boosted regression trees (BRT) models calibrated over the entire study area (regional models) or the Intersalar area (subregional models). B: bias; RMSE: root mean square error of prediction; R2: determination coefficient of the regression line between observed and predicted values. ND = November-December; JF = January-February; MA = March-April.

<table>
<thead>
<tr>
<th>Calibration procedure</th>
<th>Period</th>
<th>B</th>
<th>RMSE</th>
<th>R²</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regional MR (n = 49353)</td>
<td>ND</td>
<td>2.7 \times 10^{-5}</td>
<td>0.129</td>
<td>0.45</td>
</tr>
<tr>
<td></td>
<td>JF</td>
<td>2.1 \times 10^{-4}</td>
<td>0.093</td>
<td>0.72</td>
</tr>
<tr>
<td></td>
<td>MA</td>
<td>8.5 \times 10^{-4}</td>
<td>0.110</td>
<td>0.59</td>
</tr>
<tr>
<td>Regional BRT (n = 49353)</td>
<td>ND</td>
<td>1.7 \times 10^{-5}</td>
<td>0.082</td>
<td>0.78</td>
</tr>
<tr>
<td></td>
<td>JF</td>
<td>0.5 \times 10^{-5}</td>
<td>0.057</td>
<td>0.90</td>
</tr>
<tr>
<td></td>
<td>MA</td>
<td>0.6 \times 10^{-5}</td>
<td>0.071</td>
<td>0.83</td>
</tr>
<tr>
<td>Subregional BRT (n = 275)</td>
<td>ND</td>
<td>2.9 \times 10^{-5}</td>
<td>0.062</td>
<td>0.80</td>
</tr>
<tr>
<td></td>
<td>JF</td>
<td>1.4 \times 10^{-3}</td>
<td>0.031</td>
<td>0.82</td>
</tr>
<tr>
<td></td>
<td>MA</td>
<td>2.9 \times 10^{-3}</td>
<td>0.049</td>
<td>0.82</td>
</tr>
</tbody>
</table>

3.3. Fine resolution frost occurrence maps

Regional BRT were used in prediction to downscale frost occurrence maps from the 1-km to the 100-m scale. The statistical validation conducted on reaggregated 1-km pixel clusters shows good fit between predicted and observed (remotely sensed) frost occurrence values (Table 3), with RMSE of predicted values of the same order than in the BRT regional model directly applied at the 1-km resolution (Table 2). The 100-m scale maps display topoclimatic variations resulting in a detailed zonation of frost occurrence. As an example, Fig. 7c-d shows that flat areas surrounding Mount Tunupa are more prone to frost occurrence than the slopes of the volcano up to an elevation of approximately 4000 m, while sites located at higher altitudes are naturally colder. All over this area, east-facing slopes appear less exposed to frost than west-facing slopes. In some particular places at the west, cold air stagnation is also identifiable in the lower parts of local depressions. Such details were not visible on the 1-km resolution map (Fig. 7b).

Table 3. Statistical comparison of 100-m frost occurrence predictions reaggregated at 1-km with observed 1-km frost occurrence values (n = 49353). B: bias; RMSE: root mean square error of prediction; R2: determination coefficient of the regression line between observed and predicted values. ND = November-December; JF = January-February; MA = March-April.

<table>
<thead>
<tr>
<th>Period</th>
<th>B</th>
<th>RMSE</th>
<th>R²</th>
</tr>
</thead>
<tbody>
<tr>
<td>ND</td>
<td>0.0252</td>
<td>0.0925</td>
<td>0.74</td>
</tr>
<tr>
<td>JF</td>
<td>0.0008</td>
<td>0.0644</td>
<td>0.87</td>
</tr>
<tr>
<td>MA</td>
<td>0.0543</td>
<td>0.0945</td>
<td>0.80</td>
</tr>
</tbody>
</table>
Fig. 7. Elevation map of the Mount Tunupa area (a), and frost occurrence in the March-April period mapped at 1-km resolution from MODIS observations (b), at 100-m resolution (c) and in 3-D view using regional BRT (d). Frost occurrence is scaled between 0 and 1 as the probability of daily occurrence of negative Ts values in the March-April period.

3.4. Lapse rate estimation

Table 4 shows significant seasonal variations in the average lapse rate in land surface night temperature calculated over the study area, with statistically stronger values in the mid-summer period (-0.64 °C/100 m) in comparison with the beginning or the end of the season (ca. -0.60 °C/100 m). The
The present study provides the first application of MODIS products to characterize frost occurrence over a 45,000 km² area in the Andean highlands. Frost occurrence over the summer period was either calculated directly from land surface temperature remotely sensed at a 1-km scale, or estimated and downscaled at 100-m by means of physiographic modeling. To our knowledge this is also the first application of BRT in physiographic modeling. Both techniques are complementary in characterizing frost occurrence: remote sensing brings spatialized and repetitive information on land surface temperature and physiographic features, while BRT allow to explore the relative contribution of physiographic factors at various scales and, hence, to downscale satellite information to a level appropriate to farming and land management applications.

### 4.1. Application of remote sensing data for frost occurrence characterization

As pointed by François et al. (1999) at least three factors may potentially affect the relation between Ts and Tn records: a difference in time (ca. 6 a.m. for minimum night air temperature versus 2 a.m. for satellite radiative temperature), a difference in height (1.5 m above the soil surface for meteorological data versus land surface temperature for satellite data), and a difference in spatial resolution (ca. 100 m² footprint for local meteorological data versus 1 km² for satellite data). In spite of this, these authors observed only a stable shift of some degrees between Tn records in the Bolivian altiplano and Ts registered at 2 a.m. with a 1-km spatial resolution by the NOAA/AVHRR satellite. A similar result was found in the present study showing a linear and highly significant correlation of MODIS land surface temperature at night with minimum air temperature recorded in meteorological stations ($R^2 = 0.81$). However, this validation may be biased since, as in most mountain areas in the world, the available meteorological records are likely not representative of the most elevated and isolated parts of the study area. Regarding the MODIS satellite, recent studies have improved and validated its calibration algorithm for land surface temperature in various situations encompassing Bolivian highlands, semiarid and arid regions, or nighttime/daytime overpasses (Wan, 2008; Wang et al., 2008). This ensures the reliability of MODIS temperature data in the study area in spite of its specific location in cold and arid tropical highlands. After verifying for the normality of the distribution of Ts data, the probability of frost occurrence was estimated.
occurrence can be easily calculated from the available satellite data series (eq. (1)). It should be noted that the available series of 6-year daily records was long enough to statistically characterize frost occurrence at the standard meteorological threshold of 0 °C, but not at lower temperature levels due to the scarcity of observations of severe frost events over the considered period. Frosts at -4 or -7 °C would, however, be more relevant for agroclimatic purposes since they correspond to the frost tolerance levels of major Andean crops such as potato and quinoa (Bois et al., 2006; Garcia et al., 2007; Geerts et al., 2006; Jacobsen et al., 2005). This limitation should progressively disappear as the MODIS archives grow and allow for the statistical evaluation of less frequent (and more severe) frost events.

4.2. Spatial and temporal patterns of frost occurrence

4.2.1. Frost occurrence as affected by regional physiography and climate seasonality

The frost occurrence maps derived from MODIS data at 1-km resolution (Fig. 2) clearly show the influence of regional-scale physiography like the mountain distribution or the proximity of the salt lakes, as well as the seasonal variation of frost occurrence over a 6-month period. In their attempt to map agroclimatic suitability in the Bolivian altiplano, Geerts et al. (2006) notice that frost risk is difficult to interpolate spatially. Nevertheless, based on data from 41 ground climatic stations of the altiplano, they achieve a description of regional frost risk patterns that are globally confirmed by our satellite maps, with lower frost probabilities in the Intersalar region and higher probabilities at the south-west of the salt lake of Uyuni. Geerts et al. (2006) also mention that their kriging interpolation was improved by incorporating a WNW anisotropy due to the combined north-south influence of the Lake Titicaca and the west-east effect of zonal winds. These zonal winds affect the entire altiplano and largely control the synoptic weather types (Garreaud et al., 2003). As demonstrated in other cold regions or mountain areas in the world (Blandford et al., 2008; Dobrowski et al., 2009; Marshall et al., 2007), the occurrence and spatial patterns of the zonal winds could be important drivers of the seasonal variation in land surface temperature and temperature lapse rate found in the study area.

Another driver of frost seasonality is cloud cover which, in a typical tropical unimodal rainy season, results in progressive overcasting at the beginning of the rainy season, maximum cloud cover in the mid-season, and then progressive decrease by the end of the season. This cloud cover pattern is recorded daily at the 1-km scale by the MODIS satellite and was integrated in the calculation and mapping of frost occurrence (equation 1, Fig. 2).

The seasonal change in sky cloudiness also influences temperature lapse rates. Blandford et al. (2008) thoroughly discuss the effect of seasonal and synoptic conditions on lapse rate calculated for average or daily extreme values of near-ground temperature in temperate mountains. They outlined that minimum temperature lapse rate are shallower when air masses are dry and cold, which is explained by increased frequency of cold air drainage and temperature inversions under clear-sky and dry air conditions at night. Minimum temperature lapse rate values are also more variable during seasonal transition between summer and winter, due to fluctuating weather regime at that time and higher frequency of temperature inversions. Our estimates of minimum temperature lapse rate in successive time periods (Table 4) are consistent with both assertions, showing steeper and less variable values in mid-summer (January-February) when the sky is more cloudy and air conditions are relatively humid,
temperate, and stable. These estimates approximating –0.6 °C/100 m appear fairly high compared to minimum temperature lapse rate values, typically ranging from –0.15 to –0.35 °C/100 m, in mountains of mid-latitude regions (Blandford et al., 2008; Dobrowski et al., 2009; Harlow et al., 2004). In subtropical mountains however, De Scally (1997) states that, due to their high thermal regime, the temperature lapse rate is generally higher than in mid-latitude mountains. The high lapse rate values thus quoted for the Himalaya (De Scally, 1997) or the Andes (Frère et al., 1978; Snow, 1975 cited by Pielke & Mehring, 1977; Trombotto et al., 1997) refer unfortunately to mean daily or mean annual temperatures which cannot be compared directly to our estimates of minimum temperature lapse rates in specific time periods.

Astronomic forcing is another cause of seasonality in the topography-frost relationship, explaining why topographic controls, usually treated as stationary, show actually pronounced seasonal variations, as pointed by Deng et al. (2007) in the case of topography-vegetation relationships. In our study, seasonal changes in the effects of slope steepness and aspect on frost occurrence are illustrated by varying SLO and DPI contributions (Fig. 4b). They are explained by astronomical forcing resulting in insolation values in the early and mid-summer higher by 25% in average than in the late-summer period (see Table 1), thus giving higher influence of DPI over SLO in the former two periods.

Fig. 2 shows that the shores of the salt lakes are less prone to frost, while highlands at the west and south of the region are continuously exposed, even in mid-summer (January-February) when frost occurrence is generally low. This latter situation is obviously due to extreme elevation, while the "milding" effect of the salt lakes could be due to the specific thermal properties of these vast salted extenses. François et al. (1999) observed warmer night temperatures over the Coipasa and Uyuni salt lakes and suggest that water covering these lakes part of the summer, as well as the higher thermal conductivity and thermal capacity of the salted substratum, could explain that their borders remain warmer than the surrounding areas.

4.2.2. From regional to subregional physiographic influences on frost occurrence

Multiple regression methods were used in previous studies to evaluate the relative contribution of topographic factors to near-ground temperature and frost occurrence. These studies were generally conducted in mid- or high-latitude mountains (Bennie et al., 2009; Chuanyan et al., 2005; Dobrowski et al., 2009), and often in densely forested areas at mid-altitude (Blennow, 1998; Lindkvist et al., 2000; Pypker et al., 2007b). Our study explored an extended agricultural region at its extreme elevation limit in cold and arid tropical highlands. In this context, BRT models clearly outperformed multiple regression models, probably due to their capacity to include nonlinear effects and interactions between predictors (Martin et al., 2009). At the regional scale, BRT analyses show that elevation, distance to the salt lakes and latitude were the physiographic features most contributing to frost occurrence variations, while features directly or indirectly related to slope or topographic convergence (SLO, CTI, DPI, API, and MPI) were less important. These regional BRT models based on physiographic features alone explain between 78% and 90% of the variation in frost occurrence observed in different time periods (Table 2).

In their study of the influence of physiography on the distribution of climate variables across the United States, Daly et al. (2008) outline that the effects of elevation and proximity to large water bodies exceed
those of other topographic factors at large scales, whereas the effects of slope and landcover features become prominent at relatively smaller scales. In complex terrains, local variations in slope aspect and steepness create a mosaic of hillslopes experiencing contrasting climatic regimes (Daly et al., 2008), while topographic depressions are another landscape feature commonly associated with cold air drainage and frost occurrence (Lundquist et al., 2008; Pypker et al., 2007b). These local landform features emerge as forcing factors of frost occurrence at the local scale, where the range of variation in elevation and latitude became limited while that in local landscape features remained large. When applied to the reduced spatial domain of the Intersalar, our BRT analyses indeed showed that elevation lost some importance at the benefit of daily potential insolation (DPI), slope steepness (SLO), or topographic convergence (CTI) (Fig. 4b). As a major characteristic of the physiography of southwestern Bolivia, the vast salt lakes of Coipasa and Uyuni remained influential at that local scale, as shown by the high contribution of the distance to the salt lakes (LDS) in these BRT subregional models. The good fit of frost occurrence values predicted by BRT models applied either at the 100-m or the 1-km resolution (Tables 2 and 3) validates the use of BRT regional models for local frost occurrence estimations since these models were able to seize both the influences of large-scale factors like latitude and elevation, and of local factors like slope steepness, insolation, and landscape position. The resulting local mosaic of cold depressions and warmer slopes at particular elevations and exposures is illustrated by the map in Fig. 7c. We hypothesized that small-scale variations in soil warming due to differential insolation in the day before (or the morning after) a given night could influence soil cooling and thus radiative frost at night in particular places. In fact, the contribution of DPI appeared significant in the BRT subregional model, at least from November to February when potential insolation is at its seasonal maximum (Table 1), thus leading to highest contrasts in soil energy balance between sunlit and shaded locations. However, the small contributions of the afternoon or morning components of insolation (API and MPI) (Fig. 4b) seem to belie the idea that potential insolation is directly involved in frost vulnerability at particular places. Actually, Blennow (1998) states that the larger amount of heat stored into the ground in sunlit places cannot compensate for soil cooling at night since this cooling occurs within a few hours after sunset. Nocturnal soil cooling should be still faster under clear-sky conditions at high altitude. This is, however, in contradiction with the common perception of lower frost occurrence in sunlit slopes, particularly in stony terrains and shallow soils supposed to benefit from the thermal stability provided by the rocks. Microclimate stability associated to rock outcrops has been documented by Rada et al. (2009) in the paramo ecosystem of Venezuelan Andes at lower elevation (3800 m) and under wetter conditions (969 mm of annual precipitation). It is likely that the much drier conditions of the puna ecosystem in southern Bolivia reduce the thermal inertia of the soils, thus leading to a very fast soil cooling at night. Apart from astronomical forcing discussed previously, the varying importance of CTI, DPI and SLO in the BRT models, as well as the interactions between them (Fig. 6) reflect complex spatio-temporal relations between insolation and landform factors producing multiplicative or mitigating effects on near-ground temperature. At the microscale level, unobserved soil and vegetation properties might also interfere with landform features. Soil moisture and vegetation cover, for example, are known to influence the radiative balance at the soil surface, and might contribute to buffer the near-ground temperature from cold extremes in particular places (Fridley, 2009; Geiger, 1971).
4.3. Ecological implications

The relationships between ecological patterns and processes change across spatial and temporal scales, with singular complexity in mountain areas (e.g., Deng et al., 2007; Saunders et al., 1998). Regarding air or soil surface temperature in mountains, nested factors are interacting, from regional synoptic weather forcing to local topoclimatic situations and microscale variations in vegetation cover and soil moisture. All these factors in turn may dominate the distribution of temperatures, depending not only on the dynamics of the situation (turbulent or stable, nighttime or daytime conditions...) but also on the spatial and temporal scale of interest (from macroscale to microscale, from seasonal to instantaneous). In this way, macroscale conditions of clear sky and calm nights are required for radiative frost to occur, but the frequency and severity of these frost events are further increased by low site position (or conversely, extremely high location) and, at still smaller scales, by vegetation sparseness and soil surface dryness or roughness (De Chantal et al., 2007; Fridley 2009; Langvall & Ottonson Löfvenius, 2002; Oke, 1970). In the Andean highlands, instantaneous near-ground minimum temperature may be 4°C lower in a sparsely vegetated area compared to a neighboring forest understory (Rada et al., 2009). Similar fine scale variations in minimum air temperature occur within cultivated canopies despite the low plant cover of most Andean crop species (see Winkel et al., 2009, for the quinoa crop). These local variations in minimum near-ground temperatures may be sufficient for some part of the vegetation to escape lethal freezing. Potential frost impacts on vegetation operating at regional and subregional scales may thus be over-shadowed by microscale variability in minimum temperature. Yet, contrary to what occurs in dense forests where plant interactions within canopies are significant (Bader et al., 2008; Turnipseed et al., 2003), the sparse and low vegetation typical of the Andean highlands is likely to exert an influence limited to small spatial scales, with topography and coarse scale factors controlling most of the variation in minimum air temperature. In fact, Blennow (1998) outlines that topographic influences on minimum air temperature increase in parallel with decreasing vegetation cover.

4.4. Practical implications

The latter consideration implies that agroclimatic applications, such as crop zonation or suitability assessments, require a multi-scale approach, ideally complementing frost risk characterization at the topoclimatic scale by an evaluation of the local effects of crop practices on canopy structure and soil surface moisture and roughness. Though limited to topography-frost relationships, our attempt of downscaling frost occurrence at a 100-m scale usefully expands previous works on regional agroclimatic zoning in the Bolivian altiplano (François et al., 1999; Geerts et al., 2006). To our knowledge, this is the first time that such a detailed zonation of topoclimate is reported for this region, providing fine-scale information helpful for land management and rural planning (Theobald et al., 2005). Considering the scarcely available meteorological records in the study area, these 100-m scale maps bring new information about the spatio-temporal variation of frost occurrence, allowing now to localize exactly the seasonal pattern of frost typical of the Andean summer period (Frère et al., 1978; Troll, 1968). For instance, the virtual zero value of frost frequency in January and February derived from meteorological records at Salinas (Fig. 1), covers in reality a wide range of situations with still significant frost occurrence in mid-summer, as on the nearby border of the salar of Coipasa or the western and
southern part of the study area (Fig. 2). In fact, the recent expansion of quinoa crop in the region was firstly and mostly located in flat areas near the Coipasa and Uyuni salt lakes (Vassas et al., 2008), which exemplifies the complex trade-offs between agroclimatic risks and economic expectancies operating in farmers’ decision making (Luers 2005; Sadras et al., 2003).

4.5. Perspectives

Through remote sensing of land surface temperature and modeling of topographic features implemented within a boosted regression procedure, we were able to explicitly downscale frost occurrence at the landscape scale. The method developed here may be adapted to climatic or ecological processes other than frost. Rainfall distribution could be a candidate since its spatio-temporal patterns clearly depends on landscape characteristics over complex terrains. Current literature outlines the importance of landform as a factor of rainfall variability in the Andes (Giovannettone & Barros, 2009), though most studies were conducted at the coarse spatial resolution appropriate to continental scale climatology (Garreaud & Aceituno, 2001; Misra et al., 2003; Vuille et al., 2003). Canopy energy budget, soil water balance, or ecosystem productivity are other ecological processes tractable for topographic modeling (Bradford et al., 2005; Rana et al., 2007; Urban et al., 2000). Such applications depend firstly on the availability of remotely sensed proxies for the considered process. For example, the remotely sensed daily amplitude in surface temperature and vegetation indices can be used to derive daily evapotranspiration (Wang et al., 2006). Similarly, satellite estimates of absorbed photosynthetically active radiation may serve to evaluate net primary productivity (Bradford et al., 2005; Turner et al., 2009). An additional requisite for the calibration of these applications consists in local ground measurements for the variable of interest. This is a major issue in the case of the tropical highlands where, similarly to what occurs for meteorological data, reliable datasets on matter and energy fluxes at ground level are and will remain scarce (Vergara et al., 2007). The methods and results presented here can contribute to a better understanding of the potential risks associated with climate and land use changes in complex terrains, so that decision-makers can develop efficient strategies to improve the ecological sustainability of natural and agricultural ecosystems in vulnerable mountain areas.

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