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The use of scintillometry for validating aggregation schemes over heterogeneous grids

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ABSTRACT

A number of studies have been devoted to derive the diurnal course of regional evapotranspiration (ET) especially in semi-arid areas where the assessment of this term is of crucial importance for water resources management. One approach to derive regional evapotranspiration is based on the use of aggregation schemes in conjunction with energy-balance or land-surface models. However, the effectiveness of this approach cannot be fully assessed without a comparison between the model’s flux simulations and the ground truth observations. In the present study, the issue of using scintillometry for validating spatial and temporal aggregation schemes over heterogeneous grids has been investigated. Data collected within the SUDMED project over the oliveyard of Agdal which was located near the Marrakech city (Morocco), have been used to test the aggregation schemes. The Agdal oliveyard was made up of two contrasted fields, or patches. Even though the two sites appear relatively homogeneous, they differ strongly in terms of soil moisture status and vegetation percent cover. The higher soil moisture in the northern site creates heterogeneity at the scale of the entire olive yard (i.e. at grid-scale).

Firstly, the diurnal course of the grid-scale evapotranspiration \( \langle ET_{\text{sim}} \rangle \) estimated from spatial aggregation scheme is compared to that derived from the scintillometry \( \langle ET_{\text{LAS}} \rangle \). The \( \langle ET_{\text{sim}} \rangle \) is obtained as the residual term of the energy balance providing the estimates of the available energy \( \text{AE}(=R_n + G) \), where \( R_n \) and \( G \) are the net radiation and the soil heat flux, respectively, and sensible heat flux. The latter is estimated by using a simple two-layer model developed by Lhomme et al. (1994). The root mean square difference (RMSD) and the correlation coefficient \( (R^2) \) between \( \langle ET_{\text{sim}} \rangle \) and \( \langle ET_{\text{LAS}} \rangle \) were about 46 W m\(^{-2}\) and 0.78, respectively. Secondly, we compared the diurnal course of the grid-scale evapotranspiration \( \langle ET_{\text{sim}} \rangle \) estimated from the temporal aggregation scheme with the \( \langle ET_{\text{LAS}} \rangle \). The \( \langle ET_{\text{sim}} \rangle \) is obtained by extrapolating the instantaneous values of the available energy and the evaporative fraction \( (\text{EF} = ET/\text{AE}) \) estimated at the satellite overpass to daily ones. The instantaneous values of \( \text{AE} \) and \( \text{EF} \) have been measured using remotely sensed surface temperature measured using a ground-based infrared thermometer combined with ancillary micrometeorological data such as wind speed, incoming and outgoing solar radiation, and temperature and humidity of the air. The RMSD and the \( R^2 \) were about 43 W m\(^{-2}\) and 0.7, respectively. Despite the complexity of the site induced by the strong heterogeneity in the soil moisture which is related to the employed irrigation method (flood irrigation), and the consequences in terms of the footprint of the instruments, the obtained statistical results showed that both aggregation schemes performed successfully with regard to estimates of the evapotranspiration over heterogeneous grids.

Finally, to further assess the performance of the developed approach, a second dataset collected in northern Mexico has been also used. The result shows that the approach provides acceptable values of aggregated evapotranspiration. Consequently, scintillometry can potentially be used in the development and the validation of aggregation approaches to improve the representation of surface heterogeneity land-surface-atmosphere models operating at large scales.

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1. Introduction

Regions classified as semi-arid or arid constitute roughly one-third of the total global land surface. In these regions, due to the combined effect of human intervention and the expected modification of precipitation pattern water managers are faced...
with several challenges. Among them, water resource scarcity combined to increase of water demands, competition among different water user groups, which lead to over-exploitation of aquifers. The serious environmental and socio-economic consequences of these factors have led the earth science community to investigate the issue of the impact of human and natural induced changes on the hydrological cycle and water resources with the ultimate objective of developing tools so that managers and politicians can make decisions based on state of the art science. In this context, a strong emphasis has been directed toward understanding the processes controlling the exchanges of water and energy between the land surface and the atmosphere. Due to the importance of the evapotranspiration (ET) flux in the water cycle, especially in arid and semi-arid regions, efforts have been particularly oriented toward improving its estimates at different space-time scales. However, quantifying diurnal ET variation over large and heterogeneous areas is not straightforward (Kustas and Norman, 2000).

In this regard, remotely sensed data can be a valuable tool to address this issue (Kustas and Norman, 1996, 1999; Kustas et al., 2001, 2004; Norman et al., 1995, 2003, 2006). Geostationary sensors can provide regional scale of ET with temporal sampling from 15 min to 1 h, but their spatial resolution is very coarse. In fact, a single pixel may contain surfaces with widely varying characteristics (mixed fields), which make the interpretation of the data very difficult. In contrast, sun-synchronous satellites provide data with better spatial resolution, but the temporal resolution is poor. Therefore the issue of discrepancy between the space-time scale of satellite observation and that at which the process needs to be described is still an open research question (McCabe and Wood, 2006).

For the purpose of irrigation management, the combination of the sun-synchronous sensors data and aggregation schemes can provide a workable solution (Chehbouni et al., 2008a). The aggregation scheme is conceived as a method which seeks to link the model parameters that control surface exchange on a patch scale with the area-average value of equivalent model parameters applicable on a larger scale or grid-scale, assuming that the same equations are used to describe surface fluxes at both scales. In this regard, substantial progress has been made in the last decade to develop aggregation schemes which range from physically based through semi-empirical, to entirely empirical (Braden, 1995; Chehbouni et al., 1995; Raupach and Finnigan, 1995) or experimental studies (Araùn et al., 1996; Blyth and Harding, 1995; Chehbouni et al., 2000a; Moran et al., 1997; Noilhan et al., 1997; Sellers et al., 1997). However, one of the main difficulties regarding the development of these aggregation procedures is the evaluation of their outputs/performances against ground observations. The straightforward solution is to deploy a network of patch scale measurement devices such as eddy correlation systems. However, due to the high cost of the devices and the requirement for continuous availability of well-trained staff to operate and maintain them, this solution cannot be implemented on an operational basis.

In this context, scintillometry can be considered as an attractive method for routinely measuring area-averaged surface fluxes. Using a Large Aperture Scintillometer (LAS), one can obtain area-averaged surface fluxes over distances from a few hundred metres up to several kilometres. Recently, several investigations have indeed demonstrated its potential to derive area or path average of the sensible heat flux over large and heterogeneous surfaces (Asanuma and Lemoto, 2006; Chehbouni et al., 1999, 2000b, in press; Ezzahar et al., 2007a, 2009; Hoedjes et al., 2007; Kleissl et al., 2006; Lagouarde et al., 2002; Marx et al., 2008; Watts et al., 2000). The combination of LAS measurements and estimates of available energy can provide reasonable retrieval of area-averaged ET as the residual term of the energy-balance equation (Chehbouni et al., 2000b, in press; Ezzahar et al., 2007b, 2009; Hemakumara et al., 2003). Consequently, the scintillometer (LAS), is becoming popular in hydrometeorological studies, because it is relatively cheap, robust and easy to operate and maintain.

The main objective of the current study is to assess whether the LAS can be used to validate spatial and temporal aggregation schemes at grid-scale by comparing the ET derived from the LAS and those estimated from both aggregation methods. For the spatial aggregation method, the ET was obtained as the residual term of the energy balance providing the estimates of the available energy and sensible heat flux using ground-based radiometric surface temperature measurements and an ancillary micrometeorological data. For the temporal aggregation method, the ET was obtained by extrapolating the instantaneous values of the available energy and the evaporative fraction estimated at the satellite overpass to daily ones using a simple heuristic approach developed by Chehbouni et al. (2008a). This approach used the radiometric surface temperature derived at the satellite overpass and an ancillary micrometeorological data. The particularity of the studied is related to two factors. First, the nature of the study site is very complex: tall, sparse, large and contrasted olive trees fields and the method employed for irrigation (flood irrigation) which amplifies the heterogeneity of the grid. Second, as far as we know, this is the first study where that the LAS has been used to validate both spatial and temporal aggregation schemes.

2. Experiment site and measurements

The experiment was carried out in the fall of 2002, between day of year (DOY) 295 and 306 (22 October to 2 November) in a 275-ha Agdal olive orchard which is located to the southeast of Marrakech, Morocco (31°36.0 N, 07°58.5 W). This experiment was a part of the SUDMED project (Chehbouni et al., 2008b) which took place in the southern Mediterranean region (Marrakech, Morocco), to assess the spatio-temporal variability of water needs and consumption for irrigated crops during water shortages. In this section, site description and experimental set-up are briefly summarized; the
reader is referred to Ezzahar et al. (2007a) for a complete description. Fig. 1 displays the area of interest on a very high spatial resolution image acquired by the Quickbird satellite. The climate is typically semi-arid Mediterranean; precipitation falls mainly during winter and spring (about 75% of the total precipitation), from the beginning of November until the end of April, with an average ranging from 192 to 253 mm per year. The atmosphere is dry with an average relative humidity of 56% and the evaporative demand is very high (1600 mm per year, Er-Raki et al., 2008), greatly exceeding the annual rainfall.

The experimental area is divided into two sites, which were relatively homogeneous in terms of vegetation types, but differ strongly in characteristics (mainly soil moisture status, and, to a lesser extent, vegetation percent cover). These sites are referred to as the “southern site” and the “northern site” (see Fig. 1). The average height of the olive trees during the experiment period was 6.5 m at the southern site and 6 m at the northern site. The mean fraction cover was approximately 55% at the southern site and 45% at the northern site, as obtained from hemispherical canopy photographs (using a Nikon Coolpix 950® with a FC-E8 fish-eye lens converter, field of view 183°).

Both sites were equipped with a set of standard meteorological instruments to measure wind speed and direction (model Wp200, R.M. Young Co., Traverse City, MI, USA); air temperature and humidity (model HMP45AC, Vaisala Oyj, Helsinki, Finland) at 9 m above the ground. These instruments were set up 9 m above ground. Net radiation was measured using net radiometers (a model CNR1, Kipp and Zonen, Delft, The Netherlands at the southern site and a model Q7, REBS Inc., Seattle, WA, USA at the northern site). These radiometers were placed at 8.5 m height to embrace vegetation and soil radiances by ensuring the field of view was representative of their respective cover fractions. The CNR1 measures the four components of the net radiation, i.e. independent estimates incoming and outgoing solar and far-infrared radiation. In order to calculate the albedo over the northern site, two pyranometers (model CM5, Kipp & Zonen, Delft, The Netherlands) were mounted to measure incoming and outgoing short-wave radiation. Soil and vegetation surface temperatures were measured using two infrared thermometers (model IR7S-Ps, Apogee Instruments Inc., Logan, UT, USA), with a 3:1 field of view, at heights of 1 and 8.4 m respectively. Soil heat flux density was measured at a depth of 0.01 m using soil heat flux plates (HFT3-L, Campbell Scientific Ltd.) which were installed at three locations in order to get good average values; underneath the canopy (always shaded), in between the trees (mostly sunlit), and in an intermediate position. Time Domain Reflectometry (TDR) probes (model CS616, Campbell Scientific Ltd.) were installed at depth of 0.05 m to measure soil water content. Their outputs have been calibrated using the gravimetric method. The slope, the intercept and the correlation coefficient of the obtained linear regression were 66.58 and 0.96 respectively. Measurements were taken at 1 Hz, and averages stored at 30-min intervals on CR10X data loggers (Campbell Scientific Ltd.). The prevailing wind direction during the study period was from the northwest. The half-hourly values of the measured climatic variables including the air temperature, air relative humidity, incoming solar radiation, and wind speed are shown in Fig. 2.

Besides the standard meteorological measurements, two eddy covariance systems were installed to provide continuous measurements of the vertical fluxes of heat, water vapour and CO₂ at a height of 8.8 and 8.7 m for the southern and northern sites, respectively. The EC systems consisted of a 3D sonic anemometer (CSAT3, Campbell Scientific Ltd.) and an open-path infrared gas analyzer (LI7500, Licor Inc.). Raw data were sampled at a rate of 20 Hz and were recorded using CR23X dataloggers (Campbell Scientific Ltd.) which were connected to portable computers to enable storage of large raw data files. The half-hourly values of fluxes were later calculated off-line after performing coordinate rotation, frequency corrections, correcting the sonic temperature for the lateral velocity and presence of humidity, and the inclusion of the mean vertical velocity according to Webb et al. (1980). Data from the eddy covariance system were processed using the

Fig. 2. Half-hourly values of weather variables during the study period.
software ‘EcPack’ developed by the Meteorology and Air Quality Group, Wageningen University (available for download at http://www.met.wau.nl/).

Two identical Large Aperture Scintillometers were mounted at heights of 14 m in the southern site and 14.5 m in the northern site (see Fig. 1). These instruments were constructed by the Meteorology and Air Quality Group (Wageningen Agriculture University, The Netherlands) and were originally designed by Ochs and Wilson (1993). They have an aperture size of 0.15 m and the transmitter operates on a wavelength of 0.94 μm. At the receiver, \( C_2^s \) is sampled at 1 Hz and stored as 1-min averages using a CR510 data logger (Campbell Scientific Ltd.). Over the southern site, the LAS was installed perpendicular to the dominant wind direction, over a path length of 1050 m. The transmitter was mounted on a tripod installed on a roof located near the southwestern corner of the southern site, while the receiver was mounted on a 15-m-high tower that was positioned next to the road that separates the two sides of the orchard. Over the northern site, the LAS was almost parallel to the dominant wind direction, and it measured over a path length of 1070 m. The transmitter was mounted on a tripod installed on a roof located near the northern corner of the northern site. The receiver was installed on the same tower as the receiver of the LAS installed over the northern site in such a manner that the two signals did not interfere. The measured values of \( C_2^s \) were used to derive the sensible heat fluxes (see Appendix A) and the evapotranspiration from the LAS was calculated by imposing the energy-balance closure assumption using the measured net radiation and the measured soil heat flux. Ezzahar et al. (2007a) have evaluated the accuracy of the both scintillometers by comparing the derived sensible heat fluxes with those measured with eddy covariance systems for the same period of the current study. The obtained linear regression yielded a slope of 0.95 (1), a correlation coefficient of 0.89 (0.74) and a root mean square difference of 24 W m\(^{-2}\) (27 W m\(^{-2}\)) for the southern site (northern site). The statistical results of these comparisons showed a better agreement for the southern site than for the northern site due to the contrast between the two sites in terms of water availability. Indeed, in addition to the difference in the cover and height of vegetation between the two sites, the period of this study was chosen in order to have a distinct difference between the two sites in term of soil moisture. The southern site was dry and the northern site had just been irrigated. Fig. 3 shows the evolution of the volumetric water content throughout the experiment. From Fig. 3, it is clear that the grid, comprised of the northern and southern sites, is very heterogeneous. Therefore, this study presents a good opportunity to estimate the ET over heterogeneous grids.

3. Modeling approach

3.1. Model for surface flux estimates

3.1.1. Sensible heat flux

For homogeneous vegetation cover conditions, a single-source Soil-Vegetation-Atmosphere Transfer (SVAT) model may be suitable for estimating the sensible heat flux; however in most cases the landscape is under partial vegetation canopy so that soil and vegetation contribution to the sensible heat flux exchange should be explicitly taken into account (Norman et al., 1995). For more complex canopies as the present study site, a two-source energy-balance model provides a more realistic representation of the sensible heat flux exchanges with the lower atmosphere (Lhomme et al., 1994; Merlin and Chehbouni, 2004; Norman et al., 2000). In this specific study, the sensible heat flux is estimated using the simple two-layer model developed by Lhomme et al. (1994). Here, only a brief description of the model is provided, the reader is referred to Lhomme et al. (1994) for a complete description. According to Lhomme et al. (1994), the sensible heat flux at the patch scale is expressed as follows:

\[
H_{\text{Mod}} = \rho c_p \left( \frac{T_a - T_s}{r_a - r_e} \right) \frac{R_{\text{net}}}{c_0} \frac{e}{T_a} \frac{T_a - T_r}{r_a - r_e} \tag{1}
\]

where \( r_a \) is the aerodynamic resistance to heat transfer between the level of apparent sink of momentum and the reference height (\( \text{sm}^{-1} \)) (Brutsaert, 1982). \( r_e \) is calculated using the classical formulae which take into account the stability correction functions for wind and temperature (Brutsaert, 1982). \( T_r \) is the surface temperature (K), and \( r_a \) is the equivalent resistance defined by:

\[
r_a = \frac{r_{af} r_{as}}{r_{af} + r_{as}} \tag{2}
\]

where \( r_{as} \) is the aerodynamic resistance between the soil and the canopy source height (Shuttleworth and Gurney, 1990) and \( r_{af} \) is the bulk boundary layer resistance of the canopy (Choudhury and Monteith, 1988). The term \( \delta T \) represents the temperature difference between the foliage and the soil. Lhomme et al. (1994) have linked statistically \( \delta T \) to \( (T_a - T_s) \) by the following empirical equation:

\[
\delta T = a(T_r - T_s)^m \tag{3}
\]

Finally \( c \) is given by

\[
c = \frac{1}{1 + \left( \frac{r_{af}}{r_{as}} \right)^m} - f_v \tag{4}
\]

where \( f_v \) is the fractional vegetation cover, \( a \) and \( m \) are empirical coefficients (a positive real number and \( m \) positive integer) which were determined statistically by adjusting \( H \) estimated to \( H \) observed. The value of 0.25 and 2 were used respectively for \( a \) and \( m \) (Hoedjes et al., 2008).

3.1.2. Available energy

In general, the estimation of the evapotranspiration as the residual term of the energy-balance equation over a heterogeneous grid requires, additionally to the sensible heat flux estimates, a network of the net radiometers and the soil heat flux in order to capture the heterogeneity of the grid, which is also costly and not really feasible for operational purposes. Therefore, we proposed to estimate the available energy using a simple model which uses radiometric surface temperature, albedo and incoming solar radiation data (Chehbouni et al., 2008)). This model is described as follows:

Fig. 3. Evolution of the volumetric water content during the experimental period for the southern site (dotted line) and northern site (solid line).

3.1.2.1. Net radiation. The net radiation quantifies the energy available for crop evapotranspiration, photosynthesis, and soil heating (Monteith and Unsworth, 1990). It is the difference between the incoming and outgoing shortwave and longwave radiation fluxes, and is expressed as follows:

\[ R_n = (1 - \alpha)R_s + \varepsilon_a \sigma(e_aT_a^4 - T_0^4) \]  (5)

where \( \alpha \) is the surface albedo, \( R_s \) is the global solar radiation, \( \varepsilon_a \) is the surface emissivity which has an almost constant value (in practice 0.98), and \( T \) is the surface temperature. Both \( R_s \) and \( T \) can be expressed in function of air temperature and surface temperature (Monteith and Unsworth, 1990; Duarte et al., 2006), respectively. Then, Eq. (5) can be rewritten as:

\[ R_n = (1 - \alpha)R_s + \varepsilon_a \sigma(e_aT_a^4 - T_0^4) \]  (6)

3.2. Aggregation procedures

In this section, two aggregation algorithms are presented to estimate the diurnal course of evapotranspiration at the grid-scale: spatial aggregation which consists of upsampling the patch measurements/or estimates to grid-scale estimates and the temporal aggregation which consists of extrapolating the grid-scale instantaneous values which can be derived from remote sensing to daily values. In what follows, the area-averaged over the grid is denoted by the angle bracket \( \langle \cdot \rangle \).

3.2.1. Spatial aggregation

In the following, the theory which underlies essential aspects of the application of the spatial aggregation algorithm to formulate the grid-scale surface fluxes is described. The spatial aggregation is conceived as a method which seeks to link the model parameters which control surface exchange on a patch scale with the area-average value of equivalent model parameters applicable at larger, model grid-scale, and to adopt the equations that are accepted as reasonable descriptions of surface-atmosphere exchanges at the patch scale to describe the area-averaged behavior of heterogeneous cover on the grid-scale. The strategy adopted in this current study to infer grid-scale surface fluxes is based on two assumptions (Shuttleworth et al., 1997; Chehbouni et al., 2000a, 2008a): the first one consists in determining grid-scale surface fluxes in such a way that the flux equations on the grid-scale must have the same form as those used on a patch scale but whose arguments are the aggregate expressions of those on the patch scale. The second one stipulates that “the effective or area-average value of land surface parameters is estimated as a weighted average over the component cover types in each grid through that function involving the parameter which most succinctly expresses its relationship with the associated surface flux” (Shuttleworth et al., 1997). Expressions of grid-scale surface fluxes (denoted by angle brackets) resulting from the application of this simple aggregation rule are given below:

\[ \langle R_n \rangle = (1 - \alpha)\langle R_s \rangle + \langle \varepsilon_a \rangle \sigma(\langle e_a \rangle \langle T_a \rangle^4 - \langle T_0 \rangle^4) \]  (9)

\[ \langle G \rangle = \frac{A \cos \left[ \frac{2\pi(t + 10800)}{B} \right]}{\langle R_n \rangle} \]  (10)

\[ \langle H_{Sim} \rangle = \rho c_p \left[ \langle T_K \rangle - \langle T_a \rangle \right] - \left( \langle [\varepsilon_a] \langle T_a \rangle + \langle [\varepsilon_d] \rangle \right) - \int f(\langle T_K \rangle - \langle T_a \rangle)^m \right] \]  (11)

Similarly, the application of the second assumption leads to the following set of relationships between local (subscript \( i \)) and effective (in brackets) radiative temperature, surface emissivity, surface albedo, displacement height and roughness length (Chehbouni et al., 2008a):

\[ \langle T_K \rangle = \left[ \sum_i f_i \langle T_K \rangle^2 \right]^{0.25} \]  (12)

\[ \langle \rho_a \rangle = \sum_i f_i \langle \rho_a \rangle \]  (13)

\[ \langle \alpha \rangle = \sum_i f_i \langle \alpha \rangle \]  (14)
where \( f_i \) is the fraction of the surface covered by the patch \( i \) with
obviously \( \sum_i f_i = 1 \). \( T_{\text{hi}} \) is the radiometric surface temperature over
the diurnal cycle. In this study, \( T_{\text{hi}} \) was derived from measured soil and
Canopy temperatures weighted by the fractional area of vegetation
(Ezzahar et al., 2007b; Norman et al., 1995) as follows:

\[
T_{\text{hi}} \approx (f_i T_{\text{hi}} + (1 - f_i) T_{s4})^{1/4}
\]

where \( f_i \) is the cover fraction of olive trees, and \( T_{\text{hi}} \) and \( T_s \) are
the measured soil and canopy temperatures respectively, using two
infrared thermometers. \( \alpha_i, \beta_i, \gamma_i \) and \( d_i \) are the surface emissivity, the
albedo, the roughness length and the displacement height for the patch \( i \).

Finally, the grid-scale evapotranspiration derived from the
spatial aggregation method (denoted as \( ET_{\text{SimSA}} \)) can be obtained
as the residual term of the energy-balance equation:

\[
\langle ET_{\text{Sim}} \rangle_{\text{SA}} = \langle R_b \rangle - \langle (H + L E) \rangle (G)
\]

Although this method seems very practical for estimating
surface fluxes. However, as stated by Chehbouni et al. (2000a), it
has a major limitation since its derivation is from semi-empirical
relationships between the local and effective surface parameters
are not always theoretically supported. In the regard, the
relationship between model and observational variables (see
Eq. (3)), which is established at patch scale, can introduce
additional errors when extended to grid-scale. However, the
finding of Chehbouni et al. (2000a, 2008a) seems to indicate that
these errors have a limited impact on surface flux estimates.

Nevertheless, establishing physically based relationships between
model and observational variables at grid-scale is an ongoing
research topic.

3.2.2. Temporal aggregation

Grid-scale evapotranspiration (\( ET \)) can be also determined
using remote sensing data in conjunction with an energy-balance
model. Practically, the sun-synchronous sensors are the most
suitable for deriving \( ET \) (French et al., 2005; Chehbouni et al.,
2008a). However, these sensors provide only instantaneous values
at the satellite overpass. These are of limited interest to water
managers who are primarily focusing on daily values of \( ET \)
(Bastiaanssen et al., 2000). Several methods have been proposed
for extrapolating instantaneous \( ET \) to daily values. The simplest
consists of relating daily \( ET \) to the instantaneous near surface
vertical temperature gradient at midday (Jackson et al., 1977), or
assuming the ET diurnal course is similar to that of solar irradiance,
to be approximated by a sine function. However, due to their
empirical character, both method accuracies are limited (Zhang
and Lai, 1995). Another possibility is assuming a constant
daytime evaporative fraction \( (EF=ET/AE) \) to be used with daily
available energy \( (AE=R_b+G) \) for deriving daily ET (Sugita
and Brutsaert, 1991; Gomez et al., 2005). The \( EF \) is defined as the ratio
of \( ET \) to the available energy, AE. Recently, Hoedjes et al. (2008)
have shown that assuming a constant daytime \( EF \) to derive
accurate ET cannot be generalized to all surface conditions. Under
dry conditions, the constant \( EF \) assumption seems to lead to
reasonable results with regard to daily ET estimation. While under
wet conditions, \( EF \) depicts a concave up shape with a pronounced
decrease during early morning and a sharp increase during late
daylight afternoon (see Fig. 2 in Hoedjes et al., 2008). Furthermore, since
the largest evaporative fluxes occur during these conditions, the use of
a diurnal constant value of \( EF \) induces a large error in the
calculation of ET.

To overcome this problem, Hoedjes et al. (2008) have proposed
a new heuristic approach to parameterize the diurnal course of \( ET \)
over homogeneous surfaces using the atmospheric parameters and
soil moisture status (dry or wet). This approach has been
generalized by Chehbouni et al. (2008a) to a mixture of contrasted
fields (cotton, chickpea and wheat) in northern Mexico. In the
current study, we applied the same method developed by
Chehbouni et al. (2008a) to derive \( EF \) over a grid sparse olive
tree canopy. Compared to earlier studies, our investigations were
performed in difficult environmental conditions due to the type of
vegetation (tall and sparse vegetation), and the irregular space-
time soil moisture pattern induced by the type of irrigation. On the
grid-scale, the actual \( EF \) diurnal course parameterized when
accounting for both atmospheric demand and soil moisture status is
given by Chehbouni et al. (2008a):

\[
\langle EF_{\text{Sim}} \rangle_{\text{ET}} = \begin{cases} \langle EF_{\text{Sim}} \rangle_{\text{ET}}^{1130} & \text{if } \langle p^{1130} \rangle_{\text{ET}} \leq 1.5 \\
\langle EF_{\text{Sim}} \rangle_{\text{ET}}^{1130} & \text{if } \langle p^{1130} \rangle_{\text{ET}} > 1.5 \end{cases}
\]

\( \langle EF_{\text{Sim}} \rangle_{\text{ET}} \) is the EF diurnal course parameterized when accounting for
atmospheric demand (i.e. global solar radiation \( R_g \) and relative
humidity (RH)) only, which is formulated as:

\[
\langle EF_{\text{Sim}} \rangle_{\text{ET}} = 1.2 - \frac{0.4 R_g}{1000} + 0.5 \frac{RH}{100}
\]

\( p^{1130} \) is a correction factor given by:

\[
EF^{1130} = \frac{\langle EF_{\text{Sim}} \rangle_{\text{ET}}^{1130}}{\langle EF_{\text{Sim}} \rangle_{\text{ET}}^{1130}}
\]

where \( \langle EF_{\text{Sim}} \rangle_{\text{ET}} \) is \( EF_{\text{Sim}} \) at 11:30 UTC, and \( \langle EF^{1130} \rangle \) is the EF
estimated from remote sensing observations at 11:30 UTC calculated as:

\[
\langle EF^{1130} \rangle = (\langle AE \rangle_{\text{ET}}^{1130} - \langle H \rangle_{\text{ET}}^{1130}) / \langle AE \rangle_{\text{ET}}^{1130}
\]

where \( \langle H \rangle_{\text{ET}}^{1130} \) is the value of the sensible heat flux at 11:30.
The latter was estimated from Eq. (11) using the effective radiometric
surface temperature (Eq. (12)). \( \langle AE \rangle_{\text{ET}}^{1130} \) is the
estimated available energy at 11:30 UTC calculated by combining
Eqs. (9) and (10) using also the effective radiometric surface
temperature.

In this study, the time of 11:30 UTC was chosen since it
according to the local time of overpass of the ASTER satellite
(Hoedjes et al., 2008). When choosing the AVHRR overpass time
over north-western Mexico, i.e. 14:00 UTC, Chehbouni et al.
(2008a) have shown that this parameterization was also reasonable.
In addition to the parameterization of \( EF \), retrieval of the
diurnal course \( EF \) requires also \( AE \) over the diurnal cycle, which
is not routinely available. Here again, the same heuristic approach
developed by Chehbouni et al. (2008a) on the grid-scale, was used
in this specific study. This approach combines the instantaneous
remote sensing observations of \( AE \) \( \langle (AE) \rangle_{\text{ET}}^{1130} \) at 11:30 UTC with a
function \( f \) involving the meteorological information which can be
obtained from observation networks and/or weather forecasts.
to derive AE diurnal courses. The latter is expressed as:

$$\frac{(AE)^2}{\langle AE \rangle_{\text{Sim}}} = f \left( \frac{\langle R \rangle^t}{R^{1130}} \right)^2$$  \hspace{1cm} (22)

where $R^t$ is a function given by:

$$\langle R^t \rangle = (1 - \alpha) R^t_s + \alpha \sigma(T)^t$$  \hspace{1cm} (23)

where $t$ is the time of the day, $f$ is the following 2nd order function:

$$f \left( \frac{\langle R \rangle}{R^{1130}} \right) = a_2 \left( \frac{\langle R \rangle}{R^{1130}} \right)^2 + a_1 \left( \frac{\langle R \rangle}{R^{1130}} \right) + a_0$$  \hspace{1cm} (24)

where $a_0$, $a_1$, and $a_2$ are empirical coefficients established by Hoedjes et al. (2008) as 0.48495, 1.15120 and 0.34285, respectively, when calibrating this function over a homogenous olive orchard in Morocco. Using the same coefficients, Chehbouni et al. (2008a) have extended the AE parameterization with success to grid-scale. It is of importance to notice that outgoing long wave radiation is purposely not introduced in Eq. (23). This was made to avoid the requirement for daily course of surface temperature which is not available at the appropriate space scale.

Finally, the grid-scale evapotranspiration (denoted, $(ET)_{TA}$) is obtained as follows:

$$ET_{TA} = \left( \frac{ET_{\text{Sim}}}{AE} \right) f$$  \hspace{1cm} (25)

### 4. Results and discussion

In this study, only daytime observations have been considered, since the most important surface fluxes occur during this interval, and the behavior of the temperature structure parameter is not well known for stable conditions which can create greater uncertainty in the fluxes, especially over heterogeneous surfaces. Note that the half-hourly time scale is used in all analysis. This section will be organized as follows: firstly a comparison between the sensible heat fluxes derived from the LAS and those estimated using the Lhomme et al. (1994) model on the grid-scale. Secondly, we compare the LAS-derived diurnal course of the evapotranspiration and that estimated using spatial and temporal aggregation schemes on the grid-scale.

#### 4.1. Sensible heat fluxes

Before evaluating the accuracy of the application of the Lhomme et al. (1994) model on the grid-scale, we first present in Fig. 4 the daily average daytime values of the sensible heat flux derived from the LAS over the northern and southern sites during the study period.

![Fig. 4. Daily average daytime values of the sensible heat flux derived from the LAS over the northern and southern sites during the study period.](image)

At the patch scale, the Lhomme et al. (1994) model has been tested with success using the data collected over the southern site (Hoedjes et al., 2007, 2008). However, as far as we know such a study of the applicability of the Lhomme et al. (1994) model to the grid-scale has never been performed before. In this study, an effort has been made to apply this model over a heterogeneous grid which comprised the northern and southern sites using the aggregation rules. The simulated grid-scale sensible heat flux $(H_{\text{Sim}})$ was estimated using Eq. (11). Since satellite based surface temperature measurements were not available, ground-based surface temperature measured over each patch were used to construct grid-scale surface temperature using Eq. (12). Similarly, Eqs. (15) and (16) have been used to derive grid-scale displacement height and roughness length. Note that their patch scale values were derived as fraction of the vegetation height.

The effectiveness of this approach should have been validated by installing one scintillometer spanning the entire grid-scale. However, this could not be achieved easily for practical reasons since this unique scintillometer should have been installed much higher than the two LAS used in this study in order to avoid saturation.

To overcome this problem, Ezzahar et al. (2007a) developed a new approach to infer an aggregated structure parameter of the refractive index on the grid-scale $(C_n^2)$ using the same data collected in the current study. This approach combines LAS patch scale measurements, meteorological data and aggregation schemes. For more details the reader can refer to Ezzahar et al. (2007a). It is worth mentioning that the obtained $(C_n^2)$ behaved according to Monin–Obukhov Similarity Theory. Then, this $(C_n^2)$ was used to derive the grid-scale sensible heat flux $(H_{\text{AS}})$ by applying MOST at the grid-scale. The accuracy of this approach has been investigated by comparing $(H_{\text{AS}})$ to the area average of sensible heat flux measured by the eddy covariance systems which were installed on the meteorological towers (see Fig. 1). The result of this comparison showed a good agreement with a RMSD = 20.3 W m$^{-2}$ and $R^2 = 0.89$ (Ezzahar et al., 2007a). Here, the values obtained for $(H_{\text{AS}})$ in Ezzahar et al. (2007a) have been used to validate $(H_{\text{Sim}})$ (Fig. 5). Fig. 5 displays the comparison between $(H_{\text{AS}})$ and $(H_{\text{Sim}})$: The RMSD is 30 W m$^{-2}$ and the correlation coefficient and the slope associated with the linear regression.
forced to the origin were 0.76 and 0.90, respectively. This result indicates that the aggregation schemes are not exact and errors are associated with some of the assumptions used to drive them. Additionally, some scatter is related to the footprint effect of the scintillometers (see Fig. 6). Nevertheless, considering the complexity of the study site, the obtained result is very encouraging. Consequently, it can be concluded albeit its simplicity, the Lhomme et al. (1994) model, can be considered a suitable model for estimating the sensible heat fluxes using the effective radiometric surface temperature over heterogeneous grids.

4.2. Evapotranspiration

4.2.1. Spatial aggregation

Before evaluating the accuracy of the evapotranspiration derived from the spatial aggregation, we compare first the grid-scale available energy ($\langle AE_{\text{Sim}} \rangle$) against the ground-based measurement (denoted $\langle AE_{\text{Meas}} \rangle$) in Fig. 7. The $\langle AE_{\text{Sim}} \rangle$ was obtained by combining Eqs. (9) and (10). Here again, the estimation of the $\langle AE_{\text{Sim}} \rangle$ used the effective radiometric surface temperature ($H_{\text{Sim}}$) through Eq. (9). The effective surface emissivity and albedo required for the estimation of the $\langle AE_{\text{Sim}} \rangle$, were derived from Eqs. (13) and (14). The $\langle AE_{\text{Meas}} \rangle$ was derived as area-weighted averages of those measured over the southern and the northern sites. The correspondence between $\langle AE_{\text{Sim}} \rangle$ and $\langle AE_{\text{Meas}} \rangle$ was quite good. The RMSD value was 40 W m$^{-2}$, and the linear regression forced to the origin yielded a 0.89 slope value and a 0.98 correlation coefficient. It should be noted that in this specific study, the atmospheric radiation was estimated using Brutsaert’s formula without cloudiness correction; because the experiment period included few cloudless data. Except DOY 295, all days were sunny (see Fig. 2). Therefore, the use of Brutsaert’s equation will not introduce significant error in the estimation of atmospheric radiation. However, there might be other sources of errors such as those related the uncertainty associated with the aggregation method which is purely of a semi-empirical nature, as well as those associated with the measurement of net radiation which ranges from 5% to 7% for instruments of the same manufacture and 10% to 15% between manufacturers (Field et al., 1992). It is also possible that some error compensation might have occurred which may explained the fact that difference between the estimated and measured available was less than expected even over homogeneous surfaces.

Using values of $\langle AE_{\text{Sim}} \rangle$ and $\langle H_{\text{Sim}} \rangle$ which were calculated using the effective radiometric surface temperature (see Eqs. (9)–(11)), the diurnal course of grid-scale evapotranspiration, $\langle ET_{\text{Sim}} \rangle_{\text{SA}}$ was estimated as the residual term of the energy-balance equation (Eq. (18)). $\langle ET_{\text{Sim}} \rangle_{\text{SA}}$ was compared to the grid-scale evapotran-

spiration \((ET_{LAS})\) derived from the LAS as the difference between \((AE_{ET,Sim})\) and \((H_{LAS})\) in Fig. 8. The RMSD between \((\text{ET}_{\text{Sim}})_{\text{SA}}\) and \((\text{ET}_{\text{Sim}})_{\text{h}}\) was 46 W m\(^{-2}\) and the correlation coefficient and the slope associated with the linear regression forced to the origin were 0.78 and 0.87, respectively. This confirms the results reported by several authors where the potential of the LAS to derive accurate evapotranspiration has been demonstrated (Ezzahar et al., 2007b, 2009; Chehbouni et al., 2000b, in press; Hemakumara et al., 2003; Hoedjes et al., 2002). It should be noted that the problem of closure of the energy balance has no big effect on the results, because both approaches forced the energy-balance closure. Such discrepancy can be explained by the combination of two factors. First, the error associated to the impact of the footprint. Second, since the ET is obtained as the residual term of the energy-balance equation, any difference between measured and estimated available energy and sensible heat flux is directly translated into error in the estimated ET. However, despite the observed scatter, the correspondence between \((\text{ET}_{\text{Sim}})_{\text{SA}}\) and \((\text{ET}_{\text{Sim}})_{\text{h}}\) is acceptable considering the difficulty in estimating grid-scale latent heat flux over such complex grid. Finally, it can be concluded that the spatial aggregation procedure yielded reasonable grid surface fluxes estimates.

4.2.2. Temporal aggregation

In this section, an effort has been made to extend the heuristic approach which consists of extrapolating instantaneous values to daily ones proposed by Hoedjes et al. (2008) over a homogeneous patch to a heterogeneous grid (tall and sparse vegetation, irrigation method employed). Before obtaining the grid-scale evapotranspiration using the temporal aggregation, the grid-scale of available energy \((AE_{\text{Sim}})\) estimated using Eq. (22), was compared to the ground-based measurements \((AE_{\text{Meas}})\) in Fig. 9. The correspondence between \((AE_{\text{Sim}})\) and \((AE_{\text{Meas}})\) was quite good. The RMSD value was 47 W m\(^{-2}\), and the linear regression forced to the origin yielded a 0.90 slope value and a 0.91 correlation coefficient. By comparing these results with those obtained when we used the spatial aggregation, it can be seen that in addition to the error related to the spatial aggregation, the use of the temporal aggregation generates an added extra error in the estimation of \(AE\) (about 21%). However, considering the complexity of the grid, the footprint effect and the error associated with the assumptions used to drive aggregation rules, it can be concluded that the proposed heuristic approach leads to reasonable estimates of the diurnal course area average available energy. The results of this study confirm and generalize the findings of Hoedjes et al. (2008) who established this heuristic approach on the southern site which was one of the two patches of our grid-scale study as well as those established by Chehbouni et al. (2008a) over short vegetation.

Finally, the diurnal course of the grid-scale evapotranspiration, \((\text{ET}_{\text{Sim}})_{\text{SA}}\), was retrieved using Eqs. (19)–(25). Fig. 10 displays the validation of these \((\text{ET}_{\text{Sim}})_{\text{TA}}\) retrievals, against values derived from the LAS \((\text{ET}_{\text{LAS}})\). Also included is the grid-scale evapotranspiration calculated by considering a constant diurnal evaporative fraction (EF) equal to that at 11 H30 (EF\(_{11:30}\)). It can be clearly seen that taking into account the diurnal variation of EF significantly improves \((\text{ET}_{\text{Sim}})_{\text{TA}}\) retrieval. RMSD between \((\text{ET}_{\text{Sim}})_{\text{TA}}\) and \((\text{ET}_{\text{Sim}})_{\text{h}}\) was 3 W m\(^{-2}\), the relative error was 19% and the slope was 0.88, as compared to 52 W m\(^{-2}\), 27% and 0.82, respectively when using a constant EF. These results corroborated with those established by Hoedjes et al. (2008) and Chehbouni et al. (2008a). Additionally, by properly taking into account the effect of the grid heterogeneity due to both vegetation and soil moisture variations along the grid and the error associated to the application of the aggregation rules, the agreement between \((\text{ET}_{\text{Sim}})_{\text{TA}}\) and \((\text{ET}_{\text{LAS}})\) is considered to be acceptable.

In general, as for the spatial aggregation scheme, the temporal aggregation method can be considered suitable for practical purposes. Indeed, the spatial aggregation needs the diurnal courses of the radiometric surface temperature for calculating the sensible heat fluxes and the available energy. However, this variable cannot be obtained using remote sensing technique at the required scale for irrigation management purposes (a few hundred meters resolution). Geostationary sensors can provide the diurnal courses of spatially radiometric surface temperature with temporal sampling from 15 min to 1 h, but their spatial resolution is very coarse. The advantage of combining spatial and temporal aggregation schemes is to be able to estimate daily value of ET at the grid-scale using a single value of surface temperature at the satellite overpass time.

**Fig. 9.** Comparison between the estimated \((AE_{\text{Sim}})\), obtained using the temporal aggregation scheme (Eq. (22)) and observed \((AE_{\text{Meas}})\), obtained as area-weighted averages of those measured over both sites) area-averaged available energy.

**Fig. 10.** Comparison between \((\text{ET}_{\text{Sim}})_{\text{SA}}\) (estimated using the temporal aggregation scheme through Eqs. (19)–(25)) and \((\text{ET}_{\text{Sim}})_{\text{h}}\) (obtained form the LAS as the difference between the \((AE_{\text{meas}})\) and \((\text{ET}_{\text{LAS}})\). Also included is the grid-scale evapotranspiration calculated by considering a constant diurnal evaporative fraction (EF) equal to that at 11 H30 (EF\(_{11:30}\)). The RMSD between \((\text{ET}_{\text{Sim}})_{\text{TA}}\) and \((\text{ET}_{\text{Sim}})_{\text{h}}\) was 3 W m\(^{-2}\), the relative error was 19% and the slope was 0.88, as compared to 52 W m\(^{-2}\), 27% and 0.82, respectively when using a constant EF. These results corroborated with those established by Hoedjes et al. (2008) and Chehbouni et al. (2008a). Additionally, by properly taking into account the effect of the grid heterogeneity due to both vegetation and soil moisture variations along the grid and the error associated to the application of the aggregation rules, the agreement between \((\text{ET}_{\text{Sim}})_{\text{TA}}\) and \((\text{ET}_{\text{LAS}})\) is considered to be acceptable.

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To further assess the performance of the developed combination of temporal and spatial aggregation methods, a second dataset collected in northern Mexico (Chehbouni et al., 2008a, in press) was used. The grid consisted of three adjacent fields: cotton, chickpea and wheat. The three fields with eddy covariance flux towers are shown in Fig. 11. Both studies used the same data. Here, we briefly recall the objectives of these studies. In Chehbouni et al. (2008a), the temporal aggregation scheme for deriving diurnal course of \( \overline{ET_{sim}}/TA \) was tested with success over the three fields by comparing the \( \overline{ET_{sim}}/TA \) retrievals to those measured by the eddy covariance systems. This was achieved by using the same temporal aggregation scheme used in this study (Eqs. (19)–(25)). The study of Chehbouni et al. (in press) aimed to assess the potential and the limitations of the LAS in inferring \( H_{LAS} \) and latent \( (\overline{ET_{LAS}}) \) fluxes over the three fields by comparing the LAS fluxes to those measured by the eddy covariance systems.

Fig. 12 presents the comparison of \( \overline{ET_{sim}}/TA \) (derived in Chehbouni et al. (2008a)) with \( \overline{ET_{LAS}} \) (derived in Chehbouni et al., in press). The statistical results of this comparison showed that the RMSE was about 48 \( W \, m^{-2} \) and the correlation coefficient and the slope associated with the linear regression forced to the origin were 0.90 and 0.65, respectively. Comparing these results with those obtained in the current study, it can be concluded that the proposed approach can be used with success in different environmental conditions. The results are an important step toward developing the remote sensing algorithms for better estimation of the evapotranspiration on a large scale relying on the use of the scintillometry. Additional investigation using data collected over a range of surface type combinations are required to generalize and confirm our findings, and more importantly, future research should be directed towards building robust relationships between model and observational variables directly at the grid-scale.

5. Conclusions

Comparisons of grid-scale evapotranspiration derived from the scintillometer with those estimated from the spatial and temporal aggregation schemes, under different environmental conditions (sparseness of vegetation and heterogeneity in terms of soil moisture pattern induced by the “flood irrigation” method), showed an acceptable result using data collected in the central of Morocco. Additionally, the temporal aggregation scheme has been tested with success over a heterogeneous grid in a semi-arid region in northern Mexico. This finding confirms and generalizes the consistency of the aggregation schemes for accurate estimates of the evapotranspiration over heterogeneous grids. However, it is worth noting that the aggregation algorithms presented here have some limitations. The method to establish relationships between the local and effective surface parameters is purely of a semi-empirical nature which is not universal. Additionally this method uses local measurements of surface temperature; albedo and solar radiation which were assumed to be representative of the individual site. This assumption can certainly lead to some errors since the heterogeneity is also encountered at the field or patch scale. Future research should be thus directed towards building robust physical relationships between the local and effective surface parameters as well as testing it using remotely sensed data, which provide spatial distribution of surface temperature, albedo and solar radiation.

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Appendix A

A.1. Surface fluxes using scintillometry

The LAS is a device that provides measurements of the variation in the refractive index of air caused by atmospheric turbulence. This instrument consists of a transmitter and a receiver, both with an aperture diameter of 0.15 m, set up at a separation distance (or path length) ranging from 250 to 5000 m. The transmitter emits electromagnetic radiation, which is scattered by the turbulent atmosphere, and the resulting variations in signal intensity (scintillations) are recorded by a receiver comprising an identical mirror and a photodiode detector. The intensity fluctuations are related to the path average structure parameter of the refractive index of air, \( C_n^2 \). The scintillations are primarily the result of fluctuations in air temperature and humidity. Strictly speaking, the measured \( C_n^2 \) is related to the structure parameters of temperature \( C_T^2 \), of humidity \( C_r^2 \), and the covariant term \( C_{rT} \). For electromagnetic waves in the visible and near-infrared region, however, humidity related scintillations are much smaller than temperature related scintillations. Wesely (1976), and more recently Moene (2003), have shown that for a LAS operating at a near-infrared wavelength, we can derive the structure parameter of temperature \( C_T^2 \), from \( C_r^2 \), using:

\[
C_T^2 = C_r^2 \left( \frac{T^2}{0.78 \times 10^{-3} p} \right) \left( 1 + 0.03 \beta \right)^{-2}
\]  

(A.1)

where \( T_a \) is the air temperature (K), \( p \) is atmospheric pressure (Pa) and \( \beta \) is the Bowen ratio. The factor involving the Bowen ratio is the correction term for the influence of humidity fluctuations.

Using Monin–Obukhov Similarity Theory (MOST), the sensible heat flux \( (H_{LAS}) \) can be obtained from \( C_T^2 \) and additional wind speed data through the following dimensionless relationship:

\[
C_T^2 \left( \frac{z_{LAS} - d}{T^2} \right)^{2/3} = f \left( \frac{z_{LAS} - d}{L} \right) = C_{t1} \left( 1 - C_{t2} \left( \frac{z_{LAS} - d}{L} \right)^{-2/3} \right)
\]  

(A.2)

where \( L \) is the Obukhov length (m) \( \left( L = 0.4 \rho C_p T_a \overline{u^3}/\overline{H_{LAS}} \right) \), and \( T_a \) is the temperature scale \( \left( T_a = \frac{H_{LAS}}{H_{KL}} \right) \). The friction velocity \( (\overline{u}_*) \) is...
expressed as:

\[ u = ku \ln \left( \frac{z_{AS} - d}{z_0} \right) - \psi \left( \frac{z_{AS} - d}{L} \right)^{-1} \]  
(A.3)

where \( z_{AS} \) is the effective height of the LAS above the surface, \( \psi \) is the integrated stability function (Panofsky and Dutton, 1984), \( d \) is the displacement height and \( z_0 \) is the roughness length, \( k \) is the von Karman constant, \( \gamma \) is the gravitational acceleration, \( \rho \) is the density of air and \( c_p \) is the specific heat of air at constant pressure. Here, \( d \) and \( z_0 \) were calculated as a function of the vegetation height (Ezzahar et al., 2007a,b). During the iteration procedure, the Bowen ratio is evaluated using the \( H_{LAS} \), measured net radiation \( (R_n) \) and measured soil heat flux \( (G) \). In this study we will confine ourselves to unstable conditions and will use the MOST relationship \( f_r \) in Eq. (2) given by De Bruin et al. (1993).

Finally, the ET from the LAS can be derived by imposing the energy-balance closure assumption (Chehbouni et al., 2000b, in press; Ezzahar et al., 2007b, 2009; Hemakumara et al., 2003; Hoedjes et al., 2002).

References
