Assessment of reference evapotranspiration methods in semi-arid regions: can weather forecast data be used as alternate of ground meteorological parameters?

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Assessment of reference evapotranspiration methods in semi-arid regions: Can weather forecast data be used as alternate of ground meteorological parameters?

S. Er-Raki a,*, A. Chehbouni b, S. Khabba a, V. Simonneaux b, L. Jarlan b, c, A. Ould Dabba c, J.C. Rodriguez d, R. Allen e

a Cadi Ayyad University/IRD, Avenue Prince Moulay Abdellah, BP 2390, Marrakech 40000, Morocco
b CESBIO – Centre d’Etudes Spatiales de la Biosphère, 18 Avenue Edouard Belin, bpi 2801, 31401 Toulouse Cedex 9, France
c DMN: Direction de la Météorologie Nationale, Casablanca, Morocco
d Universidad de Sonora, Hermosillo, Mexico
e Water Resources Engineering, University of Idaho, 3793 N. 3600 E., Kimberly, ID 83341, USA

ABSTRACT

In this study, the performance of three empirical methods for estimating reference evapotranspiration (ET0): Makkink (Mak) and Priestley–Taylor (PT) (radiation-based) and Hargreaves–Samani (HARG) (temperature-based) were assessed in semi-arid regions. The values of ET0 derived using these three methods were compared to those estimated using the reference FAO Penman–Monteith (FAO-PM) method under semi-arid conditions of the Tensift basin (central of Morocco) and the Yaqui Valley (Northwest Mexico). The results showed that the HARG method is the best one to estimate ET0 over both semi-arid test sites. Conversely, the performance of the other two empirical methods was poor except under humid conditions. However when the parameters α and C0 figure in the PT and Mak equations are locally calibrated, the performance of these two methods greatly improved. Additionally, this study showed that, when measurements of meteorological parameters needed for estimating ET0 (which are not always available especially in developing countries) are lacking, the climatic data generated with numerical weather prediction models provide an alternative and effective solution to estimate ET0. In this regard, data generated using a weather forecast model (ALADIN) over the Tensift basin showed that the HARG model is the most accurate one for estimating the spatio-temporal variability of ET0.

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1. Introduction

The Food and Agriculture Organization (FAO) recommends the use of the FAO Penman–Monteith (FAO-PM) equation for estimating reference evapotranspiration (ET0) (Allen et al., 1998, 2006). This method is the most widely used in the world, and has been proven to accurately estimate ET0 in different climates (Allen et al., 1998; De Bruin and Stricker, 2000; Hussein and Al-Ghobari, 2000; Kashyap and Panda, 2001; Smith, 2000; Walter et al., 2000). However, it requires several measurements of climatic variables such as air temperature, relative humidity, solar radiation and wind speed. Unfortunately, there are a limited number of sites over the world where complete meteorological stations are installed for routine measurements of these climatic variables. This lack of meteorological data leads to the development of simpler approaches to estimate ET0 that require only a few climatic parameters. In this context, several methods have been reported in the literature to estimate ET0. Some of these methods are based on a single climatic variable, i.e., solar radiation (Blaney and Cridge, 1950; Makkink, 1957; Priestley and Taylor, 1972) or temperature (Hargreaves and Samani, 1985). Other methods are based on different combinations of climatic parameters involving solar radiation, air temperature, humidity and wind speed (Allen et al., 1998; Doorenbos and Pruitt, 1977; Monteith, 1965; Penman, 1948). When air temperature is the only available variable, Allen et al. (1998) proposed the use of the Hargreaves–Samani (HARG) equation as an alternative to estimate ET0. In this regard, several studies have shown that this equation may provide reasonable estimates of ET0 (Choisenel et al., 1992; Dinapahol, 2006; Droogers and Allen, 2002; Hargreaves, 1994; Henggeler et al., 1996; Jensen et al., 1990; Martinez-Cob and Tejero-Juste 2004). Other authors have reported that the HARG equation tends to overestimate ET0.

* Corresponding author at: Projet SudMed, Centre Geber salle 26, Faculty of Science Semlalia, Cadi Ayyad University, BP 2390, Marrakech, Morocco. Tel./fax: +212 (0) 524 43 16 26.
E-mail addresses: serraki@ucam.ma, serraki@gmail.com (S. Er-Raki).
in humid regions and to underestimate it in very dry regions (Amatya et al., 1995; Droogers and Allen, 2002; Jensen et al., 1990; Saeed, 1986; Xu and Singh, 2002). Therefore, the HARG equation may require local calibration prior to its application (Dinpashoh, 2006; Jensen et al., 1997; Vanderlinden et al., 1999; Xu and Singh, 2002). Makkink (1957) and Priestley and Taylor (1972) proposed two empirical equations for calculating ET₀ when air temperature and solar radiation data are available. The PT equation is used in many crop models (e.g. CERES model (Ritchie, 1985); EPIC (Williams et al., 1989), SWAP (Utset et al., 2004)). Similarly, several studies have shown that this method underestimated ET₀ in dry and windy conditions (Benson et al., 1992; Dugas and Ainsworth, 1983; Martinez-Cob, 2002).

When reliable climatic data are scarce or do not exist, an alternative approach might be to use data generated with numerical weather prediction models. These data present two advantages: i) they are becoming more and more available through the internet; ii) the models provide spatially distributed data, which are very relevant to the regional scale studies. Unfortunately, there are two drawbacks associated with using this type of data. The first is that, the lowest atmospheric model layer is usually situated considerably higher than the reference height recommended for climatic measurements. Secondly, the spatial resolution of these models is very coarse. For example the ARPEGE global model of Meteorological France (Déqué et al., 1994; http://www.cnrm.meteo.fr/gmgec/arpege/arpege.html) provides the data at a resolution of 20 km in France to 250 km in antipodes. The local model (ALADIN: Aire Limitée, Adaptation Dynamique, développement InterNational) of the Moroccan Meteorological Agency runs with a slightly higher spatial resolution (16.7 km) over Morocco.

The objective of this study is (1) to evaluate, under semi-arid conditions, the performance of three empirical methods (PT, Mak and HARG) for estimating ET₀ by comparing their values to those estimated using the FAO-PM equation and (2) to evaluate the potentiality of weather forecast prediction as an alternative to measured climatic data.

2. Materials and methods

2.1. Area description and weather data

The three empirical methods (Eqs. (2)-(4)) were evaluated over two sites described below (the Tensift region around Marrakech, Morocco and the Yaqui Valley in the north of Mexico) against the FAO-PM method. In addition, a weather forecast model (ALADIN) available over the Tensift basin was used to estimate the spatial—temporal distribution of ET₀.

2.1.1. Tensift basin

The Tensift basin situated in central of Morocco is located between 30.75°–32.40° N and 7.05°–9.9° W, occupying an expanse around 30 000 km². The climate is semi-arid, typically Mediterranean; with an average annual precipitation of about 250 mm. Air temperature is very high in summer (38°C) and low in winter (5°C). The mean annual value for ET₀, calculated using the FAO-PM equation, is about 1600 mm (Allen et al., 1998). In the Tensift basin, a large area is dedicated to agriculture. The Haouz plain covers around 6000 km², and is delimited to the north by the ‘bilet’ hills and to the south by the High-Atlas mountain range (that culminates up to 4000 m). Weather data sets were obtained from the 8 stations installed in the framework of the SudMed project (Chehbouni et al., 2008) (see Fig. 1). Locations of the stations are given in Table 1. In addition, the aridity index defined as the ratio of the annual rainfall to the annual ET₀ (UNEP, 1997) is calculated for each Tensift stations. Each station measures with a 30 min time step and at a 2 m height: air temperature, relative humidity, solar radiation, wind speed and direction and rainfall. In some stations (Agdal, Saada and Agafay), net radiation (Rn) was measured with a Kipp and Zonen CNR1 net radiometer. The daily values of the meteorological variables were used to compute daily ET₀. The network stations were deployed in order to cover the spatial variability of the climate over the whole Tensift basin. Based on the calculated aridity index (Table 1) during 2004, the Tensift area can be divided into two distinct climatic regions. The first one situated in the Haouz plain characterized by

Fig. 1. Study area and location of the weather stations.
Q2 the semi-arid climate, in which all stations (Agdal, Agafay, Chichaoua, Grawa, Saada and R3) have an aridity index less than 0.2. The second region located in the Atlas mountain range, characterized by the sub-humid conditions (Okaimden and Armed stations) where the aridity index was relatively higher (0.4–0.53).

Fig. 2 shows the daily evolution of the meteorological variables recorded by the station located in R3 zone (Table 1, Fig. 1) during 2003–2004. The mean annual solar radiation is about 17 MJ/m²/day, and ranges between 4 MJ/m²/day in December–January and 28 MJ/m²/day in May–June. The seasonal variation of daily air temperature was similar with respect to the shape to that of solar radiation, between 5°C in January and 36°C in August, with an annual mean of about 18.5°C. The evolution of relative humidity is out of phase with the solar radiation, and tends to increase in the winter and decrease in summer. Wind speed remained almost constant during the year around 2.1 m/s, but in some days its values exceeded 4 m/s. The cumulative precipitation during 2003 was 530 mm with most rain falling in the autumn and winter seasons. Note that this year was wetter in comparison with the average annual precipitation (250 mm). It should be mentioned that due to power supply problems, some data were missing during a few days.

2.1.2. The forecasted climatic data from the ALADIN model (Morocco)

When the meteorological parameters needed for estimating spatially $E_T$ are not available due to the scarcity of weather stations, it is possible to use the climatic data generated over a large area with the numerical weather prediction models. The numerical model used in this study is the ALADIN model adapted by the national meteorological services of Morocco (DMN) which generates all climatic parameters needed for $E_T$ estimate. ALADIN is a spectral model of numerical forecast in a limited area, based on the assimilation of daily measurements, and driven using the outputs of the ARPEGE global model (provided by French meteorological services). ARPEGE is an operational tool in the limited area modelling in Central Europe, and it is also used in several other regions (Morocco and Tunisia). The global model (ARPEGE) provides the data at resolution of 20 km in France to 250 km in antipodes, while the local model (ALADIN) is running at a higher spatial resolution (16.7 km) over Morocco. The ALADIN model over Morocco is named AL BACHIR and its main characteristics are:

- Spectral model with elliptical truncation.
- Horizontal resolution: 16.7 km.
- Vertical resolution: 37 levels.
- Horizontal extent: 2000 km x 2000 km (180 x 180 points).
- Hydrostatic dynamic.

The ALADIN model outputs include the climatic parameters (solar radiation, minimal and maximal air temperature, minimal and maximal relative humidity and wind speed) needed for $E_T$ estimate. The quality of this model, in generating weather variables, was evaluated by comparing the estimated climatic parameters with the ones measured over the Tensift basin. Importantly enough,
none of the ground station of the Tensift network installed within the frame of the SudMed project is used to drive ALADIN such as forecast and stations measurements are independent.

2.1.3. Yaqui Valley

The Yaqui Valley is a large, flat agricultural area in the Northwest of Mexico. The total irrigated surface is about 255 000 ha and the main crop (occupying more than 50% of the area) is winter wheat which grows from November to April every year. The climate of this region is semi-arid with an annual rainfall of around 350 mm. The rainy season is from July to September (with about 70% of the annual rainfall) and there is a very dry season with almost no rainfall from March to June. The mean daily temperature ranges from about 17 °C in January to 31 °C in summer (July–August). Half-hourly measurements of classical climatic data were collected over grass during 2004 using a standard micro meteorological weather station. Incoming solar radiation was measured with a BFL Delta T radiometer, air temperature and humidity were measured at 2 m height with Vaisala HMP45C probes, and wind speed was measured at a 2 m with A100R anemometers (R.M. Young Company, USA). Further details of the field experimental setup can be found in Rodriguez et al. (2004).

2.2. Reference evapotranspiration methods

There are so many different methods for estimating reference evapotranspiration ET0 that it is often difficult to decide which one to use. In this context, we choose four methods for estimating ET0 which differ with the number of climatic parameters required: The first one is the FAO Penman–Monteith (FAO-PM) which is recommended by the Food and Agriculture Organization (FAO) as the standard method (Allen et al., 1998) to estimate ET0. It has been standardized by Allen et al. (2006). This method uses several climatic data such as: air temperature and relative humidity, solar radiation and wind speed (Eq. (1)). This method is taken as a comparator basis in this study. The second equation is the PT equation (Priestley and Taylor, 1972) which requires net radiation and air temperature data (Eq. (2)). The third one is the Mak method (Makkink, 1957) which requires solar radiation and air temperature (Eq. (3)). The last method is the HARG equation (Hargreaves and Samani, 1985) which only requires air temperature (Eq. (4)).

These four methods are formulated as follows:

\[
ET_{0,\text{FAOPM}} = \frac{0.408 \cdot L(R_n - G) + \gamma \cdot \frac{0.0023}{T_f} \cdot (e_s - e_a)}{d + \gamma(1 + 0.34u_2)}
\]

(1)

\[
ET_{0,\text{PT}} = \frac{0.408 \cdot \alpha \cdot L(R_n - G)}{d + \gamma}
\]

(2)

\[
ET_{0,\text{Mak}} = \frac{0.408 \cdot C_m \cdot R_n}{d + \gamma} - 0.12
\]

(3)

\[
ET_{0,\text{HARG}} = 0.408(T_a + 17.8)(T_{\text{max}} - T_{\text{min}})^{0.5} R_n
\]

(4)

where \(ET_0\) is expressed in [mm/day]; \(R_n\) is the solar radiation [MJ/m²/day]; \(R_n\) and \(R_s\) are net radiation and extraterrestrial radiation respectively [MJ/m²/day] computed as described by Allen et al. (1998); \(G\) is the soil heat flux density [MJ/m²/day], which is assumed to be 0 at daily time step; \(T_a\) is the air temperature at 2 m height [°C]; \(u_2\) is the wind speed at 2 m height [m/s]; \(e_s\) and \(e_a\) are the saturation and actual vapor pressure [kPa] respectively; \(d\) is the slope of the vapor pressure curve at air temperature [kPa/°C] and \(\gamma\) is the psychrometric constant [kPa/°C]. \(e_s\) is computed as:

\[e_s = (e^0(T_{\text{max}}) + e^0(T_{\text{min}}))/2\]

where \(e^0\) is the saturation vapor function and \(T_{\text{max}}\) and \(T_{\text{min}}\) are the daily maximum and minimum air temperature respectively. The value 0.408 corresponds to the conversion factor from [MJ/m²/day] to mm/day. The parameters \(\alpha\), \(C_m\) and \(a\) that appear in Eqs. (2)–(4), respectively, are empirical constants. Their original values are 1.26, 0.61 and 0.0023 respectively (Allen et al., 1998; Makkink, 1957; McAneney and Itier, 1996; Priestley and Taylor, 1972).

2.3. Statistical analysis

The comparison between the three empirical methods (Eqs. (2)–(4)) and the FAO Penman–Monteith method was carried out first using ground data. The comparison is evaluated using: (1) a linear regression equation \((Y = mX + c)\), through least square regression, between \(ET_0\) computed by FAO Penman–Monteith equation and \(ET_0\) estimated from the above mentioned three methods \(m\) and \(c\) are the slope and the intercept of the regression equation, respectively; (2) the coefficient of determination \((R^2)\); (3) the Root Mean Square Error (RMSE). In the case of a perfect correlation with no bias, \(c = 0\) and \(m = 1\), \(R^2 = 1\) and RMSE = 0.

3. Results and discussions

3.1. Evaluation of predicted and measured climatic data accuracy over Tensift

The accuracy and quality of the measured weather data is evaluated over Tensift as the weather station network is quite dense (8 stations) with regard to the Yaqui Valley. The quality of meteorological measurement is simply evaluated by checking the overall consistency of the annual average of the climatic parameters (solar radiation, wind speed, air temperature and relative humidity) among different stations. Table 2 summarizes the annual average of the climatic variables over the 8 stations. The measurements appear consistent and coherent among different stations. Regarding to air temperature (\(T_a\)), the higher values are recorded in the Haouz plain (Agdal, Agafay, Chichawa, Grawa, Saada and R3) characterized by a semi-arid climate and the lower \(T_a\) is observed in the mountains (Okaimden and Armed). For relative humidity (\(RH\)), it is higher over irrigated areas (e.g. Agdal and Agafay stations) due to high evapotranspiration than in dry areas (mountain and bare soil). The measurements of wind speed (\(U\)) are also consistent between different stations. The lower \(U\) is encountered in the locations affected by the surrounding. The friction tends to decrease the wind as in the stations installed in tall vegetation (e.g. Agdal where the olive trees dominate). The higher \(U\) is observed in the opened locations as the mountain (oukaïden) and bare soil (R3, Chichaoua). For solar radiation (\(R_n\)), it is almost similar for all stations with a mean annual value of 19 MJ/m²/day. Additionally, the performance of solar radiation measurements is evaluated by comparing the measured net radiation (\(R_n\) values) against the estimated one \((R_n\text{-sim})\) from FAO-56 (Eq. (40)). Fig. 3 displays the scatter plot between measured and FAO-predicted \(R_n\) over the stations where the measurements of \(R_n\) are available. This figure reveals a very good agreement (slope = 0.96, with \(R^2 = 0.94\) and RMSE = 1.09 MJ/m²/day) between the measured and FAO-predicted \(R_n\). In addition, the coefficient of variability (CV) defined as the ratio of the standard deviation to the mean value is calculated for each climatic parameter. It was equal 3.66, 31, 8.35 and 35.8% for \(R_n\), \(T_a\), RH and \(U\) respectively. Clearly, variation in \(U\) and \(T_a\) was larger than that in \(R_n\) and RH.

As the measured weather data, the predicted ones by ALADIN were also evaluated before using them for estimating the spatial \(ET_0\). The quality of the ALADIN prediction in generating weather variables is evaluated by comparing the estimated climatic
parameters with the ones measured over the Tensift basin. The climatic data recorded in equivalent ALADIN grid points to weather stations (Table 1, Fig. 1) are used. The values of climatic data in these equivalent grid points were calculated by weighting the values of climatic data recorded in each grid point (four grid points around the weather station) by using the bilinear interpolation (Arnaud and Emery, 2000). As mentioned above, the Tensift study area can be divided into a semi-arid climate region (the Haouz plain) and a sub-humid climate region (the high Atlas mountains). Two stations were used for the local evaluation: one station (R3) characterizing the semi-arid climate in the plain, and another one (Armed) characterizing the sub-humid climate in the mountain. In this context, we compared the measured climatic parameters with the generated ones with ALADIN for two equivalent grid points to weather station (R3 and Armed, Fig. 1) during the year 2004. The associated statistical results are presented in Table 3. The ALADIN forecasts are in good agreement with the station measurements in terms of solar radiation ($R_n$) and air temperature ($T_a$) in both sites. The coefficient of determination ($R^2$) and the slope are close to 1 especially for $T_a$, and the RMSE are considered acceptable with regard to the average values. However, the comparison of the station and the forecasted values of relative humidity (RH) and wind speed ($U$) is much more scattered (Table 3). The ALADIN model is known, in particular, to overestimate the wind speed in the bottom layers of the atmosphere due to the effect of surroundings (ground cover roughness, topography) that are not correctly taken into account in the model. Finally, the remaining error certainly also originates from the difference of spatial representativeness between the ground station data and the ALADIN forecast grid point.

3.2. Assessment of ET$_0$ estimation methods

As mentioned above, the evaluation of the three methods (Eqs. (2)–(4)) is undertaken through the comparison with the FAO-PM equation. This evaluation was performed in two stages. In the first stage, ET$_0$ from the three empirical methods was computed with the original parameter values given above. In the second stage, ET$_0$ was computed with locally calibrated parameter values. Based on the aridity index, the Tensift study area can be divided into a semi-arid climate region (the Haouz plain) and sub-humid climate region (the mountain). Two sites considered to be representative of each sub-region were chosen to assess the performance of the three empirical methods. The first one is R3 which characterized the semi-arid climate in the Haouz plain. The second one is Armed situated in the Atlas mountain range, characterized by the sub-humid conditions (see Fig. 1 and Table 1).

3.2.1. Assessment of the method performances without calibration

Using the data collected in the year 2003 in the Haouz plain (station R3), daily evolution of ET$_0$ values was calculated using the three empirical methods (Eqs. (2)–(4)). These values were then compared with those obtained using the FAO-PM method (Fig. 4). The statistical results are reported in Table 4. According to these results, the HARG method seems to be the best one to calculate ET$_0$ in the Haouz plain (semi-arid climate). The coefficient of determination ($R^2$) and the slope are close to 1 and the value of RMSE = 0.67 mm/day can be also considered acceptable with regard to the average value of ET$_0$ (4.10 mm), especially during the

![Fig. 3. Scatter plot between measured net radiation ($R_n$-mes) and estimated one ($R_n$-sim) by FAO-56 (Eq. (40)).](image-url)

Table 2

<table>
<thead>
<tr>
<th>Station</th>
<th>Annual average of $R_n$ (MJ/m$^2$/day)</th>
<th>Annual average of $T_a$ ($^\circ$C)</th>
<th>Annual average of RH (%)</th>
<th>Annual average of $U$ (m/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Agdal</td>
<td>18.74</td>
<td>19.46</td>
<td>60.20</td>
<td>0.80</td>
</tr>
<tr>
<td>Agafay</td>
<td>19.30</td>
<td>18.24</td>
<td>60.07</td>
<td>1.06</td>
</tr>
<tr>
<td>Chichawa</td>
<td>20.55</td>
<td>18.01</td>
<td>59.20</td>
<td>2.07</td>
</tr>
<tr>
<td>Gnaoua</td>
<td>19.35</td>
<td>18.99</td>
<td>55.73</td>
<td>1.35</td>
</tr>
<tr>
<td>Saada</td>
<td>18.05</td>
<td>19.69</td>
<td>58.76</td>
<td>1.48</td>
</tr>
<tr>
<td>R3</td>
<td>18.67</td>
<td>20.51</td>
<td>52.21</td>
<td>2.22</td>
</tr>
<tr>
<td>Okaimden</td>
<td>19.61</td>
<td>4.61</td>
<td>45.59</td>
<td>2.53</td>
</tr>
<tr>
<td>Armed</td>
<td>18.83</td>
<td>11.18</td>
<td>56.59</td>
<td>1.23</td>
</tr>
<tr>
<td>Max</td>
<td>20.55</td>
<td>20.51</td>
<td>60.20</td>
<td>2.53</td>
</tr>
<tr>
<td>Min</td>
<td>18.05</td>
<td>4.61</td>
<td>45.59</td>
<td>0.80</td>
</tr>
<tr>
<td>Mean</td>
<td>19.14</td>
<td>16.34</td>
<td>56.04</td>
<td>1.59</td>
</tr>
<tr>
<td>CV (%)</td>
<td>3.66</td>
<td>31.00</td>
<td>8.35</td>
<td>35.90</td>
</tr>
</tbody>
</table>

$R_n$: solar radiation (MJ/m$^2$/day); $T_a$: air temperature ($^\circ$C); RH: relative humidity (%); $U$: wind speed (m/s).

CV: coefficient of variability (%) defined as the ratio of the standard deviation to the mean value.

Table 3

<table>
<thead>
<tr>
<th>R3</th>
<th>Armed</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_n$</td>
<td>$T_a$</td>
</tr>
<tr>
<td>-----------</td>
<td>-----------</td>
</tr>
<tr>
<td>Average</td>
<td>18.67</td>
</tr>
<tr>
<td>Slope</td>
<td>0.71</td>
</tr>
<tr>
<td>Y-intercept</td>
<td>5.32</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.93</td>
</tr>
<tr>
<td>RMSE</td>
<td>3.46</td>
</tr>
</tbody>
</table>

$R_n$: solar radiation (MJ/m$^2$/day); $T_a$: air temperature ($^\circ$C); RH: relative humidity (%); $U$: wind speed (m/s).

summer (Fig. 4). This is in agreement with other studies (e.g. Hargreaves, 1994; Henggeler et al., 1996; Jensen et al., 1990).

However, on some dates (DOY 71, March 12, 2003; DOY 263, September 20), a large difference between \( E_{\text{TO}} \) estimated by HARG and FAO-PM methods was observed. This is certainly due to the effect of wind speed which exceeded 3 m/s on these days (Fig. 2). Indeed, Martinez-Cob and Tejero-Juste (2004) reported that when the wind speed is strong, the Hargreaves equation could underestimate \( E_{\text{TO}} \). In the same way, Berengena and Gavilan (2005) showed that, when the advection is severe, the Hargreaves equation tends to underestimate \( E_{\text{TO}} \) up to 25% for daily periods.

In contrast to HARG model, the performance of the two other methods (PT and Mak) was poor, the corresponding RMSE were 1.30 and 1.52 mm/day for PT and Mak, respectively (see Table 4 for other statistical analysis). However, Fig. 4 indicates that two distinct periods should be considered when using these methods, a dry period (when the daily mean air relative humidity is lower than 60%) from DOY 140 to DOY 270 and the humid period (when RH is higher than 70%) for the remaining days. It appears that the PT and Mak methods clearly underestimate the values of \( E_{\text{TO}} \) calculated using FAO-PM model during the dry period. Such behaviour can be explained by the fact that the values of \( \alpha = 1.26 \) and \( c_m = 0.61 \), used in Eqs. (2) and (3), are only valid under humid conditions (Jensen et al., 1990; Priestley and Taylor, 1972). This explanation is confirmed by the results of the second period (when the cumulative rainfall was about 470 mm). The statistical values (RMSE is equal to 0.97 mm/day for the PT method and 0.98 mm/day for the Mak) are consistent with those obtained for the HARG method. This is corroborated by other studies (e.g. Benson et al., 1992; Dugas and Ainsworth, 1983; Xiaoying and Erda, 2005).

To confirm the reliability of PT and Mak models for estimating daily \( E_{\text{TO}} \) with original parameter values (\( \alpha = 1.26 \) and \( c_m = 0.61 \)) under sub-humid conditions, a comparison with the FAO-PM method is performed using climatic data collected in a sub-humid region situated in the high-Atlas mountain (Armed station, Table 1 and Fig. 1). Plotting daily values of \( E_{\text{TO}} \) estimated by FAO-PM against those estimated by both methods at this region (data not presented) revealed practically perfect agreement between the FAO-PM and the estimates from the two other methods. The values of RMSE are 0.65 and 0.59 mm/day for the PT and Mak methods respectively. These values of RMSE are acceptable, given the average value of \( E_{\text{TO}} \) (3.22 mm). Additional statistical results are presented in Table 4. The performance of the Hargreaves approach was lower in sub-humid conditions (RMSE = 0.83 mm/day) in comparison to the other methods. This is consistent with the results of other studies (Jensen et al., 1990; Xu and Singh, 2002) when they found that the HARG method tends to overestimate \( E_{\text{TO}} \) in a humid climate.

According to the above results, one can conclude that it is appropriate to use the HARG method without calibration to estimate \( E_{\text{TO}} \) in a semi-arid region (as far as the wind remains low). However, a calibration of two parameters (\( \alpha \) and \( c_m \)) in the PT and Mak equations is needed, especially for the dry periods.

### Table 4

<table>
<thead>
<tr>
<th>Statistics parameters</th>
<th>Estimation method</th>
<th>R3</th>
<th>PT</th>
<th>Mak</th>
<th>HARG</th>
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<td>n</td>
<td></td>
<td>315</td>
<td>315</td>
<td>315</td>
<td>366</td>
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<tr>
<td>Slope</td>
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<tr>
<td>Y-intercept</td>
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<td>-0.07</td>
<td>0.16</td>
<td>0.66</td>
</tr>
<tr>
<td>( R^2 )</td>
<td></td>
<td>0.82</td>
<td>0.84</td>
<td>0.92</td>
<td>0.85</td>
</tr>
<tr>
<td>RMSE (mm/day)</td>
<td></td>
<td>1.30</td>
<td>1.52</td>
<td>0.67</td>
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To confirm the reliability of PT and Mak models for estimating daily \( E_{\text{TO}} \) with original parameter values (\( \alpha = 1.26 \) and \( c_m = 0.61 \)) under sub-humid conditions, a comparison with the FAO-PM method is performed using climatic data collected in a sub-humid region situated in the high-Atlas mountain (Armed station, Table 1 and Fig. 1). Plotting daily values of \( E_{\text{TO}} \) estimated by FAO-PM against those estimated by both methods at this region (data not presented) revealed practically perfect agreement between the FAO-PM and the estimates from the two other methods. The values of RMSE are 0.65 and 0.59 mm/day for the PT and Mak methods respectively. These values of RMSE are acceptable, given the average value of \( E_{\text{TO}} \) (3.22 mm). Add}

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which is an indicator of regional climate (humid or dry). In this context, the appropriate values of $\alpha$ have been determined for each interval of relative humidity with steps of 10%. The linear regression obtained between $\alpha$ and (RH) was:

$$\alpha = 0.014RH + 2.33, \quad R^2 = 0.98$$  \hspace{1cm} (5)$$

It can be noted that this equation estimates $\alpha = 1.26$ when daily mean RH = 76% and $\alpha = 1.74$ when RH = 42%. This indicates that the calibration of $\alpha$ (Eq. (5)) could be applied in many areas depending on the climate (arid, humid...).

Similarly, the Makkink constant $C_m$ was adjusted by a linear regression to (RH):

$$C_m = -0.0062RH + 1.15, \quad R^2 = 0.96$$ \hspace{1cm} (6)$$

This calibration of the Makkink constant $C_m$ is similar to that done by Doorenbos and Pruitt (1977), where their Radiation method of FAO-24 was multiplied by a correction that was based on RH and on daytime wind speed.

After the calibration of two parameters $\alpha$ and $C_m$, the RMSE was reduced to 0.70 and 0.60 mm/day (Table 5) for the PT and Mak models.

### Table 5

<table>
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<td>$n$</td>
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<tr>
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<tr>
<td>Y-intercept</td>
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<td>RMSE (mm/day)</td>
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</table>

Fig. 5. Comparison between the values of $ET_0$ calculated by FAO-PM method and those by the three empirical methods at the Haouz plain (R3 station), using the calibrated values of the parameters $\alpha$ and $C_m$ for PT and Mak models, and the original value of the parameter $\alpha$ for HARG method during 2004. The relevant statistical parameters are included in figures.

Fig. 6. Comparison between the values of $ET_0$ calculated by FAO-PM method and those by the three empirical methods at the Yaqui Valley (Northwest Mexico), using the calibrated values of the parameters $\alpha$ and $C_m$ for PT and Mak models, and the original value of the parameter $\alpha$ for HARG method during 2000. The relevant statistical parameters are included in figures.

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methods respectively. This means an improvement of 46% and 60% of the values obtained with respect to the original values of $\alpha$ and $C_m$ (Table 4).

3.2.2.2. Model validation. The data collected during 2004 from the experimental site of the Haouz plain (R3 station) were used together with additional data set collected over the experimental site of the Yaqui Valley (Northwest Mexico) for model validation purposes.

By using the calibrated parameters (Eqs. (5) and (6)) and the original value (0.0023) of the parameter $\alpha$, daily values of ET$_0$ calculated by the PT, Mak and HARG models are compared to those obtained by the FAO-PM method. The performance of each method is shown for the Haouz plain in Fig. 5, as well as the associated statistical parameters. As shown in the previous paragraph, the HARG method always presents the best agreement to the FAO results. The coefficient of determination ($R^2$) and the slope are close to 1, the value of RMSE = 0.70 mm/day can be also considered very acceptable with respect to average value of ET$_0$ (5.07 mm) (Fig. 5).

Also both calibrated methods (PT and Mak) estimate ET$_0$ with an acceptable accuracy, the values of RMSE are 1.02 and 1.17 mm/day respectively for the PT and Mak methods. In some days (DOYs 180–183, 206–209, 234–237 and 253–254), the values of ET$_0$ obtained by the three methods are lower than those of FAO-PM method. This was due to the high values of wind speed which exceeded 3 m/s on these days (see Fig. 2), which lead to high values for the aerodynamic term (advection) that is one of the main differences between the FAO-PM method and other empirical equations (Berengena and Gavilan, 2005).

For the Yaqui Valley site (Fig. 6), the validation also provides an accuracy estimate of ET$_0$ by three models. The obtained values of RMSE, 0.79, 0.80 and 0.76 mm/day for the PT, Mak and HARG methods respectively, are considered relatively acceptable with regard to the average value of ET$_0$ which reached about 5.17 mm/day (Fig. 6). Also the HARG method is the best one to estimate ET$_0$ over this other semi-arid region.

According to these results, it can be concluded that the HARG model is the most reliable method for estimating ET$_0$ over both semi-arid test sites (Tensift basin and the Yaqui Valley) when the availability of climatic variable is limited and when wind speed not exceeded 3 m/s.

3.3. Spatially distributed modelling of ET$_0$

The spatial variation of ET$_0$ over the Tensift region is analyzed thanks to the ALADIN model forecast data. The good performance of the HARG model at the local scale together with the accurate estimation of air temperature by the ALADIN model, which is the main input of the HARG method, lead us to choose this model for estimating the spatial distribution of ET$_0$ with regard to the Mak and PT methods. In addition, the spatial estimation of ET$_0$ by the HARG model is compared to the FAO-PM method using ground based measurements of climatic parameters. Indeed, the FAO-PM is expected to be penalized by the strong discrepancy between ALADIN forecast and measured climatic data in terms of wind and air humidity.

Fig. 7 shows the cumulative monthly ET$_0$ (mm/month) maps for the whole Tensift basin by applying the HARG model to each grid point of the ALADIN model from January to December 2004. This figure exhibits a coherent spatial and temporal variation of ET$_0$. Temporally, the ET$_0$ appears to be highest in the summer (June–August), ranging from 45 to 230 mm/month during the peak period for air temperature, and the smallest ET$_0$ in November–January (16–68 mm/month). Spatially, the higher ET$_0$ is observed in the low altitude (like Haouz plain), and lower ET$_0$ is encountered in the mountain when the altitude is high and air temperature is low. It should be mentioned that lower values of ET$_0$...
are observed over the mountain in winter when the snow covering is high and precludes from evaporation. Such maps of ET₀ can be used by decision makers to assist in water management and irrigation scheduling at regional scale.

In order to go further in the evaluation of the spatial distribution of ET₀ predicted by the HARG model, the HARG ET₀ is compared to ET₀ calculated by the FAO-PM method from the meteorological data measured by the weather stations for 12 months at the eight stations (Table 1) with the spatially modelled results for the corresponding months at the corresponding equivalent grid points (Fig. 8). The associated statistical parameters are included in this figure. It should be mentioned that due to power supply problems, some data of ET₀ estimated by FAO-PM were missing in some days and the data during the corresponding month were not available. The coefficient of determination (R² = 0.92) and the slope (1.09) are close to 1. The value of RMSE = 16.01 mm/month can be also considered acceptable relative to the mean values of cumulative monthly ET₀ (120 mm/month). It is clear from Fig. 8 that the correlation is best when the monthly value of ET₀ was below 160 mm. When the monthly ET₀ was above this value, the HARG method underestimates ET₀ similarly to the local scale evaluation of the method. As already stated above, this is certainly due to the advection term that is not taken into account in the HARG method.

Finally, the FAO-PM method is run using the model forecast data. The scatter plot between ET₀ calculated by the FAO-PM method from the measured meteorological data and the calculated one using the forecast data (not shown) revealed practically an overestimation of ET₀ by the FAO-PM method with regard to the HARG method together with a strong scattering on the stations where the difference between measured and generated climatic parameters is high. For information, the statistical characteristics of the linear fit are as follows: slope = 1.10, intercept = -17.42, R² = 0.85 and RMSE = 21 mm/month. By comparing those relevant statistical parameters with those obtained when using HARG method (Fig. 8), it is clear that this latter performs best although its simplicity. A good performance of the HARG method over the studied semi-arid sites has been expected, because it was originally developed for semi-arid environments. Several studies have shown that the HARG method provides good estimates of ET₀ under semi-arid conditions in different countries, as done by Vanderlinden et al. (1999), Martinez-Cob and Tejeiro-Juste (2004) and Berengena and Gavilan (2005) in Spain, by Dinapashoh (2006) for Iran, and by Jensen et al. (1990), Choisnel et al. (1992), Hargreaves (1994) and Henggeler et al. (1996) for different locations.

4. Summary and conclusions

The FAO-PM equation has a sound physical background and has proven to accurately estimate ET₀. Nevertheless, a drawback which limits its widespread use is that it requires measurements of several meteorological variables: air temperature and relative humidity, solar radiation and wind speed. The lack of the availability of these variables in many parts of the world has led to the development of simpler ET₀ estimation equations requiring only a few climatic variables which are most likely to be available worldwide. In this context, the main objectives of this paper were to test, calibrate and validate, in semi-arid regions of central Morocco (Tensift basin) and Northwest Mexico (Yauci Valley), three methods computing ET₀ based on solar radiation (PT and Mak) and temperature (HARG) against the standard FAO-PM method. The results showed that the HARG method, with its standard constant value (0.0023), worked quite well under moderate wind conditions (<3 m/s) while the performance of the other two empirical methods was poor except in humid conditions. A local calibration of the two parameters α and Cw, which appear respectively in the PT and Mak equations is needed especially for the dry periods.

Air relative humidity (RH) appeared to affect the accuracy of the PT and Mak equations. An adjustment of two parameters α and Cw with RH by using the data collected in the semi-arid region of Tensift basin was proposed. Thus, the original coefficients 1.26 and 0.61 should be replaced by a linear regression with RH (Eqs. (5) and (6)). These locally adjusted coefficients produced a significant improvement in the equations performance. The Root Mean Square Error (RMSE) was reduced to 0.70 and 0.60 mm/day for the PT and Mak methods respectively, which meant an improvement of 46% and 60% compared to the values obtained without calibration (1.30 and 1.52 mm/day). A further validation of the adjusted coefficients α and Cw was performed using another semi-arid site in the Yauci Valley (Northwest Mexico) where the estimates of ET₀ produced by these methods were found to be very reliable.

To overcome the difficulty associated with the scarcity of weather stations measuring the needed meteorological parameters for ET₀ estimates, the possibility of using climatic data generated with numerical weather prediction model (ALADIN) has been assessed over the Tensift basin. The evaluation of the quality of this model in generating weather variables showed that the ALADIN model estimates accurately air temperature, which is the main input of the HARG method. This leads us to choose this method for estimating the spatial and temporal distribution of ET₀. This approach is of particular interest since it not only allowed us to overcome the problem of the lack of weather data, but it also able to predict water needs with a forecast lead time of few days, which is of great importance for irrigation water managers. Another interest of this research paper consists of identifying which the most reliable method for estimating ET₀ can be used in hydrological models. This will certainly improve the performance of this type of models as reported by Oudin et al. (2005) when they showed that the lumped rainfall-runoff model works well in simulating streamflow when using a simple temperature-based ET₀ instead of the Penman-type model.

Finally, it should be noted that this study was based on a limited data set. Further study including longer series of climatic data is

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desirable for considering climate variability and for improving the reliability of the proposed calibrations. However, it should be noted that this study was based on the analysis of a limited data set. A more comprehensive study, including longer series of data, is advisable to improve the reliability of the proposed calibrations.

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