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1       **Spatial distribution of air temperature in mountainous area**  
2                               **using satellite thermal Infra Red data**

3       **Distribution spatiale de la température de l'air en montagnes à**  
4                               **l'aide des données satellite de l'Infra Rouge Thermique**

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11       **Abstract**

12       Understanding the spatial distribution of air temperature in mountainous areas is essential in  
13       hydrological modelling. In the Moroccan High-Atlas range, the meteorological stations network  
14       is sparse. In order to get additional information, we investigated the thermal infrared data  
15       supplied by the Enhanced Thematic Mapper (ETM+) sensor onboard Landsat 7 satellite.  
16       Brightness temperature derived from ETM+ images is used as a proxy of air temperature to set  
17       up a model that describes its spatial. This model accounts for sun location and topographic  
18       characteristics derived from the SRTM digital elevation model. It was evaluated on the Rheraya  
19       watershed, a 225 km<sup>2</sup> region located within the semi-arid High-Atlas mountain range, using two  
20       different sources of data. The first data set consists in *in-situ* air temperature collected by  
21       meteorological stations installed during the experiment at various altitudes from 1400 to  
22       3200 m. The second data set is satellite estimates of snow-covered areas (SCA) derived from  
23       MODIS images over the whole catchment at 500m spatial resolution.

24       **Key words:** air temperature, Landsat ETM+, snow-covered areas, Moroccan High-Atlas.

# 1      **Résumé**

2      Comprendre la distribution spatiale de la température de l'air dans les zones montagneuses  
3 est essentielle pour la modélisation hydrologique. Dans la chaîne du Haut-Atlas marocain, la  
4 faible densité du réseau de stations météorologiques rend difficile l'obtention de ce paramètre.  
5 Dans ce contexte, nous avons utilisé les données infrarouge thermique fournies par le capteur  
6 Enhanced Thematic Mapper (ETM +) à bord du satellite Landsat 7. La variation relative de la  
7 température de brillance est utilisée pour construire un modèle qui décrit celle de la  
8 température de l'air. Le modèle (MSPAT) prend en compte l'angle d'élévation solaire et les  
9 caractéristiques topographiques provenant du modèle numérique de terrain SRTM avec une  
10 résolution spatiale de 90m. MSPAT a été évalué sur le bassin versant de Rheraya, région de 225  
11 km<sup>2</sup> située dans le massif semi-aride du Haut-Atlas, en utilisant deux types de données  
12 différentes : (1)des chroniques de températures de l'air mesurées partir de stations  
13 météorologiques installées au cours de l'expérience à différentes altitudes de 1400 à 3200 m ;  
14 (2) des images de surfaces enneigées (SCA) estimées à partir d'images MODIS acquises à 500 m  
15 de résolution spatiale sur l'ensemble du bassin versant.

16      **Mots clés:** température de l'air, Landsat ETM+, surface de neige, Haut-Atlas marocain.

## 17      **1. Introduction**

18      Air temperature is an important forcing variable for many environmental models, with a  
19 large range of applications concerning agronomy, hydrology or ecology. In snow hydrology, air  
20 temperature is obviously the main factor to partition liquid from solid precipitation (snowfall). It  
21 can be also used as the main driving variable to estimate snowmelt ([Martinec, 1975](#); [Bloschl, 1991](#); [Brubaker et al., 1996](#), [Richard and Gratton, 2001](#)). Therefore, it is fundamental to obtain  
22 accurate spatially-distributed temperature values for the purpose of hydrological modelling in  
23 snowy areas.

25      Spatial interpolation is widely used to obtain air temperature estimates at any point of  
26 interest. Methods can be of deterministic or stochastic nature and differ according to data  
27 availability and scale of application, and. The most common methods are Kriging and Cokriging  
28 techniques ([Matheron, 1963](#)), Inverse-Distance Weighting ([Legates and Willmont, 1990](#)),  
29 Splining ([Eckstein, 1989](#); [Hutchinson and Gessler, 1994](#)), and Polynomial regression ([Myers, 1990](#)). Many studies were carried out to distribute air temperature based on interpolation

1 methods. Over a large study area in Japan, [Ishida and Kawashima \(1993\)](#) report errors between  
2 1 and 3 K for the interpolation of hourly temperature data cokriged with elevation as an external  
3 drift factor. [Hudson and Wackernagel \(1994\)](#) also used cokriging with elevation for predicting  
4 air temperatures in Scotland, and showed that this technique performed better than simpler  
5 interpolation algorithms. Over smaller areas in Sweden, [Soderstrom and Magnusson \(1995\)](#)  
6 reported interpolation errors between 0.4 K and 1.6 K. All these studies have pointed out that  
7 the results of kriging are highly dependent on the spatial density and distribution of  
8 meteorological stations.

9 In mountainous areas, air temperature is controlled by different factors related to location  
10 and topography ([Hudson and Wackernagel, 1994](#)). Therefore, the use of interpolation methods  
11 cited above may generate substantial errors and biases ([Willmott et al., 1991](#); [Robeson and](#)  
12 [Willmott, 1993](#)). Conventionally, the method of altitudinal lapse rate is used to estimate  
13 temperatures at different elevations ([Dunn and Colohan, 1999](#); [Singh and Singh, 2001](#)). More  
14 sophisticated geostatistical method such as AURELHY ([Bénichou, 1987](#)) aims at accounting for  
15 the effects of additional topographic factors (slope, aspect). However, such methods require a  
16 dense network to be calibrated. This condition is not met in the majority of mountainous areas,  
17 especially in developing countries. Meteorological prediction may offer an alternative, but the  
18 grid of meteorological models is too coarse (1 to 10 km) for retrieving the spatial pattern of air  
19 temperature at a fine resolution over areas with a complex relief.

20 Satellite thermal infrared data allows retrieving the spatial distribution of the surface skin  
21 temperature over extended regions. Several studies, most of them based on coarse resolution  
22 data, aimed at using this information to map air temperature at a regional scale. For instance, the  
23 daily maximum air temperature field can be retrieved with an accuracy of about 2.5 K using land  
24 surface temperatures derived from NOAA-AVHRR ([Vogt et al., 1996, 1997](#)). Due to the low  
25 spatial resolution of these data (1km), these methods appear difficult to operate in mountainous  
26 regions.

27 In this context, the objective of this paper is to investigate thermal infrared satellite data  
28 acquired to improve the description of the spatial distribution of air temperature at a fine  
29 resolution over mountainous areas. The study area is the Rheraya watershed, High-Atlas  
30 mountain range, Morocco. The joint analysis of ETM+ images, meteorological data set and digital  
31 elevation model allowed to set up a model (MSPAT) that simulates continuous (daily time step)  
32 and spatially distributed (90 m resolution) air temperatures. MSPAT simulations are compared  
33 to the altitudinal lapse rate method (LRM). The comparative evaluation of these two models is

1 performed using air temperature recorded from meteorological stations and using snow cover  
2 maps derived from MODIS data at a 500m spatial resolution.

## 3 **2. Datasets**

4 The experiment took place within High-Atlas, a large mountain range in central Morocco  
5 (800km long and 70km wide). The highest peak is Jbel Toubkal, which culminates at 4174m  
6 above sea level. Precipitations in the mountains allow supplying several big irrigated areas in  
7 the surrounding plains (Chaponnière et al., 2005; Boudhar et al., 2007; Chehbouni et al., 2008).  
8 They are very irregular in time and space, which is typical of semi-arid areas. Snowfalls occur  
9 mainly during the winter season (November to April) in the upper parts of watersheds. The  
10 contribution of snowmelt to river flows is significant (between 20 and 45% of the total flows  
11 according to the characteristics of watershed, Boudhar et al. 2009).

12 The experimental data set was collected over the Rehraya atlasic sub-catchment (Fig. 1). This  
13 head watershed covers a surface area of about 225 km<sup>2</sup> and is characterized by a semi-arid and  
14 mountainous climate (precipitation of 360 mm/year at the outlet). The elevation ranges from  
15 1084 to 4167 m, and slopes are very steep, with an average grade of 19%.

16 The experimental data set consist in climatic data, Landat ETM+ and MODIS images, and the  
17 SRTM Digital Elevation Model (DEM).

### 18 **2.1. Climatic data**

19 Air temperatures were recorded by the six meteorological stations located in Fig.1. Their  
20 main topographic characteristics are summarised in Table 1. These characteristics were  
21 retrieved from the DEM in the surroundings each meteorological stations. The stations are all  
22 located within or in the close vicinity of the Rheraya catchment, with a large range of altitudes  
23 (1400m to 3200m) and aspects (from 20° northern to 184° southern exposures).

24 All these stations were equipped with HMP45C probes (Vaisala, Finland) that measure air  
25 temperature and vapour pressure on a half-hourly time step, except at the Caf station where  
26 only minimal and maximal temperatures are available. In order to have a maximal sampling,  
27 data analysis is performed for daily maximum air temperatures. As illustrated in the Fig. 2, the

1 altitude is a principal factor controlling air temperature variation: an average lapse rate of -0.56  
2 °C per 100 meters was observed during winter 2007/2008.

### 3 **2.2. Landsat ETM+**

4 The Enhanced Thematic Mapper (ETM+) sensor is operational onboard the Landsat 7  
5 satellite. ETM+ observes the Earth in seven spectral bands, amongst which one in the thermal  
6 infrared region (ETM+6: 10.40 - 12.50  $\mu\text{m}$ ). ETM+ images are acquired with a regular revisit  
7 time of 16 days at a spatial resolution of 30 m in the solar domain and 60 m for the thermal band  
8 (Table 2). The scene size is 170×183 km when orbiting at an altitude of 705 km. For this study,  
9 six images were available over the Rheraya sub-catchment (Table 3).

### 10 **2.3. MODIS data**

11 The Moderated Resolution Imaging Spectroradiometer (MODIS) is an Earth Observing  
12 System (EOS) instrument on board the Terra and Aqua platforms, launched in December 1999  
13 and May 2002, respectively. The sensor observes the earth from a sun-synchronous position  
14 near the polar orbit at an altitude of 705 km. The sensor scans  $\pm 55^\circ$  from nadir in 36 spectral  
15 bands in the visible, near- and short-wave and thermal infrared parts of the electromagnetic  
16 spectrum. During each scan, 10 along-track detectors per spectral band simultaneously sample  
17 the earth. From its polar orbit, MODIS views the Earth's entire surface ranging from every day at  
18 high latitudes to every other day at low latitudes (Justice et al., 1998).

19 In this article, we used the datasets of the daily surface reflectance product "MOD09GHK",  
20 which is a product computed from the MODIS Level 1B land bands 1-7. Images were ordered  
21 from September 2003 to June 2006 through the Earth Observing System (EOS) data gateway  
22 (<https://wist.echo.nasa.gov>). The main characteristics of MODIS images are provided in Table 4.  
23 In this study, we used surface reflectances acquired at 500m spatial resolution of 500m in the  
24 blue (band 3), the green (band 4) and the short-wave infrared (band 6) part of the  
25 electromagnetic spectrum.

## 2.4. *Digital Elevation Model (DEM)*

The digital elevation model (DEM) used in this study was derived from the Shuttle Radar Topography Mission (SRTM) data, which consists of a specially modified radar system that flew onboard the Space Shuttle Endeavour during an 11-day mission in February of 2000. It is an international project led by the U.S. National Geospatial-Intelligence Agency (NGA), U.S. National Aeronautics and Space Administration (NASA), the Italian Space Agency (ASI) and the German Aerospace Center (DLR). SRTM obtained elevation data on a near-global scale to generate the most complete high resolution digital topographic database of Earth, including three resolution products, of 1 km and 90 m resolutions for the world, and a 30 m resolution for the US (USGS, 2004). All SRTM data are freely available at: <http://srtm.csi.cgiar.org/SELECTION/inputCoord.asp>.

In this study, we used the STRM-DEM version 4 acquired at the full 90m spatial resolution over the area covered by landsat scenes (Latitudes 30°28' - 32°24' North Latitudes, longitudes 9°14' and 9°9' West). Altitude and derivatives (aspect and slope) were calculated through the ENVI DEM extraction module (© 2008 ITT Visual Information Solutions).

## 3. Methodology

ETM+ brightness temperature was first calculated (§3.1), then converted as a proxy of the maximal air temperature images (§3.2). The resulting images were analysed together with derivatives of the SRTM digital elevation model for understanding the topographical factors controlling the air temperature variability (§3.3). This analysis allowed to set up the MSPAT models that simulates continuous (daily time step) and spatially distributed (90 m resolution) air temperatures (§3.4). MSPAT simulations were compared to the altitudinal lapse rate method (LRM, described in §3.5). The comparative evaluation of these two models was performed using air temperature recorded from additional meteorological stations and using snow cover maps derived from MODIS data at a 500m spatial resolution. The snow mapping method is described in section §3.6.

### 1        **3.1.                    Brightness temperature calculation**

2        The computation of brightness temperature from ETM+6 data first requires the conversion of  
3        digital numbers to radiances. For this purpose we used the following formula developed by the  
4        National Aeronautics and Space Administration (Eq. 1, after Markham and Barker 1986).

$$5        L_{(\lambda)} = L_{\min(\lambda)} + (L_{\max(\lambda)} - L_{\min(\lambda)})Q_{dn}/Q_{\max} \quad (\text{Eq. 1})$$

6        where  $L_{(\lambda)}$  is the spectral radiance received by the sensor ( $\text{mWcm}^{-2}\text{sr}^{-1}\mu\text{m}^{-1}$ ),  $Q_{\max}$  is the  
7        maximum recorded (255), and  $Q_{dn}$  is the digital number of the analysed pixel,  $L_{\min(\lambda)}$  and  $L_{\max(\lambda)}$   
8        are the minimum and maximum spectral radiance, detected for  $Q_{dn}=0$  and  $Q_{dn}=255$ , respectively.  
9        For ETM6 with central wavelength of 11.475 mm, it has been set that  $L_{\min(\lambda)}=0.1238$  for  $Q_{dn}=0$   
10        and  $L_{\max(\lambda)} 1.56 \text{ mWcm}^{-2}\text{sr}^{-1}\mu\text{m}^{-1}$  for  $Q_{dn}=255$  (Schneider and Mauser 1996). Thus, the above  
11        equation can be simplified into the following form:

$$12        L_{(\lambda)} = 0.1238 + 0.005632156Q_{dn} \quad (\text{Eq. 2})$$

13        Once the spectral radiance  $L_{(\lambda)}$  is computed, the brightness temperature at the satellite level  
14        can be directly calculated either by inverting Planck's radiance function for temperature  
15        (Sospedra et al. 1998) or by using approximation formula (Eq. 3, after Schott and Volchok, 1985,  
16        Wukelic et al., 1989, Goetz et al., 1995 :

$$17        T_B = \frac{K_2}{\ln\left(\frac{K_1}{L} + 1\right)} \quad (\text{Eq. 3})$$

18        Where,  $T_B$  is the brightness temperature and  $K_1$  and  $K_2$  are pre-launch calibration constants:  
19         $K_1= 607.76 \text{ mWcm}^{-2}\text{sr}^{-1}\mu\text{m}^{-1}$  and  $K_2=1260.56 \text{ degK}$ , respectively (Schneider and Mauser, 1996).

### 20        **3.2.                    Derivation of Maximal Air Temperature from ETM+**

21        Maps of maximal air temperatures were established on the Rheraya watershed by combining  
22        ETM+ images and local measurements, with the assumption that air and brightness  
23        temperatures ( $T_b$ ) are linearly related. **In principle, there is a tight coupling between the surface**  
24        **and the air temperature under bare soil conditions. Coupling can also be strong when snowpack**



1 is below zero degree. Under melting conditions, snow surface is close to zero degree and there is  
2 little coupling with the air above. However, Tb distributions according to slope and elevation can  
3 be used as additional information to distribute spatially the variations in available melting  
4 energy (radiative or sensible heat) in all conditions for use within empirical degree days models  
5 (Boudhar et al., submitted). It's therefore a proxy for these variations rather than a fully  
6 deterministic variable. For each image, the brightness temperatures (Tb) of the pixels that  
7 include weather stations were extracted and compared with maximal air temperatures (Tam)  
8 obtained from the meteorological stations. It appeared that Tb was well correlated with Tam,  
9 with a correlation coefficient  $R^2$  of 0.82 (Fig. 3). Tam were thus calculated for Tb using a unique  
10 regression equation ( $Tam = 0.7 * Tb - 3.2$ ) that was successively applied on each image.

### 11 **3.3. Analysis of Maximal Air Temperature Variation**

12 Fig. 4 represents an example of the co-variation of maximal air temperature and altitude over  
13 the Rheraya watershed in 27/02/2003. Not surprisingly, the two variables were found highly  
14 correlated, with a decrease by 18 °C of air temperature associated to a 3000 m difference in  
15 elevation. This corresponds to an equivalent lapse rate value of 0.60°/100m. Not shown here,  
16 the Tam versus elevation curves extracted for the remaining images display the same pattern,  
17 with lapse rates varying between 0.43°/100m to 0.75°/100m. These values appear consistent  
18 with that of an international standard atmosphere (0.65 °C/100 m according to the International  
19 Civil Aviation Organization).

20 Fig. 5 provides an example of air temperature variations with aspect in February 27, 2003.  
21 The aspect values are expressed in degrees, with the values 0° (or 360°), 90°, 180° and 270°  
22 corresponding to the facing North, East, South and West, respectively. A difference of 10°C in air  
23 temperature between northern and southern exposures was observed this day. The variations of  
24 air temperature with aspect followed a sinusoidal curve centred on about 140°, in coherence  
25 with the sun diurnal course (the sun azimuthal angle is 165° at the time of acquisition).

26 A deeper investigation shows that the dependence of Tam with aspect is function of altitude,  
27 slope and sun elevation. Fig. 6 presents the amplitude of Tam variations with aspects for seven  
28 altitudinal zones from 1000 to 4200 m (with steps of 400 m), together with slopes. Variations of  
29 Tam with exposures match the altitudinal distribution of slopes, especially during the winter  
30 period when the sun elevation is low. For the ETM+ image acquired in May with a maximal sun  
31 elevation of 77°, this effect appears very limited.

### 3.4. Spatial distribution of Air Temperature (MSPAT model)

The air temperature in any point  $Tam(i,j)$  of the Rheraya sub catchment's was calculated from the air temperature recorded at one reference meteorological station ( $Tam(I_{ref},J_{ref})$ , OukaSM and Armed stations, and topographical differences between this point and the reference station. These differences were accounted for using the MSPAT model with the altitude, exposition and slope extracted at the pixel  $(i,j)$  and at the location of the reference station (Eq. 6). The MSPAT was set up to obtain daily images of maximal air temperature at a 90m spatial resolution.

$$Tam_{(i,j)} = Tam_{(ref)} + (G \times \Delta Alt) - A \times \left[ \cos \left( \frac{AS_{(i,j)} \cdot \pi}{180} \right) - \cos \left( \frac{AS_{ref} \cdot \pi}{180} \right) / 2 \right] \quad (\text{Eq. 6})$$

where :

$G$  is the air temperature lapse rate calculated from the two reference meteorological stations (Armed and OukaSM) at a daily time step

$\Delta Alt = Alt_{(i,j)} - Alt_{(ref)}$  is the difference in elevation between the reference station and the pixel where air temperature is calculated.

$AS(i,j)$  and  $AS_{ref}$  are the aspect in degree of the pixel  $(i, j)$  and of the reference station, respectively.

. For a given altitude, the model accounts for aspect, slope and sun elevation according to equations (Eq. 7 and Eq. 8). In details, the air temperature was calculated from the temperature averaged for a given altitudinal band with a correction of the effect of exposure based on a cosine function (Eq. 7). The maximal air temperature was logically supposed to be the highest when the surface is fully oriented at South (aspect of  $180^\circ$ ). The amplitude of the cosine was adjusted as a function of the ratio of the local slope to the sun elevation (A coefficient in Eq. 8 and Fig. 7).

$$Tam_z = \overline{Tam_z} - A \times \cos \left( \frac{AS_z}{180 \times \pi} \right) \quad (\text{Eq. 7})$$

$$A = 0.22 \cdot \left(\frac{SE}{SL}\right)^2 - 2.52 \cdot \left(\frac{SE}{SL}\right) + 8.37 \quad (\text{Eq. 8})$$

Where  $Tam_z$  is the maximal air temperature for a pixel of altitude  $z$  and aspect  $AS_z$  in degree.  $Tam_z$  is the mean of maximal air temperature for the altitudinal zone  $z$ .  $A$  is a coefficients depending of date and altitudinal zone.  $SE$  and  $SL$  are the sun elevation angle and the slope, both in degree.

### 3.5. Lapse rate method (LRM)

In the lowest 10-15 km of the atmosphere, temperature declines with an increase in altitude. This decline, known as temperature lapse rate, is controlled by the balance between heat convection from the surface and radiative cooling. However, lapse rates vary with: (1) altitude, (2) season, (3) latitude, and (4) interactions between topography and weather (e.g. dry versus moist air and inversions).

The lapse rate method (LRM) takes the maximum air temperature observed at a reference station and extrapolates that value over the entire basin via a functional relationship between air temperature and elevation data. This method assumes 1) a linear relationship between air temperature and elevation, and 2) horizontal gradients due to topographic and orographic effects are negligible. In this study, the temperature lapse rates ( $G$ ) on a daily basis using the stations were the longest dataset is available as:

$$G = \frac{Tam1 - Tam2}{Alt1 - Alt2} \quad (\text{Eq. 4})$$

Where  $Tam1$  and  $Tam2$  are the values of maximum air temperature measured at the Armed station and OukaSM stations, respectively.  $Alt1$  and  $Alt2$  are the elevations of these two stations.

Air temperature lapse rates were calculated for each study year and then applied to elevation data for Rheraya basin to determine air temperature for each pixel using air temperature measured at a reference station ( $Tam(I_{ref}, J_{ref})$ ) (Eq. 5).

$$Tam_{(i,j)} = Tam_{(ref)} + (G \times \Delta Alt) \quad (\text{Eq. 5})$$

where :

1  $\Delta Alt = Alt_{(i,j)} - Alt_{(ref)}$  is the difference in elevation between the reference station  
2 (OukaSM and Armed) and the pixel where air temperature is calculated.

### 3 **3.6. Estimates of snow-covered areas (SCA)**

4 Snow-covered areas were estimated using two methods: (1) Simulation of snowfall and  
5 snowmelt, (2) Mapping using MODIS images.

#### 6 • **Simulation**

7 The snow cover fraction (SCA) was parameterized as an asymptotically function of the snow  
8 water equivalent (SWE) according to equation (Eq. 9) (Anderson, 1976).

$$9 \quad SCA = SCA_{\max} \times \tanh(100 \times SWE) \quad (\text{Eq. 9})$$

10 Where SWE is the snow water equivalent (in mm), and SCAMax is the maximum allowed  
11 snow cover fraction, set to 0.95.

12 SWE was calculated as the balance between the accumulations processes (snowfall) and the  
13 ablation processes (snowmelt). During precipitation events, SWE increased by the daily snowfall  
14 if the mean air temperature is below 0°C, otherwise precipitation is rain. Snowmelt was  
15 calculated with a classical temperature index described in Equation 10.

$$16 \quad M_s = \begin{cases} a \cdot (T_d - T_0), & T_d > T_0 \\ 0, & T_d \leq T_0 \end{cases} \quad (\text{Eq. 10})$$

17 Where  $M_s$  is the daily bulk loss of water from the snowpack (mm/day);  $T_d$  is the mean daily  
18 air temperature (°C);  $T_0$  is the base temperature (0°C); and  $a$ , the degree-day factor  
19 (mm/°C/day). The later is computed as 1.1 multiplied by the ratio of snow and water densities  
20 (Martinec, 1975).

21 Two sets of simulations were performed for years 2003/2004, 2004/2005 and 2005/2006  
22 over the entire Rheraya watershed using a 90m spatial grid, with the air temperature spatially  
23 distributed either with the MSPAT model or with the simple lapse rate method. In both case, the

1 precipitations are distributed using the precipitations recorded at the ARMED station and an  
2 average observed elevation gradient of 0.03 mm/100m (Boudhar et al., 2009).

3 • **Mapping**

4 To select the cloud-free data, we initially eliminated the images showing high reflectances in  
5 the blue band (on average higher than 20%) over the lower-lying areas close to the High-Atlas  
6 (approximately 5000 snow-free pixels, where the altitude is lower than 1000 meters). Indeed,  
7 these high reflectances are due to the presence of clouds on the Atlas foothills, and therefore  
8 probably on nearby Atlas summits. In a second phase, we identified clouds on the remaining  
9 images by visual examination. After this filtering phase, the number of useful images is  
10 respectively 44, 52 and 82 for the seasons 2003/2004, 2004/2005 and 2005/2006 (equivalent  
11 of 1 image per week).

12 The snow-mapping algorithm makes use of the contrast of reflectances between a visible  
13 band (MODIS band 4, 0.545–0.565  $\mu\text{m}$ ) and shortwave infrared band (MODIS band 6, 1.628–  
14 1.652  $\mu\text{m}$ ). These two bands were combined to calculate the normalized difference snow index  
15 (NDSI, Eq. 11), which is a proxy of SCA (Hall et al., 2002).

16 
$$NDSI = \frac{B_4 - B_6}{B_4 + B_6} \text{ (Eq. 11)}$$

17 Where  $B_4$  and  $B_6$  are the reflectances in the 4<sup>th</sup> and the 6<sup>th</sup> MODIS spectral bands.

18 In order to reduce errors due to variations of the background reflectance, we used the  
19 Modified Normalized Difference Snow Sndex (MNDSI, Eq. 12). This approach was successfully  
20 tested by Chaponniere et al., 2005 using a snow indices specifically designed for the SPOT-  
21 VEGETATION sensor. This methodology was applied for all cloud-free MODIS images acquired  
22 during three years from 2003 to 2005.

23 
$$MNDSI = NDSI - NDSI_0 \cdot \frac{NDSI_{100} - NDSI}{NDSI_{100} - NDSI_0} \text{ (Eq. 12)}$$

24  $NDSI_0$  is the snow index of totally snow-free surfaces (computed, for each pixel, from images  
25 acquired in summer), and  $NDSI_{100}$  are the snow index of pixels totally covered with snow (one  
26 single value was fixed as the maximum of  $NDSI$  on images acquired during winter).

## 4. Results and discussion

### 4.1. *Model evaluation at Local scale*

Daily maximum air temperatures modelled using MSPAT at the location of meteorological stations were evaluated against all measurements available over the Rheraya watershed, together with estimates of air temperature based on the lapse rate method (referred to as “LRM”). The evaluation was carried out using classical statistical variables (RMSE, BIAS, and  $R^2$ ).

Fig. 8 present the scatter plots between observed and simulated air temperatures during the 2007/2008 season, year with the largest number of available climatic data. Table 5 shows the statistical variables obtained by comparing the predictions and the measurements of daily maximum daily air temperature on an annual basis. Biases and RMSE were null for the Armed station which provides with the reference air temperature. Bias was also null for the OukaSM station since it was used for calculating the altitudinal lapse rate. From the statistics calculated on the remaining stations, we noted that the performance of LRM and MSPAT models were similar, with moderate to excellent correlation ( $R^2$  from 0.35 to 0.94), low biases (from  $-0.5^\circ$  to  $1.2^\circ$ ) and error varying from 1 to  $3.2^\circ$ . The MSPAT model performed slightly better than the LRM method for 2 stations (Caf and Neltner), whereas it is the opposite for 2 others (Imsker and Tachdert). These results shown that, at local scale, the MSPAT model did not improve the estimate of air temperature.

### 4.2. *Catchment scale*

The snow-covered areas derived from MODIS data and simulated with climatic data (LRM and MSPAT models) were compared for the three seasons of study (2003-2004 to 2005-2006). The time series of SCAs averaged on the whole Rheraya watershed were plotted in Fig. 9. The two simulated snow covered area compared favourably to that derived from MODIS images. However, there was a slight underestimation of SCA simulated using the LRM method during the two previous years (2003 to 2005) and a slight overestimation of SCA simulated using the MSPAT model at the begin of the last year (December 2005). The peaks of SCA were well modelled with the two methods, even thought those occurring after generalized snowfall events were clearly underestimated. This smoothing effect was due to the use of an asymptotic function between SCA and snow water equivalent.

1       The Fig. 10 show three examples of SCA maps simulated by the two climatic models and  
2 derived from MODIS data during a snowmelt period between 03/12/2003 and 30/12/2003.  
3 Simulated SCA appeared much more realistic when the MSPAT model was used to distribute air  
4 temperature. This was obvious on the two first dates when looking at the north-eastern and at  
5 the western part of the catchment, as well as for the last date for which the spatial extent of  
6 snowy areas simulated using the LRM data pattern appeared too limited. This qualitative  
7 comparison allowed to show that patterns of SCA were not only matching altitude variations but  
8 also exposures. This was consistent with previous studies carried out at the scale of the whole  
9 High-Atlas mountains range showing that southern facing slopes have lower SCA than northern  
10 ones (Boudhar et al., 2007).

11       The scatter plot between SCA simulated by the two climatic models and derived from MODIS  
12 allowed to quantify the previous findings (Fig. 11). This comparison was carried out at a  
13 degraded resolution of 2km<sup>2</sup> in order to limit the impact of miss-registration between MODIS  
14 and simulated SCA images. SCA modelled with LRM model were found very under-estimated,  
15 especially during seasons 2004/2005 and 2005/2006. In contrast, SCA modelled using the  
16 MSPAT were less scattered. The statistics results for each season are summarized in Table 6. We  
17 noted a remarkable improvement of the SCA modelled with MSPAT model. This improvement  
18 was significant in the two seasons 2004/2005 and 2005/2006 with decreasing in bias by 2.9 and  
19 1.8%, respectively. Theses differences in SCA estimating between LRM and MSPAT models are  
20 due principally to the aspect effect not taken account by LRM formulation. In the later, air  
21 temperature varies only with altitude and horizontal gradients due to topographic and  
22 orographic effects are negligible.

## 23       **5. Conclusion**

24       This study focused on testing a method of air temperatures spatial variation, principally  
25 developed for high-relief mountain environments with scarce meteorological data. The thermal  
26 infrared band of Enhanced Thematic Mapper (ETM+) images was used to calculate the  
27 brightness temperature. Brightness temperatures were compared with maximal air temperature  
28 measured in meteorological stations available, and the correlation equation obtained allowed to  
29 compute maps of a proxy of the maximal air temperature. This information was used to  
30 characterize its spatial variation according to topographic factors (elevation, aspect and slope)  
31 and solar elevation angle. From this, we set up a model to spatialise air temperature.

1 The results of air temperature simulation with MSPAT model was compared with lapse rate  
2 model (LRM). The simulated air temperatures with the two models were similar at the location  
3 of available meteorological stations. Over all the study area, the models were evaluated using  
4 snow cover area (SCA) estimates. The last are then compared with SCA product mapped from  
5 MODIS data. Results showed that MSPAT model had a considerable improvement on the  
6 modelling SCA. It is thus believed that the pseudo air temperature approximated using ETM+  
7 brightness temperature may be useful to monitor the dynamics of snowpacks. The approach  
8 developed here may be beneficial for hydrological applications, especially snowmelt modelling  
9 at watershed scale with scarce data.

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