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Automatic unmixing of MODIS multi-temporal data for inter-annual monitoring of land use at regional scale (Tensift, Morocco)

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Abstract. The objective of this study is to develop an approach for monitoring the land use over the semi-arid Tensift-Marrakech plain, a 3000 km² intensively cropped area in Morocco. In this objective, the linear unmixing method is adapted to process a 6-year archive of MODIS NDVI 16-day composite data at 250 m spatial resolution. The result of the processing is a description of land use in term of fractions of three predominant classes: orchard, non-cultivated areas and annual crop. The typical signatures of land classes – endmembers – are retrieved on a yearly basis using an automated algorithm that detects the most pure pixels in the study area. The algorithm first extracts typical NDVI profiles as potential endmembers, then selects the profiles that have the best ability to reproduce the variability of MODIS NDVI time series.
within all the study area. The endmembers appear stable over the 6 years of study and
coherent with the vegetation seasonality of the three targeted land classes. Validation
data allows to quantify the error on land class fractions to about 0.1 at 1 km resolution.
Land use fraction maps are consistent in space and time: the orchard class is stable, and
differences in water availability (irrigation and rainfall) partly explain a part of the inter-
annual variations observed for the annual crop class. The advantages and drawbacks of
the approach are discussed in the conclusion.

Keywords: NDVI; land use; semi-arid; linear unmixing; endmembers; MODIS.

1. Introduction

Changes in Land Use and Land Cover (LULC) is a major issue in Environmental
Science, interconnected with many question concerning climate change, carbon cycle
and biodiversity (Aspinall and Justice 2003; Lepers et al. 2005). The monitoring of
LULC is also vital for managers and policy makers to make informed decisions
regarding the sustainability of agriculture and provision of safe drinking water,
especially in semi-arid areas. Remote sensing is very well-suited to achieve this
monitoring since it allows observations regularly distributed in space and time (Rogan

Multi-temporal images are widely investigated for mapping and monitoring land-cover
and land-use changes. At the present time, time series of images can be obtained at a
high spatial resolution by programming a series of SPOT or FORMOSAT-2
acquisitions. These images with both high spatial resolution (~10 m) and high temporal
repetitivity (a few days) offer strong opportunities to monitor land surfaces over small
areas: 25x25 km² for FORMOSAT-2, 60x60 km² for SPOT. However, constraints
related to acquisition, cost and processing often prevent the use of high spatial
resolution data. Multi-temporal data acquired by low or moderate spatial resolution
sensors such as NOAA-AVHRR, SPOT- VEGETATION or TERRA-MODIS are thus
preferred for regional and continental studies (e.g. Lambin and Ehrlich 1997, Hansen et
al. 2000; Lunetta et al. 2006, Matsuoka et al. 2007; Stibig et al. 2007). Indeed, they
offer a costless global coverage of the Earth on a daily basis. However, the spatial
resolution of large field of views sensors – from 250m for MODIS to 1 km for
VEGETATION and AVHRR – is generally much higher than the size of homogeneous
areas (units) at the Earth surfaces. These sensors generally provide images with pixels
that include a mixture of different units (mixed pixels). Consequently, the use of low
spatial resolution data for a directly monitoring of LULC is not straightforward.
Furthermore, conventional classification approaches based on signature clustering (like
maximum likelihood, Richards 1999) are not suitable since they aim to identify an
unique class for each pixel.

For these reasons, the linear unmixing model has been developed (Adams et al. 1986,
Smith et al. 1990, Elmore et al. 2000) based on the following assumption: the signature
of a mixed pixel results from a linear combination of the distinctive signatures
(endmembers) that are representative of the various land surfaces included in the study
area. These typical signatures must describe as well as possible a pure component
having meaningful features for an observer (Strahler et al. 1986). Knowing these
signatures is a prerequisite for applying the linear unmixing model (Cross et al. 1991, Quarmby et al. 1992, Foody and Cox 1994, Milton and Emery 1995). Unmixing approaches can be divided into two categories depending on how the endmembers are estimated:

- Supervised approaches use the spectral signatures of endmembers as *a priori* information. These typical spectra can be collected at field or laboratory to define predefined library endmembers (Adams et al. 1995, Roberts et al. 1998, Smith et al. 1990). They can also be derived from high spatial images using a training data set (small region where the land use is known). The use of predefined libraries may be not appropriate since differences in the acquisition conditions (e.g. sun-target-sensor geometry, atmospheric effects) may occur between endmembers and the data to be unmixed (Song and Woodcock 2003).

- In unsupervised approaches (see Plaza et al. 2004 for a review), the identification of endmembers is automated. The common point in unsupervised algorithms is that they search endmembers directly from images (Atkinson et al. 1997, Elmore et al. 2000, Ridd 1995, Wessman et al. 1997). In this case, the endmembers are retrieved at the same scale and conditions than the data to be unmixed.

The temporal variability of the observations is generally not considered in the above-mentioned studies, though it is also an important source of information. In particular, the time courses of vegetation indices such as the Normalized Difference Vegetation Index NDVI allow to monitor the phenology of vegetation (Gutman and Ignatov 1995, Justice et al. 1998, Duchemin et al. 1999). This may be very useful for discriminating
land classes. Differences in phenology depicted by vegetation indices can be used to map land surfaces using low spatial resolution data (e.g. Kerdiles and Grondona 1995, Cardot and Faivre 2003, Ballantine et al. 2005, Knight et al. 2006). These studies showed that: 1) land use maps are more accurate when vegetation indices are used instead of reflectances; 2) the use of NDVI with a linear approximation for its combination results in minor inaccuracies; 3) linear unmixing provides satisfactory results when the number of endmembers is limited. These considerations, which are of prime importance in unmixing procedure, are accounted for in this study.

In this context, the primary objective of this study is to evaluate the potential of MODIS data for monitoring the land use on the semi-arid Tensift/Marrakech plain. A secondary objective is to analyse the space-time variability of land classes in relation with water availability. The methodology is based on the unmixing of MODIS multi-temporal NDVI images. Land use maps are evaluated using ground data and high spatial resolution images, and their space-time variability is analysed together with information on irrigation water.

2. Research Design

The methodology is an unsupervised unmixing approach based on a statistical analysis for identifying endmembers directly from MODIS multi-temporal images at 250 spatial resolution (MOD13Q1 product, i.e. 16-day NDVI composite images by CV-MVC
algorithm, Huete et al. 2002). The algorithm first extracts typical NDVI profiles, then
selects the endmembers amongst these profiles based on their ability to reproduce the
space time variability of MODIS NDVI time series. The approach requires the two
following assumptions: (1) pure pixels can be identified at the 250m resolution and
(2) endmembers are stationary over the Tensift-Marrakech plain.

The approach is set up to retrieve the fractions (surface covered by homogeneous units
within each pixel) of three classes: orchard, non-cultivated areas and annual crop. These
classes are predominant in the study area, they display distinct phenological features
and they encompass the range of crop water needs: non-cultivated areas (no needs),
annual crops (water needs ~ 400 mm/y) and orchards (water needs ~ 1000 mm/y).

The algorithm is applied to a six-year archive of MODIS NDVI to obtain maps of land
use fractions on a yearly basis, from agricultural season 2000-2001 to 2005-2006. The
algorithm is applied on two different areas, the whole study area and a subpart of the
study area where the landscape is rather regular and where more data are available for
evaluation. The processing results in 12 land use maps (6 years x 2 training areas) in
term of the fractions of the three predominant classes (orchard, non-cultivated areas and
annual crop).

MODIS estimates are quantitatively evaluated against ground truth collected on a 9 km²
area and a reference land use map derived from a time series of high spatial resolution
images (SPOT and Landsat). These data were collected during the 2002-2003
agricultural season. The evaluation is based on classical statistical variables (correlation
R², efficiency EFF, RMSE and bias) computed between land use fractions estimated with MODIS and derived from the validation data sets at 1 km resolution. In order to test the robustness of the algorithm, the performance of the algorithm is also discussed from the results obtained with the whole MODIS data set (2000-2006 period). Here we analyse the inter-annual variability of both endmembers and land use maps using rainfall and irrigation data as an indicator of water availability and vegetation growth.

3. Materials and Methods

In this section, we present the study area, the ground and satellite data, and the linear unmixing algorithm.

3.1. Study area and ground data

The study area is the eastern part of the semi-arid Tensift plain, a 3000 km² region located in center of Morocco (figure 1). The climate of this region is arid, with annual rainfall around 250 mm/year and a very high evaporative demand around 1500 mm/year (Duchemin et al. 2006, Chehbouni et al. 2007).

According to the regional public agency in charge of agricultural water management (ORMVAH), there are three dominant land classes that represent more than 80% of land surfaces: (1) orchards, most of it perennial (olive and citrus trees); (2) cereal crops, mainly wheat, to less extent barley; (3) non-cultivated areas. Additional land classes
include forages (mainly alfalfa, colza and oat), vineyards, broad-leave orchards (apple, apricot and peach trees), and small vegetable crops.

[Insert Figure 1 about here]

The High-Atlas mountain range experiences much higher precipitations and provides irrigation water to the plain (Chaponniere et al. 2005, Chehbouni et al. 2007). There are three types of irrigation systems: the modern network connected with dams, the traditional network, and pumping stations (Duchemin et al. 2007). The main irrigated areas are supplied by dam water and managed by ORMVAH. They cover about 1200 km² with three distinct sub-regions (figure 1):

• The western NFIS sub-region, mainly cropped with orchards on fields of irregular size (~ 100 m² to ~ 10 ha);
• The central Haouz sub-region, mostly cropped with cereals, where the landscape appears rather uniform with relatively larger fields (3-4 ha);
• The eastern Tessaout sub-region, very patchy with a mixture of various annual crops and orchards cultivated on very small fields (100 to 1000 m²).

In order to evaluate land use maps, we use two sets of ground data collected during the 2002-2003 agricultural season. The first one is composed of 151 individual fields spread over the study area divided as following: 11 plots of orchard on bare soil, 80 plots of orchard on annual crop, 28 plots of non-cultivated areas and 32 plots of annual crop (see Simonneaux et al. 2007). The second one exhaustively covers a 3 x 3 km² area within the Haouz sub-region during the 2002-2003 agricultural season (see Duchemin et al.
2006). It is composed of 313 plots divided as following: 5 plots of orchard, 67 plots of non-cultivated areas and 241 plots of cereal crops (wheat and barley).

In order to study the space-time variability of land classes, we analyse data on dam irrigation water and precipitations. ORMVAH collects the annual amount of dam irrigation water supplied to the three sub-regions. As it is difficult to exactly know when and where irrigation occurs, we assume a uniform distribution: the amount of dam irrigation water is divided by the total area of each sub-region to provide average values in mm. Precipitations are collected from a network made of about 20 raingauges stations spread over the plain. There is a large seasonal variability of rainfall, both in terms of annual quantity and of seasonal distribution: accumulated values of 140 mm for the driest years (2000-2001 and 2004-2005) against 300 mm for the most humid years (2003-2004 and 2005-2006); early rainfall in 2003-2004 or delayed rainfall in 2001-2002.

3.2 Satellite data

High spatial resolution data are used to produce a reference land use map in order to evaluate classification maps obtained with MODIS data. We use a SPOT5 panchromatic image at 2.5m resolution acquired the 23/07/2002 and 10 cloud-free Landsat/ETM7+ and SPOT4/5 images acquired during the 2002-2003 agricultural season. The Landsat/SPOT images were collected between 07/11/2002 and 20/06/2003 with a revisit time of approximately three weeks. These images were geometrically corrected using GPS ground control points and resampled to 30m. The radiometric
processing (calibration and atmospheric correction) was performed using reflectance values recorded at field (Duchemin *et al.* 2006, Simonneaux *et al.* 2007).

Terra-MODIS data are freely available from the NASA website ([http://delenn.gsfc.nasa.gov/](http://delenn.gsfc.nasa.gov/)). We have downloaded 16-day composite images (MOD13Q1 product) from the 2000-2001 to the 2005-2006 agricultural seasons. These images contain atmospherically corrected reflectances and NDVI at 250m spatial resolution based on the Constrained View Maximum Value Composite algorithm (Huete *et al.* 2002). They were resampled at 270m (9x30m) spatial resolution using the cubic convolution technique, then subset to the Tensift-Marrakech plain. They were stacked into 6 multi-temporal NDVI images (from September 2000 to August 2001, September 2001 to August 2002 etc). A total of 141 images were processed and visually examined in order to detect eventual anomalies. Most of images are of good quality excepted three images (18/02/2001, 23/04/2001 and 01/01/2003) that were eliminated because they display geometric problems. All images are free of clouds. This is expected since the time step of compositing is rather long (16 days) and the cloudiness is low in the study area, around 30% (Hadria *et al.* 2006).

### 3.3. Reference land use map (2002-2003 season)

The reference land use map is derived from high spatial resolution data on the common area between the Landsat images, the SPOT ones and the study area (about 1500 km², see figure 2). The classification identifies the three predominant land classes using a two-step procedure:
1) The orchards are depicted on the 2.5m panchromatic SPOT image using the 
“Olicount” software (Simon et al. 1998). The software operates with a set of input 
parameters that essentially define the morphology of trees (shape) and their 
radiometry (gray level). This first class groups all the areas where trees are detected, 
including case of intercropping (trees + wheat or trees + alfalfa) and the natural 
vegetation that may also grow between the trees or in the understory.

2) To discriminate the two remaining classes, NDVI maximum values are calculated 
from NDVI profiles derived from time series of SPOT and Landsat images. Pixels 
with a maximum NDVI below 0.4, which contain sparse vegetation, are assigned to 
the class bare soil. The remaining pixels are supposed to include irrigated areas and 
are assigned to the class annual crop. The threshold value (0.4) was calibrated to 
obtain a maximal global accuracy of the classification.

This processing leads to the partition of the area into three classes with about 20% of 
orchard, 50% of bare soil and 30% of annual crop. The land use map (figure 2) shows 
that: the bare soil class is predominant outside irrigated areas in western and southern 
parts of the region; the annual crop class is mainly depicted at the eastern part of the 
study area within Haouz and Tessaout irrigated sub-regions as well as downstream 
High-Atlas wadis; orchards are spread over the plain, with the maximal density in the 
western NFIS irrigated sub-region.
The reference land use map is evaluated against the ground truth collected on individual fields (see §3.1). According to the confusion matrix (table 1), the overall accuracy, i.e. the number of well-classified pixels divided by the total number of pixels, is around 78%, with very low omission errors for the class orchard on bare soil (about 10%) and for the class annual crop (about 3%). Two types of confusion are detected: 1) between annual crop and orchard on annual understory, and 2) between bare soil and annual crop. The causes of these confusions were discussed in Simonneau et al. (2007) and Benhadj et al. (2007). They are related to the disparities that exist for a same land class, which causes overlapping of signatures between the three land classes. For cereals, there is a large heterogeneity in cereal crop calendar as well as irrigation and fertilisation schedules. Non irrigated areas may include a wide range of vegetation type (colza, oat, grass). Finally, there are large variations of density and age in tree plantations, which may include an understory of vegetation cultivated as forage (wheat, grass, alfalfa…).

The reference land use map is used for evaluating MODIS estimates for the 2002-2003 agricultural season at 1 km² scale. For this purpose, a co-registration between MODIS data and the reference land use map is done using an automatic correlation algorithm (Benhadj et al. 2006). Then the reference map is up-scaled at 1 km resolution by spatial averaging to obtain the fractions covered by orchards, bare soils and annual crops.

### 3.4 Linear unmixing of MODIS data
To predict the land use fractions of the three dominant land classes, the linear unmixing model is applied to MODIS multi-temporal NDVI images. The model calculates the NDVI of a mixed pixel as the sum of the NDVI values of the different land classes weighted by their corresponding fraction within the pixel (equation 1). We retrieve the typical NDVI time course of each land class (endmember) using the three-step procedure which is detailed below.

\[
NDVI_i(t) = \sum_{j=1}^{3} \pi_{ij} \times NDVI_j(t) + \varepsilon_i(t)
\]

(1)

where \( NDVI_i \) is the NDVI of MODIS mixed pixel \( i \) at the date \( t \), \( \pi_{ij} \) is the fraction of class \( j \) in pixel \( i \), \( NDVI_j \) is the endmember of class \( j \) (\( j = 1 \) to 3) and \( \varepsilon_i \) is an error term of the pixel \( i \).

Step 1. An unsupervised classification “k-means” (Tou and Gonzalez 1974) is applied to MODIS multi-temporal images in order to group the pixels which have similar NDVI seasonal courses. The result is \( N \) mean NDVI profiles corresponding to \( N \) groups of pixels. We set \( N \) to 20, which appears as a good compromise allowing a reasonable computing time cost while keeping a sufficient level of details to describe the NDVI space-time variability within the study area. Furthermore, the grouping of pixels with the same vegetation seasonality allows the reduction of local noise due to: (1) imperfect superimposition of MODIS data before temporal compositing, (2) inaccuracy in

\(^1\) The term ‘groups’ is used to refer the classes identified by the K-means method in order to avoid confusion with those derived from MODIS data after unmixing.
Step 2. An iterative test is applied for all possible triplets of endmembers (three land classes) among the series of $N$ mean NDVI profiles. The total number of iteration $nb$ is $C_N^3$. For each triplet, the land use fractions are retrieved for the remaining 17 (i.e. N-3) groups by minimizing the Root Mean Square Error (RMSE, equation 2) between the NDVI profiles observed by MODIS and those reconstructed from the endmembers.

$$\text{RMSE}_i = \sqrt{\frac{1}{T} \times \sum_{t=1}^{T} [e_i(t)]^2}$$

(2)

With $\pi_{ij} \geq 0$ and $\sum_{j=1}^{3} \pi_{ij} = 1$

Where $T$ represents the number of MODIS data

Step 3. We calculate an error term ($M_k$, equation 3), which represents the ability of the triplet number $k$ to explain the NDVI response for the 17 groups. Finally, the triplets are sorted according to this error term: the triplet for which $M_k$ is minimal is called triplet rank 1, the following is called triplet rank 2, etc.

$$M_k = \frac{1}{\sqrt{[(N-3) \times T] \times \sum_{i=1}^{N-3} \sum_{t=1}^{T} [e_i(t)]^2}}$$

(3)

With $k \in [1, nb]$ and $nb = C_N^3 = \frac{N!}{3!(N-3)!}$
Once the endmembers are identified, they are assigned to the appropriate land use class and the surface covered by a class within a pixel (land use fraction) is retrieved by minimization (equation 2). This is applied pixel by pixel using land use fractions ranging from 0 to 1 and under the constraint that the sum of fractions is equal to 1.

We apply the algorithm using two different areas for the identification of endmembers. The first one is the whole study area (figure 1). The second one is the reference area (figure 2) on which the reference land use map is available (§3.3). In both case, the land use fractions maps are analysed at the scale of the whole area. MODIS estimates are evaluated against the reference land use map (see §3.3) and against the ground truth collected on the 3 x 3 km² area (see §3.1). In order to explain the difference between annual crop endmembers between the two investigated areas, we carry out a purity analysis. The pixels of each group resulting from the k-means classification are located in the reference land use map (figure 2) and their compositions are averaged.

4. Results and discussion

In this section, we successively present: a quantitative evaluation of the results obtained during the 2002-2003 agricultural season; a generalised analysis of inter-annual coherence and variability of the results through the 2000-2006 period; an error analysis with typical cases for which the results are not satisfactory.

4.1 Typical NDVI time series and endmembers (2002-2003 agricultural season)
The NDVI profiles of the 20 groups identified with K-means classification over the two areas of interest (whole and reference areas) can be discriminated through the combination of NDVI seasonal amplitude and average value (figure 3). It appears that the K-means method groups pixels according to the density of perennial vegetation (hierarchy of rather stable NDVI profiles with average values from 0.15 to 0.55) and according to the vegetation seasonality (contrast between high NDVI values during the agricultural season and low values in summer).

When looking at the endmembers (figure 3), it is noticeable that the algorithm tends to select the profiles that display extreme values and rejects intermediates ones. Furthermore, the endmembers appear descriptive of the three dominant classes: the first one, with maximum NDVI values below 0.2, corresponds to the bare soil class; the second one, with NDVI always high (between 0.45 and 0.65), appears representative of a dense perennial vegetation (orchard class); the third one, with a large NDVI amplitude, can be associated to the class annual crop. The latter displays minimum values in November (at the sowing period), then a rapid increase to maximum values mid-March when cereal reaches full development, and a final decrease until June after total senescence of plants. This analysis makes easy to label each endmember.

The case of annual crop is of particular interest since the endmembers are not the same for the two investigated areas (figure 3). In particular, there is a difference in the NDVI value at the beginning (September to November 2002, before day 90) and ending of the
season (June to August 2003, after day 280). The level is around 0.25 for the endmember extracted on the whole area, while it is only 0.18 for the endmember extracted on the reference area. This last endmember appears to be more characteristics of annual crop, for which minimal NDVI values are close to those of bare soil (~0.15) out of the agricultural season.

In order to explain the difference between annual crop endmembers, their purity are analysed (table2). The endmembers display a high proportion of either bare soil or annual crop or orchard for the two areas comparing to the remaining 17 NDVI profiles non selected as endmembers. One exception is detected for the class annual crop when the whole area is considered (72% of annual crop in group 3 that is selected as endmember against 88% in group 20, see the main left column of table 2). The difference of endmembers purity between the two areas is small for the bare soil and orchards classes, but large for annual crop (purity of 88% for the reference area against 72% for the whole area, compare group 3 in the two main columns of table 2). This difference is due to significant presence of orchard in the annual crop endmember derived over the whole area (~27%, against ~9% for the reference area). When the whole area is used, the automatic extraction algorithm selects groups that include pixels of the Tessaout sub-region, where there is a mixture of olive orchards and annual crops cultivated on very small fields. In contrast, when the identification of endmembers is restricted to the reference area, the algorithm selects pixels in the irrigated Haouz sub-region where fields are mainly cropped with cereals and of larger size. Therefore, this analysis demonstrates that: (1) our working hypothesis, i.e. pure pixels may exist at the spatial resolution of 250m, is valid; (2) the automatic extraction algorithm is able to
identify the most pure areas; (3) there is an advantage to derive the endmembers on the
reference area compared to the whole area.

[Insert table 2 about here]

4.2 Quantitative evaluation of land use map (2002-2003 agricultural season)

The comparison of land use fractions estimated with MODIS and the reference land use
map (figure 4) shows the consistency of areas with low and high fractions between the
two maps. This is true for the three land classes: high proportion of bare soil at South-
West; high proportion of annual crop near High-Atlas foothills and on the Haouz and
Tessaout irrigated areas in the eastern part; high proportion of orchard near the Tensift
river at North and within the NFIS irrigated area at West. Average land use fractions
derived from reference and estimated maps display an overall agreement (table 3),
which denotes the global ability of the algorithm to describe the study area using three
dominant land classes. However, the algorithm slightly underestimates the orchard and
the annual crop fractions at the benefit of bare soil fractions when the whole area is
considered. This underestimation is attenuated when the reference area is used to derive
the endmembers.

[Insert Figure 4 about here]

[Insert Table 3 about here]
The quantitative comparison of MODIS and the reference land use map (table 4 and figure 5) shows that the two land use fractions always well correlate (R² around 0.8 with a minimal value of 0.68), and the efficiency is generally largely positive (>0.65). When the reference area is used to derive the endmembers, the method gives more accurate estimates of bare soil and orchard fractions (lower RMSE and bias, larger efficiency). For both areas, the estimates of orchard fractions appear less accurate than for the two other classes (efficiency of 0.65-0.7 instead of 0.80). This is likely due to the fact that the orchard class is rather heterogeneous because trees are of different nature, age and spacing, with possible case of inter-cropping. In contrast, the endmember associated to this class is representative of dense perennial vegetation (mainly old olive and citrus tree with low spacing between crown). Despite this limitation, we consider that land use fractions are correctly estimated, though the study area is only described by three typical NDVI profiles.

Finally, the comparison of MODIS land use fractions and the ground truth available over the 9 km² area shows a global agreement of land use fractions for all classes (figure 6), with few orchards (less than 2% of the 9 km², see table 5). For the two others classes, we obtain accurate results, with R² larger than 0.85 and RMSE lower than 0.1. The accuracy of estimates is improved when the endmembers are derived on the reference area (RMSE of 0.07 against 0.09 in figure 6).
All the results presented in this section, obtained for the 2002-2003 agricultural season, confirm the capacity of the linear unmixing model to describe the land use of the study area on the basis of three NDVI profiles associated to the predominant classes (orchard, annual crop, bare soil) and automatically extracted from MODIS multi-temporal images.

4.3 Generalised analysis of endmembers (2000-2006 period)

The algorithm is applied to the 2000-2006 period using successively each MODIS multi-temporal NDVI images. The endmembers expected for the orchard and the bare soil classes are always selected (figure 7a and 7b, respectively), the first ones with rather high NDVI values (>0.4) and low seasonal amplitudes (~0.2), the second ones with the lowest values (six-year maximum of 0.22).

For the bare soil and orchard classes, there is a general stability of the endmembers from one year to the other (figure 7). In contrast, the NDVI profiles with the highest amplitudes (annual crop endmembers, figure 8) display a higher variability. When the
whole area is used to retrieve the endmembers, the NDVI profiles display rather high value (>0.23) at the beginning and the end of the agricultural season for all years except 2005-2006 (figure 8-top). A detailed investigation of the groups of pixels resulting from the k-mean classification shows that the annual crop endmember mainly include pixels of the Tessaout region for the first 5 years (2000-2005), while it includes those of the Haouz region for the last year (2005-2006). The selection of pixels in the Tessaout region results in a significant proportion of trees included in the annual crop class, as discussed in section §4.1 for the 2002-2003 season. This problem disappears when the endmembers are extracted on the reference area. In this case (figure 8-bottom), the seasonality of the annual crop endmember is generally consistent with the phenology of cereal crops (growing season from December to April, and NDVI values below 0.2 outside), but two exceptions can be noticed:

- For the 2001-2002 season, the increase of NDVI is delayed and largely reduced (peak of NDVI around 0.4 after April, figure 8-bottom-left). This year is characterised by a shortage in irrigation water after the severe drought that occurs during the 1999-2001 period. In this case, the NDVI pattern matches the 2001-2002 seasonal distribution of rainfall, with most of precipitations recorded in March and April. Therefore, the 2001-2002 annual crop endmember appears not suitable for the retrieval of annual crop fractions. The analysis of other NDVI profiles for this year shows that no profile is representative of the phenology of cereal crop. As an alternative, we replace the 2001-2002 annual crop endmember by the average NDVI profile of the endmember identified on the four ‘normal’ years (2000-2001, 2002-2003, 2004-2005 and 2005-2006).

- For the 2003-2004 season, the NDVI display an early NDVI from 0.2 to 0.4 between November and December (“03-04 (rank 1)” profile in figure-bottom-right).
This pattern also appears coherent with the seasonal distribution of rainfall. Heavy rainfall at the very beginning of the season resulted in an early sowing or growth of natural vegetation. Here the analysis of other NDVI profiles allows to identify a substitute to represent the phenology of cereal crops. This endmember (“03-04 (rank 2)” profile in figure 8-bottom-right) is similar to the ones observed for the ‘normal’ years, and results in a low unmixing error (second rank in the minimisation process).

[insert Figure 8 about here]

4.4 Spatio-temporal variability of land use maps (2000-2006 period)

A visual examination of land use fractions maps (figure 9) shows that the algorithm always detects the same region with low or high proportion of each class. Orchard fractions appear especially stable during the six years, in coherence with the duration of tree plantations. On the contrary, there are some compensations in the fractions of the two other classes (bare soil and annual crop). In particular, there is a high proportion of bare soil and a low proportion of annual crop for the 2001-2002 agricultural season compared to others. These compensations are analysed on what follows.

[Insert Figure 9 about here]

Land use statistics are calculated for the six years of study by averaging fractions over each of the three irrigated sub-regions (table 6). One can see that the proportion of orchard is quite stable, around 37% for NFIS, 18% for Haouz and 32% for Tessaout.
These values appear coherent with the qualitative knowledge of the study area (§3.1). Except for the 2001-2002 season, bare soil fractions are rather stable, between 50 and 56% for the NFIS sub-region, 35 and 46% for the Haouz and between 16 and 21% for the Tessaout. The variation of annual crop fractions around its average value is of the same order. The 2001-2002 season is very particular with an important reduction of annual crop fractions, by a factor 2.5 within NFIS (4% in 2001-2002 against 10% the other years) and Tessaout (20% against 45-50%) and a factor 5 within Haouz (8% against 40%).

The anomaly detected in annual crop fractions for the 2001-2002 agricultural season appears as an indicator of the water shortage experienced this year. We illustrate this for the Haouz sub-region, where the anomaly is of maximal amplitude (figure 10). The limitation of irrigation water during the driest year (annual average of 30 mm in 2001-2002 instead of 130 mm for the other years) results in a large decrease of annual crop fractions (by about 30%) and a large increase of non-cultivated areas (by about 30%). The orchard fractions appear stable despite the shortage of irrigation water, consistent with the fact that orchards are irrigated in priority.

4.5 Error and limitation analysis
In order to identify the limitations of the approach, we calculate the relative error (RRMSE, equation 4) between MODIS observations (\( NDVI(t)_{obs} \)) and the NDVI reconstructed from the linear combination of the endmembers associated to their land use fractions (\( NDVI(t)_{sim} \)). This criteria allows us to quantify the ability of the three endmembers to reproduce MODIS NDVI space-time patterns over the study area. Maps of RRMSE are computed for each season and averaged over the six seasons (figure 11).

\[
RRMSE = \sqrt{\frac{1}{T} \sum_{t=1}^{T} (NDVI(t)_{obs} - NDVI(t)_{sim})^2} \times 100 \tag{4}
\]

It can be seen that the MODIS NDVI time courses are generally well reproduced (figure 11). The histogram associated to the spatial variation of RRMSE displays a peak centred around a value of 10%, with 90% of pixels have a value of RRMSE lower to 20%. This confirms the efficiency of the algorithm to recover NDVI space time variations, but some anomalous pixels display high errors (RRMSE>40%). These pixels are mainly located in the NFIS irrigated sub-region at the western part of the study area. There are two main cases where the capacity of the algorithm to fit MODIS observations is low:

- In case 1, the NDVI time course displays two peaks at the middle (January) and at the end (April) of the agricultural season; this indicates successive cropping of vegetables with a short growing period;
In case 2, the NDVI time course displays an inverse pattern than the one of annual crop, with a large growing period between April and January; such pattern is consistent with the phenology of deciduous tree crops (apricot, apple, peach trees) and vineyards.

The two previous confusions concern a small part of the study area (0.2% with RRMSE>40%). Further investigations would be necessary to analyse the performance of the algorithm using more endmembers and more NDVI profiles as an input of the minimisation procedure (N>20 in equation 3). However, this may result in larger computation time and additional compensations/overlaps between land use classes.

5. Conclusion

In this study, we investigate the potential of time series of MODIS data (MOD13Q1 product, i.e. 16-day NDVI composite images by CVMVC algorithm, Huete et al. 2002) to monitor the land-use of the Tensift plain, a semi-arid region located in the surrounding of the Marrakech city. MODIS data offers a costless coverage of the Earth with a high temporal resolution, but its spatial resolution (250m) is large compared to the average field size in the study site. Thus, we develop an approach based on the linear unmixing of multi-temporal MODIS data. In this approach, the identification of endmembers - key point in linear unmixing - is performed on an annual basis following a two-step procedure: 1) pixels are grouped according to the vegetation seasonality; (2) the set of groups that displays the best ability to explain all NDVI time courses are automatically extracted using a statistical analysis. Some advantages can be mentioned here. Firstly, there is no need of extra information such as a training set where the land use is known. Secondly, there are no substantial differences in the acquisition conditions.
between endmembers and the data that are unmixed. Thirdly, the regional conditions on which the vegetation growth (e.g. dry or humid year) are integrated to the endmembers.

This procedure provides a continuous description of the land use in term of fractions of three classes (orchard, annual crop, non-cultivated areas) and on an annual basis (September to August, i.e. the agricultural season). These three classes are the most important for agricultural water management because they are predominant and they corresponds to very different water needs. The use of these three broad categories also facilitate the analysis of the inter-annual variability of MODIS estimates of land use fractions as well as its evaluation against additional data sets (ground truth and high spatial resolution images).

The analysis of typical NDVI profiles firstly demonstrates that our working assumption, i.e. quite pure pixels exist at the spatial resolution of 250m, is valid. Secondly, the algorithm is able to identify the most pure areas associated to each of the three classes of interest. The NDVI profiles retained as endmembers match with phenological features of non-cultivated areas (flat profiles with low values on the bare soil class), dense perennial vegetation (flat profiles with rather high values on the orchard class) and cereals (largest NDVI seasonality on the annual crop class). Thirdly, the algorithm is robust since the endmembers generally slightly differ between years. The inter-annual stability of endmembers is particularly true for orchards and bare soils, while the endmembers associated to the annual crop class display a larger inter-annual variability, in relation with changes in water availability (dam irrigation water, seasonal amount and distribution of rainfall).
Maps of land use fractions are in coherence with the qualitative knowledge of the study area, in particular for the three main irrigated sub-regions (NFIS, Haouz and Tessaout). Using both high spatial resolution data and ground truth, we quantify the error in land use fractions to around 0.1 at 1km spatial resolution (2002-2003 season). The analysis of land use maps derived for the six successive agricultural seasons (2000-2001 to 2005-2006) also confirms the performance of the approach. The orchard class is logically the most stable, with fractions around 37%, 18% and 32% for the NFIS, Haouz and Tessaout sub-regions, respectively. The compensations observed between the fractions of bare soil and annual crop show a high degree of space-time coherence with irrigation statistics. In particular, the algorithm retrieves a large reduction of annual crops after the severe drought that occurs at the beginning of the period of study. These results are promising in the perspective of the regional monitoring of water resources in the semi-arid Tensift/Marrakech plain.

Finally, the examination of some anomalous NDVI profiles, i.e. which are not well reproduced by the linear unmixing model, denotes the incapacity of the algorithm to describe the phenology of particular crop types (e.g. vineyards, vegetable crops). Inclusion of other land use components would provide additional information and possibly more accurate results. Further tests should be performed to identify the optimal number of both the endmembers and the groups of pixels used as endmembers potential candidates. In this perspective, the availability of time series of images with both high spatial resolution and high temporal repetitivity (e.g. FORMOSAT-2, GMES-Sentinel, RapidEye or Venµs) would offer additional opportunities.
Acknowledgements

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References


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FIGURE CAPTIONS

Figure 1. Delimitation of the whole study area (in red) and its three main irrigated sub-regions – NFIS (in yellow), Haouz (in black) and Tessaout (in cyan) – on a Landsat7 image. The white square represents the coverage of Landsat and SPOT4/5 images.

Figure 2. Land use map derived from high spatial resolution data on the reference area (2002-2003 season, 30m spatial resolution).

Figure 3. 2002-2003 NDVI profiles averaged over the 20 groups of pixels resulting from the k-means classification (gray lines) on the whole area (a) and on the reference area (b). Bold lines with symbols highlight the NDVI endmembers associated to orchard (■), bare soil (●), and annual crop (▼). The first day is September the 1\textsuperscript{st}, 2002.

Figure 4. 2002-2003 land use fraction maps derived on each class from the reference land use map (left) and from linear unmixing of MODIS data with the endmembers extracted on the whole area (middle) and on the reference area (right).

Figure 5. Estimated versus reference land use fractions (2002-2003 season, 1km spatial resolution): orchard (a), bare soil (b), annual crop (c). Estimates are provided by the linear unmixing model with the endmembers extracted on the whole area (1, at top) and on the reference area (2, at bottom). Black lines are X=Y lines; gray lines are regression lines.

Figure 6. Estimated versus observed land use fractions (3 km x 3 km R3 irrigated area, 2002-2003 season, 1km spatial resolution). Estimates are provided by the linear unmixing model with the endmembers extracted on the whole area (a) and on the reference area (b). Black lines are X=Y lines.

Figure 7. Estimated endmembers through the six-year period of study (2000-2001 to 2005-2006 agricultural seasons) on orchard (a) and bare soil (b) classes. The endmembers are extracted on the whole area (top figures) and on the reference area (bottom figures). On all X-axis, the first day is 1\textsuperscript{st} September.

Figure 8. Same as Figure 7 for the annual crop class: (a) 2000-2001 to 2002-2003 seasons, (b) 2003-2004 to 2005-2006 seasons. The endmembers are extracted on the whole area (top figures) and on the reference area (bottom figures). In figure a (bottom), the “4 year average” represents the average of the 2000-2001, 2002-2003, 2004-2005 and 2005-2006 annual crop endmembers. In figure b (bottom), “03-04 (rank1)” and “03-04 (rank2)” correspond to the endmembers linked to the 1\textsuperscript{st} and the 2\textsuperscript{nd} ranks in the minimisation procedure, respectively.

Figure 9. Maps of land use fractions derived from linear unmixing of MODIS data for the six years of study (2000-2001 to 2005-2006 agricultural seasons): orchard (left), bare soil (middle) and annual crop (right).
Figure 10. Estimated land use fractions averaged over Haouz irrigated sub-region for the six years of study (2000-2001 to 2005-2006 agricultural seasons), together with the annual average of irrigation.

Figure 11. Left: map of the relative root mean square error (RRMSE) maps, averaged for the six years of study. Right: histogram associated to the spatial variation of RRMSE.
Figure 2

- **Green**: Orchard
- **Brown**: Bare soil
- **Blue**: Annual crop

Legend:

- 0 km
- 2.5 km
- 5 km
- 10 km

North (N) is at the top of the map.
Figure 3

(a) (b)
Figure 4

- Orchard
- Bare soil
- Annual crop
Figure 5

(1)

(2)
Figure 6

(a) Y = 0.82X + 0.03
R² = 0.97

(b) Y = 0.95X + 0.01
R² = 0.9

Legend:

+ orchards  ● bare soil  ◇ annual crops
Figure 7

(a) (b)

NDVI vs Day

NDVI vs Day
Figure 8

(a) (b)
Table 1. Confusion matrix of the 2002-2003 reference land use map (in pixels)

<table>
<thead>
<tr>
<th>Field observations</th>
<th>Orchard on annual understory</th>
<th>Orchard on bare soil</th>
<th>Bare soil</th>
<th>Annual crop</th>
<th>total</th>
<th>Commission error (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Orchard</td>
<td>369</td>
<td>237</td>
<td>0</td>
<td>17</td>
<td>623</td>
<td>2.7</td>
</tr>
<tr>
<td>Bare soil</td>
<td>0</td>
<td>3</td>
<td>279</td>
<td>0</td>
<td>282</td>
<td>1.1</td>
</tr>
<tr>
<td>Annual crop</td>
<td>162</td>
<td>24</td>
<td>165</td>
<td>499</td>
<td>850</td>
<td>41.3</td>
</tr>
<tr>
<td>total</td>
<td>531</td>
<td>264</td>
<td>444</td>
<td>516</td>
<td>1755</td>
<td></td>
</tr>
<tr>
<td>Omission error (%)</td>
<td>30.5</td>
<td>10.2</td>
<td>37.2</td>
<td>3.3</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Overall Accuracy = 77.6%**
Table 2. Reference land use fractions (%) averaged over the 20 groups of pixels resulting from the k-means classification of 2002-2003 MODIS data; gray colors highlight the composition of the groups selected as endmembers; numbers in bold indicates the highest purity for each of the three classes of interest.

<table>
<thead>
<tr>
<th>Group</th>
<th>Whole area</th>
<th>Reference area</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Orchard</td>
<td>Bare soil</td>
</tr>
<tr>
<td>1</td>
<td>70</td>
<td>3.4</td>
</tr>
<tr>
<td>2</td>
<td>1.8</td>
<td>97.4</td>
</tr>
<tr>
<td>3</td>
<td>26.6</td>
<td>1.3</td>
</tr>
<tr>
<td>4</td>
<td>3.9</td>
<td>91.9</td>
</tr>
<tr>
<td>5</td>
<td>57.2</td>
<td>12.5</td>
</tr>
<tr>
<td>6</td>
<td>27.3</td>
<td>6.4</td>
</tr>
<tr>
<td>7</td>
<td>3.8</td>
<td>73.5</td>
</tr>
<tr>
<td>8</td>
<td>27.4</td>
<td>59.0</td>
</tr>
<tr>
<td>9</td>
<td>50.1</td>
<td>19.8</td>
</tr>
<tr>
<td>10</td>
<td>26.6</td>
<td>24.1</td>
</tr>
<tr>
<td>11</td>
<td>55.4</td>
<td>26.5</td>
</tr>
<tr>
<td>12</td>
<td>16.9</td>
<td>51.4</td>
</tr>
<tr>
<td>13</td>
<td>41.4</td>
<td>41.2</td>
</tr>
<tr>
<td>14</td>
<td>43.8</td>
<td>5.4</td>
</tr>
<tr>
<td>15</td>
<td>64.0</td>
<td>9.1</td>
</tr>
<tr>
<td>16</td>
<td>4.0</td>
<td>31.8</td>
</tr>
<tr>
<td>17</td>
<td>15.5</td>
<td>77.2</td>
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<tr>
<td>18</td>
<td>7.3</td>
<td>22.4</td>
</tr>
<tr>
<td>19</td>
<td>52.9</td>
<td>1.8</td>
</tr>
<tr>
<td>20</td>
<td>6.1</td>
<td>5.7</td>
</tr>
</tbody>
</table>
Table 3. Reference and estimated land use fractions (%) averaged over the reference area (2002-2003 season).

<table>
<thead>
<tr>
<th>Land Use Fractions</th>
<th>Orchard</th>
<th>Bare Soil</th>
<th>Annual Crop</th>
</tr>
</thead>
<tbody>
<tr>
<td>Derived from high spatial resolution data</td>
<td>22.3</td>
<td>50.9</td>
<td>26.8</td>
</tr>
<tr>
<td>Derived from MODIS with the endmembers extracted on the whole area</td>
<td>18.7</td>
<td>57.4</td>
<td>23.9</td>
</tr>
<tr>
<td>Derived from MODIS with the endmembers extracted on the reference area</td>
<td>23.1</td>
<td>53.1</td>
<td>23.7</td>
</tr>
</tbody>
</table>
Table 4. Statistical variables calculated between the estimated and the reference land use fractions (2002-2003 season, 1km spatial resolution); estimates are provided by the linear unmixing model applied with the endmembers extracted on the whole area (left part) and on the reference area (right part).

<table>
<thead>
<tr>
<th>Land class</th>
<th>Whole area</th>
<th>Reference area</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$R^2$</td>
<td>RMSE</td>
</tr>
<tr>
<td>Orchard</td>
<td>0.69</td>
<td>0.11</td>
</tr>
<tr>
<td>Bare soil</td>
<td>0.90</td>
<td>0.12</td>
</tr>
<tr>
<td>Annual crop</td>
<td>0.81</td>
<td>0.11</td>
</tr>
</tbody>
</table>
Table 5. Observed and estimated land use fractions (%) averaged over the 3 km x 3 km R3 area (2002-2003 season).

<table>
<thead>
<tr>
<th></th>
<th>Orchard</th>
<th>Bare soil</th>
<th>Annual crop</th>
</tr>
</thead>
<tbody>
<tr>
<td>land use fractions observed at ground</td>
<td>1.7</td>
<td>23.5</td>
<td>74.8</td>
</tr>
<tr>
<td>land use fractions derived from MODIS with the endmembers extracted on the whole area</td>
<td>0.8</td>
<td>30.9</td>
<td>68.3</td>
</tr>
<tr>
<td>land use fractions derived from MODIS with the endmembers extracted on the reference area</td>
<td>3.3</td>
<td>18.7</td>
<td>78.0</td>
</tr>
</tbody>
</table>
Table 6. Estimated land use fractions averaged over the three main irrigated sub-regions for the six years of study (2000-2001 to 2005-2006 agricultural seasons).

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Orchard (%)</td>
<td>36.7</td>
<td>33.9</td>
<td>35.2</td>
<td>35.4</td>
<td>39.2</td>
<td>39.9</td>
<td>36.7</td>
</tr>
<tr>
<td></td>
<td>Bare soil (%)</td>
<td>55.9</td>
<td>62.2</td>
<td>52.0</td>
<td>54.4</td>
<td>52.1</td>
<td>50.5</td>
<td>54.5</td>
</tr>
<tr>
<td></td>
<td>Annual crop (%)</td>
<td>7.3</td>
<td>3.7</td>
<td>12.7</td>
<td>10.0</td>
<td>8.5</td>
<td>9.4</td>
<td>8.6</td>
</tr>
<tr>
<td>NFIS</td>
<td>Orchard (%)</td>
<td>16.6</td>
<td>20.2</td>
<td>17.3</td>
<td>18.3</td>
<td>20.0</td>
<td>17.6</td>
<td>18.3</td>
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<tr>
<td></td>
<td>Bare soil (%)</td>
<td>46.1</td>
<td>72.2</td>
<td>42.8</td>
<td>39.5</td>
<td>40.4</td>
<td>35.3</td>
<td>46.1</td>
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<tr>
<td></td>
<td>Annual crop (%)</td>
<td>37.3</td>
<td>7.6</td>
<td>39.9</td>
<td>42.2</td>
<td>39.5</td>
<td>47.1</td>
<td>35.6</td>
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<tr>
<td>Haouz</td>
<td>Orchard (%)</td>
<td>29.3</td>
<td>31.7</td>
<td>27.1</td>
<td>37.4</td>
<td>37.3</td>
<td>35.5</td>
<td>33.1</td>
</tr>
<tr>
<td></td>
<td>Bare soil (%)</td>
<td>21.7</td>
<td>47.5</td>
<td>16.4</td>
<td>20.0</td>
<td>18.4</td>
<td>17.8</td>
<td>23.6</td>
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<tr>
<td></td>
<td>Annual crop (%)</td>
<td>49.0</td>
<td>20.8</td>
<td>56.5</td>
<td>42.6</td>
<td>44.3</td>
<td>46.7</td>
<td>43.3</td>
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